Principles of Concurrent Programming

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To Margalit
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Concurrent programming—the programming tools and techniques for dealing with parallel processes—has traditionally been a topic in operating systems theory texts. There are several reasons why concurrent programming deserves a book of its own and should be the core of an advanced computer science systems course:

1. Concurrent programming is what distinguishes operating systems and real-time systems from other software systems. Computer science students who have taken courses in programming, data structures, computer architecture and probability can easily master the applications of these disciplines in operating systems, but they need to be introduced to techniques that will enable them to deal with parallelism.

2. I doubt if many of my students will ever design or construct a multiprocessor time-sharing system where algorithms for paging and scheduling are of prime importance. I am certain that they will be designing and constructing real-time systems for mini- and microcomputers. A sound knowledge of concurrent programming will enable them to cope with real-time systems—in particular with the severe reliability requirements that are imposed.

3. There is a trend towards increasing use of abstract concurrency that has nothing to do with the parallelism of actual systems. Data flow diagrams used in software engineering are nothing more than networks of concurrent processes. Traditionally, such a design must be implemented in a sequential language, but UNIX† is a programming system which encourages the use of concurrent processes. Ada‡, the new language designed for the U.S. Department of Defense, includes concurrent programming features as an integral part of the language.

† UNIX is a trademark of Bell Laboratories.
‡ Ada is a trademark of the United States Dept. of Defense.
4. Finally, concurrent programming is an important topic in computer science research. The basic results in the field are still scattered throughout the literature and deserve to be collected into one volume for a newcomer to the field.

The book requires no prerequisites as such other than computer science maturity (to borrow the term from mathematics). The book is aimed at advanced undergraduate students of computer science. At the Tel Aviv University, we arrange the course of study so that a student has four semesters of computer science courses which include extensive programming exercises. The material is also appropriate for practicing systems and real-time programmers who are looking for a more formal treatment of the tools of their trade.

I have used the material for half of a weekly four-hour semester course in operating systems—the second half is devoted to the classical subjects: memory management, etc. I should like to see curricula evolve that would devote a quarter or trimester to (theoretical) concurrent programming followed by a project oriented course on operating systems or real-time systems.

The book is not oriented to any particular system or technique. I have tried to give equal time to the most widespread and successful tools for concurrent programming: memory arbiters, semaphores, monitors and rendezvous. Only the most elementary features of Pascal and Ada are used; they should be understandable by anyone with experience in a modern programming language.

Much of the presentation closely follows the original research articles by E. W. Dijkstra and C. A. R. Hoare. In particular, Dijkstra's *Co-operating Sequential Processes* reads like a novel and it was always great fun to lecture the material. This book is an attempt to explain and expand on their work.

Verification of concurrent programs is one of the most exciting areas of research today. Concurrent programs are notorious for the hidden and sophisticated bugs they contain. Formal verification seems indispensable. A novel feature of this book is its attempt to verify concurrent programs rigorously though informally. Hopefully, a student who is introduced early to verification will be prepared to study formal methods at a more advanced level.

One cannot learn any programming technique without practicing it. There are several programming systems that can be used for class exercise. For institutions where no such system is available, the Appendix contains the description and listing of a simple Pascal-S based concurrent programming system that I have used for class exercise.
ACKNOWLEDGEMENTS

I am grateful to Amiram Yehudai for the many discussions that we have had over the past few years on programming and how to teach it. He was also kind enough to read the entire manuscript and suggest improvements.

I should also like to thank Amir Pnueli for teaching me programming logic and verification, and Henry Hirschberg of Prentice/Hall International for his encouragement during the transition from notes to book.

Also, special thanks to my wife Margalit for drawing the sketches on which the illustrations were based.
Principles of Concurrent Programming
1 WHAT IS CONCURRENT PROGRAMMING?

1.1 FROM SEQUENTIAL TO CONCURRENT PROGRAMMING

Figure 1.1 shows an interchange sort program. The program can be compiled into a set of machine language instructions and then executed on a computer. The program is sequential; for any given input (of 40 integers) the computer will always execute the same sequence of machine instructions.

If we suspect that there is a bug in the program then we can debug by tracing (listing the sequence of instructions executed) or by breakpoints and snapshots (suspending the execution of the program to list the values of the variables).

There are better sequential sorting algorithms (see Aho et al., 1974) but we are going to improve the performance of this algorithm by exploiting the possibility of executing portions of the sort in parallel. Suppose that (for \( n=10 \)) the input sequence is: 4, 2, 7, 6, 1, 8, 5, 0, 3, 9. Divide the array into two halves: 4, 2, 7, 6, 1 and 8, 5, 0, 3, 9; get two colleagues to sort the halves simultaneously: 1, 2, 4, 6, 7 and 0, 3, 5, 8, 9; and finally, with a brief inspection of the data, merge the two halves:

\[
\begin{align*}
0 \\
0, 1 \\
0, 1, 2 \\
\ldots
\end{align*}
\]

A simple complexity analysis will now show that even without help of colleagues, the parallel algorithm can still be more efficient than the sequential algorithm. In the inner loop of an interchange sort, there are \((n-1) + (n-2) + \ldots + 1 = n(n-1)/2\) comparisons. This is approx. \(n^2/2\). To sort \(n/2\)
program sortprogram;
const n=40;
var  a: array[1..n] of integer;
    k: integer;
procedure sort(low,high: integer);
var  i,j, temp: integer;
begin
  for i := low to high-1 do
    for j := i+1 to high do
      if a[j] < a[i] then
        begin
          temp := a[j];
          a[j] := a[i];
          a[i] := temp
        end;
  begin (* main program *)
    for k := 1 to n do read (a[k]);
    sort (1, n);
    for k := 1 to n do write (a[k])
  end.

Fig. 1.1.

elements, however, requires only \((n/2)^2/2 = n^2/8\) comparisons. Thus the parallel algorithm can perform the entire sort in twice \(n^2/8 = n^2/4\) comparisons to sort the two halves plus another \(n\) comparisons to merge. The table in Fig. 1.2 demonstrates the superiority of the new algorithm. The last column shows that additional savings can be achieved if the two sorts are performed simultaneously.

<table>
<thead>
<tr>
<th>(n)</th>
<th>(n^2/2)</th>
<th>((n^2/4)+n)</th>
<th>((n^2/8)+n)</th>
</tr>
</thead>
<tbody>
<tr>
<td>40</td>
<td>800</td>
<td>440</td>
<td>140</td>
</tr>
<tr>
<td>100</td>
<td>5000</td>
<td>2600</td>
<td>1350</td>
</tr>
<tr>
<td>1000</td>
<td>500 000</td>
<td>251 000</td>
<td>126 000</td>
</tr>
</tbody>
</table>

Fig. 1.2.

Figure 1.3 is a sequential program for this algorithm. It can be executed on any computer with a Pascal compiler and it can be easily translated into other computer languages.
program sortprogram;
const n=20;
  twon=40;
var  a: array[1..twon] of integer;
  k: integer;
procedure sort(low, high: integer);
  (* as before *)
procedure merge(low, middle, high: integer);
var  count1, count2: integer;
  k, index1, index2: integer;
begin
  count1 := low;
  count2 := middle;
  while count1 < middle do
    if a[count1] < a[count2] then
      begin
        write (a[count1]);
        count1 := count1+1;
        if count1 >= middle then
          for index2 := count2 to high do
            write(a[index2])
      end
    else
      begin
        write (a[count2]);
        count2 := count2+1;
        if count2 > high then
          begin
            for index1 := count1 to middle-1 do
              write (a[index1]);
            count1 := middle (* terminate *)
          end
      end
  end;
begin (* main program *)
  for k := 1 to twon do read (a[k]);
  sort(1, n);
  sort(n+1, twon);
  merge(1, n+1, twon)
end.

Fig. 1.3.
Suppose that the program is to be run on a multiprocessor computer—a computer with more than one CPU. Then we need some notation that can express the fact that the calls sort(1,n) and sort(n+1, twon) can be executed in parallel. Such a notation is the cobegin-coend bracket shown in Fig. 1.4. cobegin p_1; \ldots ; p_n coend means: suspend the execution of the main program; initiate the execution of procedures p_1, \ldots , p_n on multiple computers; when all of p_1, \ldots , p_n have terminated then resume the main program.

\begin{verbatim}
program sortprogram;
  (*declarations as before *)
begin (* main program *)
  for k := to twon do read(a[k]);
  cobegin
    sort(1, n);
    sort(n+1, twon)
  coend;
  merge(1, n+1, twon)
end.
\end{verbatim}

Fig. 1.4.

The programs of Figs. 1.3 and 1.4 are identical except for the cobegin-coend in Fig. 1.4. There would be no need for both versions if the definition of cobegin-coend was modified. Instead of requiring that the procedures be executed in parallel, cobegin-coend becomes a declaration that the procedures may be executed in parallel. It is left to the implementation—the system hardware and software—to decide if parallel execution will be done. Processors may be added or removed from the system without affecting the correctness of the program—only the time that it would take to execute the program.

The word concurrent is used to describe processes that have the potential for parallel execution. We have shown how an algorithm can be improved by identifying procedures that may be executed concurrently. While the greatest improvement is obtained only under true parallel execution, it is possible to ignore this implementation detail without affecting the superiority of the concurrent algorithm over the sequential algorithm.

1.2 CONCURRENT PROGRAMMING

Concurrent programming is the name given to programming notations and techniques for expressing potential parallelism and for solving the resulting synchronization and communication problems. Implementation of parallelism is a topic in computer systems (hardware and software) that is essentially
independent of concurrent programming. Concurrent programming is important because it provides an abstract setting in which to study parallelism without getting bogged down in the implementation details. This abstraction has proved to be so useful in writing clear, correct software that modern programming languages offer facilities for concurrent programming.

The basic problem in writing a concurrent program is to identify which activities may be done concurrently. If the merge procedure is also included in the \texttt{cobegin–coend} bracket (Fig. 1.5), the program is no longer correct. If you merge the data in parallel with sorting done by your two colleagues, the scenario of Fig. 1.6 might occur.

\begin{verbatim}
\texttt{cobegin}
\texttt{    sort(1, n);}
\texttt{    sort(n+1, twon);}
\texttt{    merge(1, n+1, twon)}
\texttt{coend}
\end{verbatim}

\textbf{Fig. 1.5.}

\begin{center}
\begin{tabular}{llll}
\hline
 & \texttt{Colleague1} & \texttt{Colleague2} & \texttt{You} \\
\hline
Initially & 4, 2, 7, 6, 1 & 8, 5, 0, 3, 9 & – \\
\texttt{Colleague1} exchanges & 2, 4, 7, 6, 1 & 8, 5, 0, 3, 9 & – \\
\texttt{Colleague2} exchanges & 2, 4, 7, 6, 1 & 5, 8, 0, 3, 9 & – \\
\texttt{You merge} & ” & ” & 2 \\
\texttt{You merge} & ” & ” & 2, 4 \\
\texttt{You merge} & ” & ” & 2, 4, 5 \\
\hline
\end{tabular}
\end{center}

\textbf{Fig. 1.6.}

However, \texttt{merge} could be a concurrent process if there were some way of synchronizing its execution with the execution of the sort processes (Fig. 1.7).

\begin{verbatim}
\texttt{while count1 < middle do}
\texttt{    wait until i of procedure call sort(1, n) is greater than count1 and i of}
\texttt{    procedure call sort(n+1, twon) is greater than count2 and only then:}
\texttt{        if a[count1] < a[count2] then}
\texttt{          …}
\end{verbatim}

\textbf{Fig. 1.7.}

Parallelism is important not only for the improvement that can be achieved in program performance but also in program quality. Consider the
following problem:

Read 80-column cards and print them on 125-character lines. However, every run of \( n = 1 \) to 9 blank spaces is to be replaced by a single blank followed by the numeral \( n \).

This program is difficult to write as a sequential program. There are many interacting special cases: a run of blanks overlapping the end of a card, the pair blank-\( n \) overlapping the end of a line and so on. One way to improve the clarity of the program would be to write three separate programs: one to read cards and write a stream of characters onto a temporary file; a second program to read this character stream and modify runs of blanks, writing the new stream onto a second temporary file; and a third program to read the second temporary file and print lines of 125 characters each.

This solution is not acceptable because of the high overhead of the temporary files. However, if the three programs could be run concurrently (not necessarily in parallel) and communications paths could be established between them, then the programs would be both efficient and elegant.

\[
\begin{array}{cccc}
\text{INPUT} & \text{Deformat cards} & \text{Modify runs of blanks} & \text{Format lines} & \text{OUTPUT} \\
\text{Sequence of cards} & P_1 & P_2 & P_3 & \text{Sequence of lines}
\end{array}
\]

Processes \( P_1, P_2, P_3 \) may execute concurrently

### 1.3 Correctness of Concurrent Programs

Concurrent programming is much more difficult than sequential programming because of the difficulty of ensuring that a concurrent program is correct. Consider the sequential sort programs of Figs. 1.1 and 1.3: if they were tested on several sets of input data then we would feel confident that they are correct. Guidelines for testing would be to include a sorted input, a reversed input, an input all of whose elements are identical and so on. A run-of-the-mill bug (such as an incorrect for-loop limit) would seldom escape detection.

The scenario in Fig. 1.6 illustrates that the concurrent program of Fig. 1.5 is incorrect. However, this program is not a sequential program and other scenarios exist. If the processors assigned to sort are sufficiently rapid then merge may always be working on sorted data. In that case, no amount of testing would detect any problem. One day (perhaps months after the program has been put into production) an improved component in the computer system causes the merge to speed up and then the program gives incorrect answers as demonstrated in 1.6. Of course the natural reaction is:
This program worked yesterday so the new component must be at fault."

A scenario is a description of a possible execution sequence of a program and shows how a computer might "act out" a program. It is usually used to show that a program is incorrect: since the computer may execute the program in a manner that produces the wrong answer, the program cannot be correct.

Conversely, how can we show that the concurrent program in Fig. 1.4 is correct? It no longer makes sense to look for and test paths that can be execution sequences. At times, there may be two such sequences caused by parallel execution of the algorithm.

Sequential programming has a well-developed proof theory. Assertions are made about the state of the computer (i.e. the values of the variables and the program counter) before and after executing an instruction, and these are then combined into a logical proof. In concurrent programming, this method needs to be modified because the programs can interfere with each other.

The correctness assertions for procedures sort and merge of the previous sections are elementary to state and prove:

sort input assertion: a is an array of integers,

sort output assertion: a is "sorted", i.e. a now contains a permutation of the original elements and they are in ascending order,

merge input assertion: the two halves of a are "sorted",

merge output assertion: the elements of a have been written in ascending order.

The correctness of the program in Fig. 1.4 is immediate from the correctness of procedure sort. The correctness of 1.3 is easily obtained by concatenating the correctness proofs of sort and merge. The correctness of Fig. 1.4 needs a new technique. We have to be able to express the fact that the two instances of sort do not interfere with one another. The program in Fig. 1.5 is incorrect though the procedures comprising it are correct; unfortunately, they interact in a manner which makes the program incorrect. The program in 1.7 is correct but new ideas are needed to be able to reason about synchronization.

1.4 INTERLEAVING

Interleaving is a logical device that makes it possible to analyze the correctness of concurrent programs. Suppose that a concurrent program P consists of two processes P₁ and P₂. Then we say that P executes any one of the execution sequences that can be obtained by interleaving the execution sequences of the two processes. It is as if some supernatural being were to execute the instructions one at a time, each time flipping a coin to decide whether the next instruction will be from P₁ or P₂.
We claim that these execution sequences exhaust the possible behaviors of \( P \). Consider any instructions \( I_1 \) and \( I_2 \) from \( P_1 \) and \( P_2 \), respectively. If \( I_1 \) and \( I_2 \) do not access the same memory cell or register then it certainly does not matter if \( I_1 \) is executed before \( I_2 \), after \( I_2 \) or even simultaneously with \( I_2 \) (if the hardware so allows). Suppose on the other hand that \( I_1 \) is "Store 1 into memory cell M" and that \( I_2 \) is "Store 2 into memory cell M". If \( I_1 \) and \( I_2 \) are executed simultaneously then the only reasonable assumption is that the result is consistent. That is, cell M will contain either 1 or 2 and the computer does not store another value (such as 3) of its own volition.

If this were not true then it would be impossible to reason about concurrent programs. The result of an individual instruction on any given data cannot depend upon the circumstances of its execution. Only the external behavior of the system may change—depending upon the interaction of the instructions through the common data. In fact, computer hardware is built so that the result of executing an individual instruction is consistent in the way just defined.

Thus, if the result of the simultaneous execution of \( I_1 \) and \( I_2 \) is 1 then this is the same as saying that \( I_1 \) occurred before \( I_2 \) in an interleaving and conversely if the result is 2.

Interleaving does not make the analysis of concurrent programs simple. The number of possible execution sequences can be astronomical. Nevertheless, interleaved execution sequences are amenable to formal methods and will allow us to demonstrate the correctness of concurrent programs.

### 1.5 THE ORIGIN OF OPERATING SYSTEMS

Concurrent programming, though generally applicable, grew out of problems associated with operating systems. This section outlines the development of such systems so that the background to the growth of concurrent programming can be appreciated.

It is not often that an obsolete technology reappears. Programmable pocket calculators have resurrected machine language programming: absolute addresses must be used for data and labels. On the other hand, the owner is not constrained to working during the hours that the computer center is open.

While the pocket calculator is a marvel of electronics, machine language programming directly on the computer is slow and difficult. In the 1950s, when computers were few and expensive, there was great concern over the waste caused by this method. If you signed up to sit at the computer console from 0130 to 0200 and you spent 25 minutes looking for a bug, this 25 minutes of computer idle time could not be recovered. Nor was your colleague who signed up for 0200–0230 likely to let you start another run at 0158.

If we analyze what is happening in the terms of the previous sections we
see that the manual procedures that must be performed—mounting tapes, setting up card decks, or changing places at the console—are disjoint from the actual computation and can be performed concurrently with the computer’s processing.

The second generation of computers used a supervisor program to batch jobs. A professional computer operator sat at the console. Programmers prepared card decks which were concatenated into “batches” that were fed into the computer once an hour or so. The increase in throughput (a measure of the efficiency of a computer; it is the number of jobs—suitably weighted—that can be run in a given time period) was enormous—the jobs were run one after another with no lost minutes. The programmers, however, lost the ability to dynamically track the progress of their programs since they no longer sat at the computer console. In the event of an error in one job, the computer simply commenced execution of the next job in the batch, leaving the programmer to puzzle out what happened from core dumps. With a turnaround time (the amount of time that elapses between a job being submitted for execution and the results being printed) of hours or days, the task of programming became more difficult even though certain aspects were improved by high-level languages and program libraries.

Despite this improvement in throughput, systems designers had noticed another source of inefficiency not apparent to the human eye. Suppose that a computer can execute one million instructions per second and that it is connected to a card reader which can read 300 cards per minute (= one card in 1/5 second). Then from the time the read instruction is issued until the time the card has been read, 200 000 instructions could have been executed. A program to read a deck of cards and print the average of the numbers punched in the cards will spend over 99% of its time doing nothing even though 5 cards per second seems very fast.

The first solution to this problem was spooling. The I/O speed of a magnetic tape is much greater than that of the card reader and the line printer that are the interface between the computer and the programmer. We can decompose the operation of the computer into three processes: a process to read cards to tape; a process to execute the programs on the tape and write the results onto a second tape; and a process to print the information from the second tape. Since these processes are disjoint (except for the exchange of the tapes after processing a batch), the throughput can be greatly increased by running each process on a separate computer. Since very simple computers can be used to transfer information to and from the magnetic tape, the increase in cost is not very great compared to the savings achieved by more efficient use of the main computer.

Later generations of computer systems have attacked these problems by switching the computer among several computations whose programs and data are held simultaneously in memory. This is known as multiprogramming. While I/O is in progress for program \( P_1 \), the computer will execute
several thousand instructions of program $P_2$ and then return to process the
data obtained for $P_1$. Similarly, while one programmer sitting at the terminal
of a time-sharing system† is thinking, the computer will switch itself to
execute the program requested by a second programmer. In fact, modern
computer systems are so powerful that they can switch themselves among
dozens or even hundreds of I/O devices and terminals. Even a minicompu-
ter can deal with a dozen terminals.

The importance of the concept of interleaved computations mentioned
in the previous section has its roots in these multiprogrammed systems.
Rather than attempt to deal with the global behavior of the switched com-
puter, we will consider the actual processor to be merely a means of interleav-
ing the computations of several processors. Even though multiprocessor
systems—systems with more than one computer working simultane-
ously—are becoming more common, the interleaved computation model is
still appropriate.

The sophisticated software systems that are responsible for multi-
programming are called operating systems. The term operating system is
often used to cover all manufacturer-provided software such as I/O pro-
grams and compilers and not just the software responsible for the multi-
programming.

While the original concern of operating system designers was to
improve throughput, it soon turned out that the throughput was affected by
numerous system “crashes” when the system stopped functioning as it was
supposed to and extensive recovery and restart measures delayed execution
of jobs. These defects in the operating systems were caused by our inadequa-
ate understanding of how to execute several programs simultaneously and
new design and programming techniques are needed to prevent them.

1.6 OPERATING SYSTEMS AND CONCURRENT PROGRAMMING

If you could sense the operation of a computer that is switching itself every
few milliseconds among dozens of tasks you would certainly agree that the
computer seems to be performing these tasks simultaneously even though
we know that the computer is interleaving the computations of the various
tasks. I now argue that it is more than a useful fiction to assume that the
computer is in fact performing its tasks concurrently. To see why this is so, let
us consider task switching in greater detail. Most computers use interrupts

† A time-sharing system is a computer system that allows many programmers to
work simultaneously at terminals. Each programmer may work under the
illusion that the computer is working for him alone (though the computer may
 seem to be working slowly if too many terminals are connected).
for this purpose. A typical scenario for task switch by interrupts is as follows. Program $P_1$ makes a read request and then has its execution suspended. The CPU may now execute program $P_2$. When the read requested by $P_1$ has been completed, the I/O device will interrupt the execution of $P_2$ to allow the operating system to record the completion of the read. Now the execution of either $P_1$ or $P_2$ may be resumed.

The interrupts occur asynchronously during the execution of programs by the CPU. By this is meant that there is no way of predicting or coordinating the occurrence of the interrupt with the execution of any arbitrary instruction by the CPU. For example, if the operator who is mounting a magnetic tape happens to sneeze, it may delay the "tape ready" signal by 8.254387 seconds. However, if he is "slow" with his handkerchief, the delay might be 8.254709 seconds. Insignificant as that difference may seem, it is sufficient for the CPU to execute dozens of instructions. Thus for all practical purposes it makes no sense to ask: "What is the program that the computer is executing?" The computer is executing any one of a vast number of execution sequences that may be obtained by arbitrarily interleaving the execution of the instructions of a number of computer programs and I/O device handlers.

This reasoning justifies the abstraction that an operating system consists of many processes executing concurrently. The use of the term process rather than program emphasizes the fact that we need not differentiate between ordinary programs and external devices such as terminals. They are all independent processes that may, however, need to communicate with each other.

The abstraction will try to ignore as many details of the actual application as possible. For example, we will study the producer–consumer problem which is an abstraction both of a program producing data for consumption by a printer and of a card reader producing data for consumption by a program. The synchronization and communication requirements are the same for both problems even though the details of programming an input routine are rather different from the details of an output routine. Even as new I/O devices are invented, the input and output routines can be designed within the framework of the general producer–consumer problem.

On the other hand, we assume that each process is a sequential process. It is always possible to refine the description of a system until it is given in terms of sequential processes.

The concurrent programming paradigm is applicable to a wide range of systems, not just to the large multiprogramming operating systems that gave rise to this viewpoint. Moreover, every computer (except perhaps a calculator or the simplest microcomputer) is executing programs that can be considered to be interleaved concurrent processes. Minicomputers are supplied with small multiprogramming systems. If not, they may embedded in
real-time systems where they are expected to concurrently absorb and process dozens of different asynchronous external signals and operator commands. Finally, networks of interconnected computers are becoming common. In this case true parallel processing is occurring. Another term used is distributed processing to emphasize that the connected computers may be physically separated. While the abstract concurrency that models switched systems is now well understood, the behavior of distributed systems is an area of current research.

1.7 AN OVERVIEW OF THE BOOK

Within the overall context of writing correct software this book treats the single, but extremely important, technical point of synchronization and communication in concurrent programming. The problems are very subtle; ignoring the details can give rise to spectacular bugs. In Chapter 2 we shall define the concurrent programming abstraction and the arguments that justify each point in the definition. The abstraction is sufficiently general that it can be applied without difficulty to real systems. On the other hand it is sufficiently simple to allow a precise specification of both good and bad behavior of these programs.

Formal logics exist which can formulate specifications and prove properties of concurrent programs in this abstraction though we will limit ourselves to informal or at most semi-formal discussions. The fact that the discussion is informal must not be construed as meaning that the discussion is imprecise. A mathematical argument is considered to be precise even if it is not formalized in logic and set theory.

The basic concurrent programming problem is that of mutual exclusion. Several processes compete for the use of a certain resource such as a tape drive but the nature of the resource requires that only one process at a time actually accessed the resource. In other words, the use of the resource by one process excludes other processes from using the resource. Chapter 3 presents a series of attempts to solve this problem culminating in the solution known as Dekker’s algorithm. The unsuccessful attempts will each point out a possible “bad” behavior of a concurrent program and will highlight the differences between concurrent and sequential programs.

Dekker’s algorithm is itself too complex to serve as a model for more complex programs. Instead, synchronization primitives are introduced. Just as a disk file can be copied onto tape by a single control language command

† Whereas a time-sharing system gives the user the ability to use all the resources of a computer, the term real-time system is usually restricted to systems that are required to respond to specific pre-defined requests from a user or an external sensor. Examples would be air-traffic control systems and hospital monitoring systems.
or a file can be read by writing `read` in a high level language, so we can define programming language constructs for synchronization by their semantic definition—what they are supposed to do—and not by their implementation. We shall indicate in general terms how these primitives can be implemented but the details vary so much from system to system that to fully describe them would defeat our purpose of studying an abstraction. Hopefully, it should be possible for a "casual" systems programmer to write concurrent programs without knowing how the primitives are implemented. A model implementation is described in the Appendix.

Chapter 4 commences the study of high level primitives with E. W. Dijkstra's semaphore. The semaphore has proved extraordinarily successful as the basic synchronization primitive in terms of which all others can be defined. The semaphore has become the standard of comparison. It is sufficiently powerful that interesting problems have elegant solutions by semaphores and it is sufficiently elementary that it can be successfully studied by formal methods. The chapter is based on the producer–consumer problem mentioned above; the mutual exclusion problem can be trivially solved by semaphores.

Most operating systems have been based on monolithic monitors. A central executive, supervisor or kernel program is given sole authority over synchronization. Monitors, a generalization of this concept formalized by Hoare, are the subject of Chapter 5. The monitor is a powerful conceptual notion that aids in the development of well structured, reliable programs. The problem studied in this chapter is the problem of the readers and the writers. This is a variant of the mutual exclusion problem in which there are two classes of processes: writers which need exclusive access to a resource and readers which need not exclude one another (though as a class they must exclude all writers).

The advent of distributed systems has posed new problems for concurrent programming. C. A. R. Hoare has proposed a method of synchronization by communication (also known as synchronization by rendezvous) appropriate for this type of system. The designers of the Ada programming language have chosen to incorporate in the language a variant of Hoare's system. Anticipating the future importance of the Ada language, Chapter 6 studies the Ada rendezvous.

A classic problem in concurrent programming is that of the Dining Philosophers. Though the problem is of greater entertainment value than practical value, it is sufficiently difficult to afford a vehicle for the comparison of synchronization primitives and a standing challenge to proposers of new systems. Chapter 7 reviews the various primitives studied by examining solutions to the problem of the Dining Philosophers.

Programming cannot be learned without practice and concurrent programming is no exception. If you are fortunate enough to have easy access to
a minicomputer or to a sophisticated simulation program, there may be no difficulty in practicing these new concepts. If not, the Appendix describes in full detail an extremely simple simulator of concurrency that can be used for class exercise. In any case, the Appendix can serve as an introduction to implementation of concurrency.

The book ends with an annotated bibliography suggesting further study of concurrent programming.

1.8 PROGRAM NOTATION

The examples in the text will be written in a restricted subset of Pascal-S, which is itself a highly restricted subset of Pascal. This subset must of course be augmented by constructs for concurrent programming. It is intended that the examples be legible to any programmer with experience in Pascal, Ada, C, Algol, or PL/I.

The implementation kit in the Appendix describes an interpreter for this language that will execute the examples and that can be used to program the exercises. The language in the kit contains more Pascal language features than are used in the text of the book and thus users of the kit are assumed to be able to program in sequential Pascal. These extra features are necessary in order to use the kit to solve the exercises, although the exercises themselves could be programmed in other languages that provide facilities for concurrent programming.

The examples in the chapter on monitors are standard and can be adapted to the many systems that provide the monitor facility such as Concurrent Pascal, Pascal-Plus, or CSP/k. The examples in the chapter on the Ada rendezvous are executable in Ada.

We now present a sketch of the language that should be sufficient to enable programmers unfamiliar with Pascal to understand the examples.

1. Comments are inserted between (• and •).

2. The first line in a program should be

   program name;

3. Symbolic names for constants may be declared by the word const followed by the constant itself:

   const twon=40;

4. All variables in each procedure in the main program must be declared by the word var followed by the names of the variables and a type:

   var i, j, temp: integer;
   found: boolean;
The available types are: \texttt{integer, boolean} (with constants \texttt{true} and \texttt{false}) and arrays:

\begin{verbatim}
var a:array[lowindex...highindex] of integer;
\end{verbatim}

5. Following the declaration of the variables, procedures and functions may be declared: \texttt{procedure} \texttt{name ( formal parameters )}; and \texttt{function} \texttt{name ( formal parameters ): returntype};. The formal parameter definition has the same form as that of a variable list:

\begin{verbatim}
procedure sort (low,high: integer);
function last(index: integer): boolean;
\end{verbatim}

6. The body of the main program or of procedures is a sequence of statements separated by semi-colons between \texttt{begin} and \texttt{end}. The main program body is terminated by a period and the procedure bodies by semi-colons. The usual rules on nested scopes apply.

7. The statements are:

\begin{verbatim}
assignment statement
if boolean-expression then statement
if boolean-expression then statement else statement
for index-variable := lowindex to highindex do statement
while boolean-expression do statement
repeat sequence-of-statements until boolean-expression
\end{verbatim}

The syntactic difference between \texttt{while} and \texttt{repeat} is that \texttt{while} takes a single statement and \texttt{repeat} takes a sequence of statements (separated by semi-colons). The semantic difference is that the \texttt{while} tests before the loop is done and \texttt{repeat} tests afterwards. Thus \texttt{repeat} executes its loop at least once.

8. A sequence of statements may be substituted for “statement” in the above forms by enclosing the sequence of statements in the bracket \texttt{begin \ldots end} to form a single “compound” statement:

\begin{verbatim}
if \texttt{a[j]} < \texttt{a[i]} then
begin
  \texttt{temp} := \texttt{a[j]};
  \texttt{a[j]} := \texttt{a[i]};
  \texttt{a[i]} := \texttt{temp}
end
\end{verbatim}

In detail this is read: if the boolean expression (\texttt{a[j]} < \texttt{a[i]}) has the value \texttt{true}, then execute the compound statement which is a sequence of three assignment statements. If the expression is \texttt{false}, then the (compound) statement is not executed and the execution continues with the next statement.
9. Assignment statements are written variable := expression. The variable may be a simple variable or an element of an array: \( a[i] \). The type (integer or boolean) of the expression must match that of the variable. Integer expressions are composed of integer variables and constants using the operators: +, −, *, div (integer divide with truncation) and mod. Boolean expressions may be formed from relations between integer expressions: =, <>, (not equal), <, >, <= (less than or equal) >= (greater than or equal). The boolean operators and, or and not may be used to form compound boolean expressions.

10. For those who know Pascal we list here the additional features that are defined in the language of the implementation kit some of which will be necessary if you plan to write any programs using the kit.
   (a) Type declarations. Since there are no scalar, subrange or record types, this is mostly useful for array types:
   ```pascal
   type sortarray = array[1..n] of integer
   var a: sortarray;
   ```
   (b) Character constants and variables of type char.
   (c) Multidimensional arrays (arrays of arrays).
   (d) A parameter may be passed by reference rather than value by prefixing the formal parameter by var.
   (e) Recursive functions and procedures.
   (f) I/O may be performed only on the standard textfiles input and output. To ensure that you do not forget this restriction, the declaration of external files in the program card has been removed. read, readln, write, writeln, eoln, eof (all without a file parameter) function as in Pascal. Only the default field widths may be used in a write, which will, however, accept a 'string' as a field to be printed:
   ```pascal
   writeln ('the answer is', n).
   ```

1.9 EXERCISES‡

1.1 Write a two-process concurrent program to find the mean of \( n \) numbers.

1.2 Write a three-process concurrent program to multiply \( 3 \times 3 \) matrices.

1.3 Each process of the matrix multiply program executes three multiplications and two additions for each of three rows or altogether 15 instructions. How many execution sequences of the concurrent program may be obtained by interleaving the executions of the three processes?

‡ Slightly harder exercises are marked throughout the book with an asterisk (*).
1.4 Perform a similar analysis for *sortprogram*. You will have to make some assumptions on the number of interchanges that will be done.

1.5 Test the concurrent *sortprogram* of Fig. 1.3.

1.6 Test the concurrent *sortprogram* of Fig. 1.4 which has the *merge* defined as a third process. Run the program several times with exactly the same data.

1.7 Run the program in Fig. 1.8 several times. Can you explain the results?

```plaintext
program increment;
const m = 20;
var n: integer;
procedure incr;
var i: integer;
begin
  for i := 1 to m do n := n + 1
end;
begin (* main program *)
  n := 0;
  cobegin
    incr, incr
  coend;
  writeln (' the sum is ', n)
end.

Fig. 1.8.
```
2 THE CONCURRENT PROGRAMMING ABSTRACTION

2.1 INTRODUCTION

Concurrent programming is not the study of operating systems or real-time systems, but of abstract programming problems posed under certain rules. Concurrent programming was motivated by the problems of constructing operating systems, and its examples are abstract versions of such problems. Most importantly, the rules of concurrent programming are satisfied in many systems and thus its techniques can be used in real systems. Components of a system which are not amenable to concurrent programming techniques should be singled out for extremely careful design and implementation.

Chapter 1 gave the definition of a concurrent program. It consists of several sequential processes whose execution sequences are interleaved. The sequential programs are not totally independent – if they were so there would be nothing to study. They must communicate with each other in order to synchronize or to exchange data.

The first means of communication that we shall study is the common memory. This is appropriate for the pseudo-parallel switched computers where all processes are running on the same processor and using the same physical memory. It is also used on some truly parallel systems such as the CDC Cyber computers where even though one CPU and ten PP's (peripheral processors) are simultaneously executing separate programs, synchronization is accomplished by having the PP's read and write the CPU's memory. In our abstraction, common memory will be represented simply by global variables accessible to all processes.

Common memory can also be used to hold access-restricted procedures. Access to these procedures is, in effect, allocated to a process. This is the way most third generation operating systems were implemented. The "system" programs can only be called by special instructions which ensure that only one process at a time is executing a system program.
With the introduction of distributed computing it is no longer valid to assume that a common central memory exists. Chapter 5 discusses concurrent programming by means of sending and receiving signals instead of reading and writing a common variable or executing a common procedure. Synchronization by message-passing has been used on several experimental systems for single-processor computers but this approach has not been widely accepted because of the possible inefficiency of message-passing compared with simpler systems. Of course, distributed systems have no choice.

2.2 MUTUAL EXCLUSION

Mutual exclusion is one of the two most important problems in concurrent programming because it is the abstraction of many synchronization problems. We say that activity \( A_1 \) of process \( P_1 \) and activity \( A_2 \) of process \( P_2 \) must exclude each other if the execution of \( A_1 \) may not overlap the execution of \( A_2 \). If \( P_1 \) and \( P_2 \) simultaneously attempt to execute their respective activities, \( A_1 \) and \( A_2 \), then we must ensure that only one of them succeeds. The losing process must block; that is, it must not proceed until the winning process completes the execution of its activity \( A \).

The most common example of the need for mutual exclusion in real systems is resource allocation. Obviously, two tapes cannot be mounted simultaneously on the same tape drive. Some provision must be made for deciding which process will be allocated a free drive and some provision must be made to block processes which request a drive when none is free. There is an obvious solution: run only one job at a time. But this defeats one of the main aims of concurrent programming – parallel execution of several processes.

Meaningful concurrency is possible only if the processes are loosely connected. The loose connection will manifest itself by the need for short and occasional communication. The abstract mutual exclusion problem will be expressed:

\[
\text{remainder} \\
\text{pre-protocol} \\
\text{critical section} \\
\text{post-protocol.}
\]

“remainder” will be assumed to represent some significant processing. Occasionally, i.e. after the completion of remainder, the process needs to enter a short critical section. It will execute certain sequences of instructions,
called protocols before and possibly after the critical section. These protocols will ensure that the critical section is in fact executed so as to exclude all other critical sections. Of course, just as the critical section should be short relative to the main program in order to benefit from concurrency, the protocols must also be relatively short. The protocols represent the overhead paid for concurrency. Hopefully, if the critical sections and the protocols are sufficiently short then the significant processing abstracted as remainder can be overlapped thus justifying the design of the multiprogramming system.

There is another, more important, reason for requiring loose connection among concurrent processes and that is to ensure reliability. We want to be assured that if there is a bug in one of the processes, then it will not propagate itself into a system "crash". It should also be possible to gracefully degrade the performance of a system if an isolated device should fail ("failsoft"). It would be absurd to have a system crash just because one tape drive became faulty.

The abstract requirement will be that, if a process abnormally terminates outside the critical section then no other process should be affected. (For this purpose the protocols are considered to be part of the critical section.) Since the critical section is where the communication is taking place, it is not reasonable to require the same of the critical sections. We might use the following metaphor. If a runner in a relay race fell after he has passed the baton then the race should not be affected. It is unreasonable to hope that the race is unaffected if the fall occurred at the critical moments during the baton exchange.

This restriction is not unreasonable even in practice. Critical sections such as disk I/O will often be executed by common system routines or by compiler-supplied routines which have been written by a competent systems programmer. The probability of a software error in such a routine should be much smaller than in a run-of-the-mill program.

2.3 Correctness

What does it mean for concurrent programs to be correct? An ordinary program is correct if it halts and prints the "right" answer. In general, you will know a "right" answer if you see one. This is also true of some concurrent programs such as sortprogram.

On the other hand, the single most distinguishing feature of an operating system or real-time system is that it must never halt. The only way to halt a typical operating system is to push the start button on the computer panel. An operating system prints nothing of its own (except some non-essential logging and accounting data). Thus when studying operating systems, we
must revamp our notions of what it means for a program to be correct. Since most concurrent programming is done within operating systems and real-time systems, this is the area to be studied in this book.

An obvious truism is that any program must do what its specifications say that it is supposed to do. This is no less true in the case of concurrent programs though the specifications are radically different from those of sequential programs. In our abstraction, we shall distinguish two types of correctness properties: safety properties and liveness properties.

Safety properties are those required by the static portions of the specifications. These are often the only requirements explicitly specified. Mutual exclusion is a safety property: the requirement that critical sections exclude one another is absolute and does not change during the execution of the program. The safety property of the producer–consumer problem is that the consumer must consume every piece of data produced by the producer and that it must do so in the order in which they were produced.

Safety properties are akin to what is known in the theory of sequential programs as partial correctness: if the program terminates, the answers must be "correct". Safety properties are usually relatively easy to show. They are explicitly required by the specifications and programs are designed to meet these specifications. You can always achieve more safety by giving up some concurrency and letting more segments of the process execute sequentially.

Violation of mutual exclusion is the cause of most operating system crashes. Dynamic memory allocation is frequently involved: a process may be convinced that it knows the location of a certain table in memory while in fact the table has been removed and its memory allocated to another process.

At a computer center known to the Author, an unscrupulous programmer managed to insert into the system a program that, on command, would give his programs the highest priority. However, he did not know that mutual exclusion protocols were required because the scheduling table was not fixed in memory. Thus the execution of his command would often write into some other table of the system causing a crash. Since the crash occurred many minutes later, the memory dumps gave no clue as to what had happened. After several weeks, the problem was solved by noting the strange command on the system log. If such an error had been made in a regular systems program it would have been even more difficult to catch.

Liveness, on the other hand, deals with dynamic properties. It is akin to sequential programming's total correctness: the program terminates and the answer is "correct". In concurrent systems, liveness means that if something is supposed to happen then eventually it will happen. If a process wishes to enter its critical section then eventually it will do so. If a producer produces data then eventually the consumer will consume it.
The most serious breach of liveness is the global form known as deadlock.† Deadlock means that the computer is no longer doing any (useful) work. A loop that searches for a free tape drive when none is ever going to be available is not useful work. If all processes are suspended or in such loops, then the computer is said to be deadlocked. This system hangs is catastrophic since all users in a multiprogrammed system are affected.

The following deadlock scenario actually occurred in an operating system. The system had multiple processors. Each job wrote its accounting data into a common area of memory which was written to a disk file when it filled. The write procedure ran on whatever processor was free. If all the processors tried to write accounting data at the same time, there was no free processor to write to disk. Since no program voluntarily relinquished its processor, the system deadlocked. A typical solution in this case is to use the computer console terminal to fool a process into thinking that the memory area is empty. Of course, some data will be lost but this is usually preferable to a deadlocked system and restarting all currently running programs.

A local breach of liveness is called lockout or (individual) starvation. In this case there is always some process which can progress but some identifiable process is being indefinitely delayed. Lockout is less serious than deadlock since the computer is still doing some (presumably) useful work. On the other hand, lockout is difficult to discover and correct because it can happen only in complex scenarios where some processes unwittingly “conspire” to deny a resource to a hapless process.

For reasons to be discussed in the next section, we limit our discussion to qualitative liveness which means that the word “eventually”, used in the definition of liveness, means exactly that: within an unspecified but finite length of time.

Between the complete disregard of time by the liveness concept and the introduction of explicit time, is the concept of fairness: a process wishing to progress must get a fair deal relative to all other processes. Fairness is more difficult to define precisely and we will mention it only occasionally. In addition, many systems will consciously be “unfair” by designing a priority scheme to favor some processes over others.

### 2.4 Timing

We make no assumptions concerning the absolute or relative speeds at which the processes are executed. This statement seems rather shocking at first. However, failure to follow this restriction in systems design can cause

† Deadlock is theoretically considered to be a safety property because it is something that should never happen. However, absence of deadlock can be shown by proving that there is always at least one live process.
serious bugs. The statement is shocking because of the naive preoccupation with efficiency that most programmers have. After all, we know that a disk is slower than a CPU and it is tempting to take advantage of that fact in designing not only the structure of the system but also the synchronization details.

One reason for ignoring timing is that our intuition is not able to cope with the scale involved. There are only about \( \frac{1}{4} \) million minutes in a year but there are a million microseconds in a second. It is folly to state that: process \( P_1 \) ought to be able to finish its critical section before process \( P_2 \) finishes its non-critical section, unless such a statement is backed up by a detailed calculation.

A second reason for ignoring timing is that time-dependent bugs are extremely difficult to identify and correct. Qualitative treatments as presented in this book, are insufficient; timing calculations must be included. Each such bug can mean weeks of work for a team of programmers. We shall pay any reasonable penalty in efficiency to obtain a reliable system. You have to save an enormous number of microseconds to make a half-hour system crash worthwhile.

Finally there is an important practical reason to design a software system that is independent of timing assumptions and that is the dynamic nature of a computer configuration. Even if able to carry out the calculations necessary to ensure reliability in a time-dependent system, one is at the mercy of any configuration change. Theoretically, the addition of a single terminal could invalidate the reliability of the system. This is not too far-fetched. A computer manufacturer once started to market a modernized component that ran at twice the speed of the original component. The first customers received a notice that in effect said: "Thanks for buying our double-speed component but please run it at the original speed for a few months while we comb the operating system for time dependencies"! A system may certainly require some time-dependent processing but these functions should be clearly identified and isolated to ensure the flexibility and reliability of the system.

The advantages that accrue to a time-independent (asynchronous) system can be demonstrated on the hardware level by the architecture of the DEC PDP-11 computers. Instead of synchronizing access to memory and I/O devices by a clock, all data in the basic PDP-11 is transferred asynchronously according to a protocol that is not too different conceptually from what we will be doing. The overhead of the protocol means that for any given electronic technology, the PDP-11 will be somewhat slower than a computer built to a synchronous design. On the other hand, the architecture has proved to be extremely flexible; for example, memory modules of arbitrary speeds can be freely mixed. If a new technology produces memory 1.267 faster than before, such a module can be added to a current system and
will respond to the protocol just that much faster. A synchronous system can
generally mix only modules whose speeds are multiples of each other.

In the abstraction, certain assumptions will be made to avoid meaning-
less pathologies. Since infinite delay is indistinguishable from a halt, we will
assume (globally) that, if there is at least one process ready to run, then some
(unspecified) process is allowed to run within a finite time. We also assume
(locally) that if a process is allowed to run in its critical section then it
will complete the execution of the critical section in a finite period of
time.

On the other hand, we allow ourselves to use the adversary approach in
checking for possible bugs. A concurrent program suffers from deadlock if it
is possible to devise a scenario for deadlock under the sole finiteness assump-
tions of the previous paragraph. If someone offers you a concurrent pro-
gram, you can tailor your counterscenario specifically to the given program;
you are an "adversary" allowed to plot against the program.

### 2.5 IMPLEMENTING PRIMITIVE INSTRUCTIONS

Our solutions to the mutual exclusion problem will always cheat by making
use of mutual exclusion provided on a lower level—the hardware level. Just
as the user of a high level language need not know how a compiler works as
long as he is provided with an accurate description of the syntax and
semantics of the language, so we will not concern ourselves with how the
hardware is implemented as long as we are supplied with an accurate
description of the syntax and semantics of the architecture. Presumably the
same thing happens at lower levels—the computer logic designer need not
know exactly how an integrated circuit is implemented; the integrated circuit
designer need only concern himself with the electronic properties of semi-
conductors and need not know all the details of the quantum physics that
explain these properties.

In common memory systems there is an arbiter which provides for
mutual exclusion in the access to an individual memory word. The word
"access" is a generic term for read and write or, as they are usually called,
Load and Store corresponding to the assembler instructions for these
actions. The arbiter ensures that in case of overlap among accesses, mutual
exclusion is obtained by executing the accesses one after the other. The
order of the accesses is not guaranteed to the programmer. On the other
hand, the consistency of the access is ensured as described in Chapter 1.

Note that the access to a single word is an action that may not be
apparent in a high level language. Suppose that $n$ is a global variable that is
initially zero and is used as a counter by several processes executing the
instruction: \( n := n + 1 \). The compiler compiles such a statement into the three assembler instructions:

- Load \( n \)
- Add 1
- Store \( n \)

Consider now the following scenario. The value of \( n \) is 6. \( P_1 \) executes Load \( n \) and then \( P_2 \) also executes Load \( n \). \( P_1 \) increments the value of \( n \) in its internal register to obtain 7. Similarly, \( P_2 \) obtains the value 7 in its internal register. Finally, the two processes execute the Store instruction in succession and the value 7 is stored twice. Hence the final value of \( n \) is 7. That is we have incremented the value 6 twice and have obtained 7.

Common memory arbiters are found both on multiprocessor systems and on single processor systems whose I/O equipment is connected for direct memory access (DMA). Normally an I/O device would transfer each data word to the CPU for the CPU to store in the memory. However, this imposes an unacceptable overhead on the CPU. Instead, the I/O device is given the address of a block of memory. It only interrupts the CPU when the transfer of the whole block is completed. There is an arbiter to ensure that only one device (or the CPU) has access to the memory at any one time.

In this case we say that DMA is being implemented by cycle stealing. The memory is assumed to be driven at its maximum access speed, say one access per microsecond. Each such access is also called a memory cycle. To implement DMA the CPU is normally allowed to compute and access memory. When a data word arrives from an I/O device the right to access memory is usurped by the CPU and the device is allowed to "steal" a memory cycle. There is no real overhead. The memory cycle is needed anyway to store the word and with cycle stealing the CPU need not concern itself with individual words.

The computer hardware will be trusted to function properly. We only concern ourselves with the correctness of the system software. This is not always true of course and in practice one must be alert to hardware malfunction. One of the most spectacular bugs known to the Author was caused by a hardware fault that resulted in mixing two memory addresses instead of interleaving them. The net result was a store of data in the mixed-up address, and the presence of foreign data in these memory addresses was never explained by software specialists. Fortunately this sort of thing rarely happens.

Another way of using a common memory system is to define a primitive procedure call that is guaranteed to exclude other calls of the same procedure. That is, if two processes try to call the same procedure, only one will succeed and the losing process will have to wait. As usual it is not specified in which order simultaneous requests are granted.
In multiprogramming systems, the interrupt facility is used. A critical procedure is written as an interrupt routine to be executed when a process causes an interrupt. A hardware flag ensures mutual exclusion by inhibiting the interrupt—placing the computer in an uninterruptable state. Upon completion of the interrupt routine, the flag is reset and another process may now cause an interrupt.

Another method of implementing mutual exclusion is polling. Each process is interrogated in turn to see if it requires some service that must be done under mutual exclusion.

We shall allow ourselves the luxury of defining primitive instructions and, beyond the sketch in this section, we shall not worry about the implementation. With some experience in computer architecture and data structures it should not be too difficult to implement any of these primitives. However, the details differ widely from computer to computer. A study of the implementation kit may help. In the bibliography we give references to several descriptions of concurrent programming implementations. In addition, the serious student should study the architecture of whatever computer and operating system he is using.

### 2.6 CONCURRENT PROGRAMMING IN PASCAL-S

Sequential Pascal (and the subset used in this book) must be augmented by concurrent programming constructs. The concurrent processes are written as Pascal procedures and their identity as concurrent processes is established by their appearance in the `cobegin . . . coend` statement

\[
\text{cobegin } P_1; P_2; \ldots; P_n \text{ coend.}
\]

A request for concurrent execution of several processes may appear only in the main program and may not be nested. The semantics of the `cobegin . . . coend` statement are specified as follows:

The `cobegin` statement is a signal to the system that the enclosed procedures are not to be executed but are to be marked for concurrent execution. When the `coend` statement is reached, the execution of the main program is suspended and the concurrent processes are executed. The interleaving of the executions of these processes is not predictable and may change from one run to another. When all concurrent processes have terminated, then the main program is resumed at the statement following the `coend`.

An additional notational device that we make use of is the statement `repeat . . . forever` which is exactly equivalent in its semantic content with `repeat . . . until false`. However, the latter is rather obscure and we prefer the more transparent notation.
The use of repeat . . . forever emphasizes that these examples are intended to be prototypes of cyclic programs in operating systems and real-time systems.

To execute any of the examples in the book on the implementation kit you will generally have to do the following. (See Fig. 1.5 and, for a larger example, Fig. 4.18).

1. Replace repeat . . . forever by a for-loop that will execute each process a fixed number of times or otherwise arrange for termination.
2. Insert write statements in the main program or in the concurrent processes to trace the execution of the program.
3. Often, certain procedures have been left unspecified to emphasize the generality of the algorithms. For example, in the producer–consumer problem, we have invoked procedures named produce and consume. These procedures must be specified. One possibility is to produce by incrementing an integer and consume by printing it.
4. Warning The interpreter in the kit is very inefficient, so do not get carried away with the size of the programs that you intend to execute.

2.7 SUMMARY

This list summarizes the concurrent programming abstraction.

1. A concurrent program will consist of two or more sequential programs whose execution sequences are interleaved.
2. The processes must be loosely connected. In particular, the failure of any process outside its critical section and protocols must not affect the other processes.
3. A concurrent program is correct if it does not suffer from violation of safety properties such as mutual exclusion and of liveness properties such as deadlock and lockout.
4. A concurrent program is incorrect if there exists an interleaved execution sequence which violates a correctness requirement. Hence it is sufficient to construct a scenario to show incorrectness; to show correctness requires a mathematical argument that the program is correct for all execution sequences.
5. No timing assumptions are made except that no process halts in its critical section and that, if there are ready processes, one is eventually scheduled for execution. We may impose other fairness requirements.
6. We shall extend our basic programming language with synchronization primitive instructions. As long as the syntax and semantics of these instructions are clearly defined we do not concern ourselves with their implementation.

2.8 EXERCISES

2.1 Standing Exercise Write formal specifications of the programs in this book. For example:
Specification for sortprogram.
Input: A sequence of 40 integers: \( A = \{a_1, \ldots, a_{40}\} \).
Output: A sequence of 40 integers: \( b = \{b_1, \ldots, b_{40}\} \).
Safety property: When the program terminates then (i) \( b \) is a permutation of \( a \), and (ii) \( b \) is ordered, i.e. for \( 1 \leq i \leq 40 \), \( b_i \leq b_{i+1} \).
Liveness property: The program terminates.

2.2 Standing Exercise Test the example programs in the text.
3 THE MUTUAL EXCLUSION PROBLEM

3.1 INTRODUCTION

A solution to the mutual exclusion problem for two processes $P_1$ and $P_2$ will now be developed without introducing any primitive instructions (other than the common memory arbiter). The purpose of this chapter is not so much to present Dekker's elegant solution to this very difficult problem as to present Dijkstra's step-by-step development of Dekker's solution. During the development we will encounter most of the possible bugs that a concurrent program can have and thus illustrate the theoretical discussion of the previous chapter. The serious reader will want to try to analyze each attempted solution before reading further.

The mutual exclusion problem for two processes is as follows: Two processes $P_1$ and $P_2$ are each executing in an infinite loop a program which consists of two sections, critical sections crit1 and crit2 and the

Fig. 3.1.

29
remainder of the program, non-critical sections \textit{rem1} and \textit{rem2}. The execution of \textit{crit1} and \textit{crit2} must not overlap.

\section{First Attempt}

Let us imagine a "protocol igloo" containing a blackboard (Fig. 3.1). The igloo itself and the entrance tunnel are so small that only one person can be in the igloo at any given time. On the blackboard is written the number of the process whose "turn" it is to enter the critical section. The small size of the igloo is our metaphor for the memory arbiter.

A process wishing to enter its critical section crawls into the igloo when it is empty and checks the blackboard. If its number is written, it leaves the igloo and happily proceeds to its critical section. If the number of the other process is written then it sadly leaves the igloo to wait for the other process to finish.

Ideally, the unfortunate process would be able to take a nap until its turn arrives but we have no way of expressing this in an ordinary programming language. Instead, the process can run laps around the igloo to warm up (this is doing "nothing"). Periodically it can re-enter the igloo to check the blackboard. This is known as \textit{busy waiting} because the energy expended by the waiting process is just purposeless work. When a process has completed its critical section, it writes the number of the other process on the board. Since only one process is in the igloo at any one time, the board shows either a one or a two (assuming that neither process malfunctions within the igloo).

\begin{verbatim}
program firstattempt;
var    turn: integer;
procedure p1;
begin
    repeat
        while turn=2 do (* nothing *);
        crit1;
        turn := 2;
        rem1
    forever
end;
procedure p2;
begin
    repeat
        while turn=1 do (* nothing *);
        crit2;
        turn := 1;
        rem2
    forever
end;
\end{verbatim}
begin (* main program *)
  turn := 1;
  cobegin
    $p_1$; $p_2$
  coend
end

Fig. 3.2.

This solution (Fig. 3.2) satisfies the mutual exclusion requirement. A process $P_i$ enters its critical section only if $\text{turn} = i$. Since, by the common memory assumption, $\text{turn}$ will be consistent (will have either a value of 1 or 2), only one process at a time enters its critical section. Since the value of $\text{turn}$ is not changed until the termination of the critical section, a second process will not be able to infiltrate before termination of the first critical section.

Deadlock is also impossible. Since $\text{turn}$ has either the value 1 or the value 2, exactly one process will always be able to progress or, to put it another way, it is impossible for both processes to be simultaneously stuck at the while loops.

Similarly, if every statement of each program takes a finite amount of time then the process whose turn it is to enter the critical section will always do so and will eventually allow the other process to enter also. Thus there is no lockout since neither process can prevent the other from entering its critical section.

Even though this solution fulfils our requirements for the correctness of concurrent programs, it does not fulfil one of the design requirements of the abstraction. The processes are not loosely connected. The right to enter the critical section is being explicitly passed from one process to the other.

This has two drawbacks. Firstly, if process $P_1$ needs to enter its critical section 100 times per day while $P_2$ needs to enter only once per day then $P_1$ is going to be coerced into working at $P_2$’s pace of once per day. When $P_1$ has finished its critical section, then, it chalks up a 2 and until $P_2$ decides to re-enter the critical section, $P_1$ will be forced to wait.

The second drawback is as serious. Suppose $P_1$ is waiting for $P_2$ to execute a critical section and then change the number written on the board from 2 to 1. If by chance $P_2$ is devoured by a polar bear on its way to the igloo then not only is $P_2$ terminated but $P_1$ is hopelessly deadlocked. This is true even if $P_2$ is in $\text{rem2}$ outside the critical section when it terminates, thus conforming with our assumption that a process may terminate only outside its critical section.

This explicit passing of control is a programming technique known as coroutines. By executing an instruction such as $\text{resume} (p_2)$, $P_1$ is able to request that its execution be suspended in favor of $P_2$. $P_2$ then executes until it in turn returns the control of $P_1$ by a $\text{resume} (p_1)$ statement. Coroutines
are a useful programming technique but a system of coroutines must be designed as a single integrated process and are not a substitute for concurrent programs.

### 3.3 SECOND ATTEMPT

![Diagram of an igloo with two processes, labeled c1 and c2, and a figure labeled 3.3.

Fig. 3.3.

We try to remedy the previous solution by giving each process its own key to the critical section so if one is devoured by a polar bear then the other can still enter its critical section. There is now (Fig. 3.3) an igloo (global variable) identified with each process. It is worth noting that, while in the solution in Fig. 3.2 the variable *turn* is both read (Load) and written (Store) by both processes, the present solution may be easier to implement because each process reads but does not write the variable identified with the other process.

If *P₁* (say) wishes to enter its critical section, it crawls into *P₂*’s igloo periodically until it notes that *c₂* is equal to 1 signifying that *P₂* is currently not in its critical section. Having ascertained that fact, *P₁* may enter its critical section after duly registering its entrance by chalking a 0 on its blackboard—*c₁*. When *P₁* has finished, it changes the mark on *c₁* to 1 to notify *P₂* that the critical section is free.

```plaintext
program secondattempt;
var  c₁, c₂: integer;
procedure p₁;
  begin
    repeat
```
while \( c_2 = 0 \) do:
\[\begin{array}{l}
    c_1 := 0;
    \text{crit1};
    c_1 := 1;
    \text{rem1}
\end{array}\]
forever
end;

procedure \( p_2 \);
begin
repeat
    \[\begin{array}{l}
        \text{while } c_1 = 0 \text{ do:}
        \\
        c_2 := 0;
        \text{crit2};
        c_2 := 1;
        \text{rem2}
    \end{array}\]
forever
end;

begin (* main program *)
\[\begin{array}{l}
    c_1 := 1;
    c_2 := 1;
\end{array}\]
cobegin
\[\begin{array}{l}
    p_1; p_2
\end{array}\]
coend
end.

Fig. 3.4.

This program (Fig. 3.4) does not even satisfy the safety requirement of mutual exclusion. The following scenario gives a counter-example where the first column describes the interleaving and the next columns record the values of the variables.

\[
\begin{array}{cccc}
    & c_1 & c_2 \\
\text{Initially} & 1 & 1 \\
\text{\( P_1 \) checks \( c_2 \)} & 1 & 1 \\
\text{\( P_2 \) checks \( c_1 \)} & 1 & 1 \\
\text{\( P_1 \) sets \( c1 \)} & 0 & 1 \\
\text{\( P_2 \) sets \( c2 \)} & 0 & 0 \\
\text{\( P_1 \) enters crit1} & 0 & 0 \\
\text{\( P_2 \) enters crit2} & 0 & 0 \\
\end{array}
\]

Since \( P_1 \) and \( P_2 \) are simultaneously in their critical sections, the program is incorrect.
3.4 THIRD ATTEMPT

program thirdattempt;
var c_1, c_2: integer;
procedure p_1;
begin
repeat
  c_1 := 0;
  while c_2 = 0 do;
  crit1;
  c_1 := 1;
  rem1
forever
end;
procedure p_2;
begin
repeat
  c_2 := 0;
  while c_1 = 0 do;
  crit2;
  c_2 := 1;
  rem2
forever
end;
begin (* main program *)
  c_1 := 1;
  c_2 := 1;
  cobegin
  p_1; p_2
  coend
end.

Fig. 3.5.

Analyzing the failure of the second attempt, we note that, once \( P_1 \) has ascertained that \( P_2 \) is not in its critical section, \( P_1 \) is going to charge right into its critical section. Thus, the instant that \( P_1 \) has passed the while statement, \( P_1 \) is in effect in its critical section. This contradicts our intention that \( c_1 = 0 \) should indicate that \( P_1 \) is in its critical section because there may be an arbitrarily long wait between the while statement and the assignment statement.

The third attempt (Fig. 3.5) corrects this by advancing the assignment statement so that \( c_1 = 0 \) will indicate that \( P_1 \) is in its critical section even before it checks \( c_2 \). Hence \( P_1 \) is in its critical section the instant that the while has been successfully passed.
Unfortunately this program easily leads to system deadlock as seen by the following scenario:

<table>
<thead>
<tr>
<th></th>
<th>$c_1$</th>
<th>$c_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Initially</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>$P_1$ sets $c_1$</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>$P_2$ sets $c_2$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$P_1$ checks $c_2$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$P_2$ checks $c_1$</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

\[\ldots\]

The continual checking of the variables can be continued indefinitely and cannot be considered progress. Thus the program is hopelessly deadlocked.

Even though this program is unacceptable because of the deadlock, it is instructive to prove that it satisfies the mutual exclusion property. By symmetry it is sufficient to show that: ($P_1$ in crit1) implies ($P_2$ is not in crit2).

1. (When $P_1$ entered crit1) then ($c_2$ was not 0).
   This follows from the structure of the program, namely the test on $c_2$ by $P_1$.
2. ($c_2$ is not 0) implies ($P_2$ is not in crit2).
   $crit2$ is bracketed between assignments to $c_2$ which ensure that this statement is always true.
3. (When $P_1$ entered crit1) then ($P_2$ was not in crit2).
   This is a logical consequence of (1) and (2).
4. ($P_1$ in crit1) implies ($c_1$ is 0).
   crit1 is bracketed between assignments to $c_1$.
5. ($c_1$ is 0) implies ($P_2$ does not enter crit2).
   The test will not allow $P_2$ through.
6. ($P_1$ in crit1) implies ($P_2$ does not enter crit2).
   A logical consequence of (4) and (5).
7. As long as ($P_1$ is in crit1), ($P_2$ will never enter crit2).
   This follows from (6). Since (6) refers to an arbitrary instant of time, then as long as its antecedent ($P_1$ in crit1) remains true, so will its consequent ($P_2$ does not enter crit2).
8. ($P_1$ in crit1) implies ($P_2$ is not in crit2).
   From (3) and (7).

Note that the proof has the simple structure of a deduction in the propositional calculus except for the need to express and deduce time-related properties such as “when”, “as long as” etc. There is a formal logic called temporal logic that can express these properties and can be used to formally prove properties of concurrent programs. For example, the reasoning in this proof can be formalized as an induction on the time that has passed since $P_1$ entered crit1. We are trying to prove that mutual exclusion is never violated: (3) ensures the basis of the induction; (6) is an induction step: assuming that $P_1$ is now in crit1, we can deduce that $P_2$ will not now enter
crit2 so that upon the conclusion of the current instruction, mutual exclusion will still not be violated.

3.5 FOURTH ATTEMPT

program fourthattempt;
var c1, c2: integer;
procedure p1;
begin
repeat
  c1 := 0;
  while c2 = 0 do
    begin
      c1 := 1;
      (* do nothing for a few moments *)
      c1 := 0
    end;
  crit1;
  c1 := 1;
  rem1
forever
end;
procedure p2;
begin
repeat
  c2 := 0;
  while c1 = 0 do
    begin
      c2 := 1;
      (* do nothing for a few moments *)
      c2 := 0
    end;
  crit2;
  c2 := 1;
  rem2
forever
end;
begin (* main program *)
  c1 := 1;
  c2 := 1;
cobegin
  P1; P2
coend
end.

Fig. 3.6.
In the previous solution, when $P_1$ chalks up 0 on $c_1$ to indicate its intention to enter its critical section, it also turns out that it is insisting on its right to enter the critical section. It is true that setting $c_1$ before checking $c_2$ prevents the violation of mutual exclusion but if $P_2$ is not ready to yield then $P_1$ should yield.

In the next attempt (Fig. 3.6) we correct this stubborn behavior by having a process relinquish temporarily its intention to enter its critical section to give the other process a chance to do so. $P_1$ enters its igloo and chalks up a 0. If upon checking $P_2$'s igloo, $P_1$ finds a 0 there too, it chivalrously returns to its igloo to erase the 0. After a few laps around the igloo it restores the signal $c_1 = 0$ and tries again. The comment is there simply to remind you that since arbitrary interleaving is permissible, the sequence of two assignments to the same variable is not meaningless.

First note that the previous proof of mutual exclusion holds here. From the above discussion, it should now be clear that there is such a thing as too much chivalry. If both processes continue yielding then neither will enter the critical section. The scenario is as follows:

<table>
<thead>
<tr>
<th></th>
<th>$c_1$</th>
<th>$c_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Initially</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>$P_1$ sets $c_1$</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>$P_2$ sets $c_2$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$P_1$ checks $c_2$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$P_2$ checks $c_1$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$P_1$ sets $c_1$</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>$P_2$ sets $c_2$</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>$P_1$ sets $c_1$</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>$P_2$ sets $c_2$</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

It is clear that this could be indefinitely extended and that liveness does not hold because neither process will ever enter its critical section. However, it is extremely unlikely ever to occur. Nevertheless we are forced to reject this solution. The main objection here is not so much that neither process will ever enter the critical section (it is unlikely that perfect synchronization continues indefinitely) but that we have no way of giving an *a priori* bound on the number of iterations that the loops will execute before they are passed. Thus we have no way of guaranteeing the performance of such a system.

Should this bug be classified as deadlock or lockout? On the one hand, both processes are looping on a protocol which is certainly not useful computation and the situation is similar to the previous attempt. However, we prefer to call this lockout to emphasize the following distinction. In the previous attempt the situation is hopeless. From the instant that the program is deadlocked, all future executions sequences remain deadlocked. In this
case however, the slightest aberration of the scenario will free one of the processes and in practice this will eventually happen. The key notion here is the conspiracy between the processes and not the hopelessness of the situation. It is only because we wish to be able to guarantee a worst-case behavior that we reject the current attempt.

3.6 Dekker's Algorithm

```plaintext
program Dekker;
var
  turn: integer;
  c1, c2: integer;

procedure p1;
begin
  repeat
    c1 := 0;
    while c2 = 0 do
      if turn = 2 then
        begin
          c1 := 1;
          while turn=2 do;
          c1 := 0
        end;
        crit1;
        turn := 2;
        c1 := 1;
        rem1
      forever
    end;

procedure p2;
begin
  repeat
    c2 := 0;
    while c1 = 0 do
      if turn=1 then
        begin
          c2 := 1;
          while turn=1 do;
          c2 := 0
        end;
        crit2;
        turn := 1;
        c2 := 1;
        rem2
      forever
  end;
```
begin (* main program *)
c_1 := 1;
c_2 := 1;
turn := 1;
cobegin
  p_1; p_2
coend
end.

Fig. 3.7.

Dekker's solution is an ingenious combination of the first and fourth attempted solutions. Recall that in the first solution we explicitly passed the right to enter the critical section between the processes. Unfortunately, the key to the critical section could be irretrievably lost if one of the processes is terminated. In the fourth solution we found that keeping separate keys leads to the possibility of infinite deferment of one process to the other.

Dekker's algorithm (Fig. 3.7) is based on the previous solution but solves the problem of lockout by explicitly passing the right to insist on entering the critical section. Each process has a separate igloo so it can go on processing even if one process is terminated by a polar bear. Note that we are here using the assumption that no process is terminated in its critical section (including the protocol).

There is now an "umpire" igloo with a blackboard labelled "turn", (Fig. 3.8). If P_1 chalks up a 0 on c_1 and then finds that P_2 has also chalked up a 0, it goes to consult the umpire. If the umpire has a 1 written upon it, then P_1 knows that it is its turn to insist and so P_1 periodically checks P_2's igloo. P_2 of course notes that it is its turn to defer and chivalrously chalks up a 1 on c_2 which will eventually be noted by P_1. P_2 meanwhile waits for P_1 to terminate.
its critical section. Upon termination, \( P_1 \) not only frees the critical section by setting \( c_1 \) to 1 but also resets \( \text{turn} \) to 2 both to free \( P_2 \) from the inner loop and to transfer the right to insist to \( P_2 \).

Mutual exclusion is proved exactly as in Section 3.4 since the value of \( \text{turn} \) has no effect on the decision to enter the critical section.

Proving liveness is somewhat of a challenge. Symmetrically it is sufficient to prove that, if \( P_1 \) executes \( c_1 := 0 \) indicating its intention to enter the critical section, then eventually it does so. This is done in two parts. First we prove that if \( P_1 \) attempts to enter its critical section but cannot do so, eventually the variable \( \text{turn} \) is permanently held at the value 1. But if \( \text{turn} \) is held permanently at 1 then \( P_1 \) can always enter its critical section.

### 3.7 A Proof of Dekker's Algorithm

Let us now prove the liveness of Dekker's Algorithm. The algorithm is shown in flowchart form in Fig. 3.9. The formal statement that we want to prove is that if the program counter of process \( P_1 \) is at point \( \alpha_2 \) (i.e. \( P_1 \) has left \( \text{rem1} \) and thus expresses a wish to enter the critical section), eventually the program counter of \( P_1 \) will be at \( \alpha_5 \) (i.e. \( P_1 \) may enter the critical section). Of course an exactly symmetrical proof will prove the liveness of \( P_2 \).

Our notation will be more concise: \( \alpha_i \) will be an abbreviation for the statement that the program counter of \( P_1 \) is at \( \alpha_i \). Similarly for \( P_2 \) and \( \beta_i \).

Remember the assumption that a process is never terminated in its critical section (including the protocols). Thus if \( P_1 \) is at \( \alpha_6 \), it will eventually reach \( \alpha_8 \). If \( P_1 \) is at \( \alpha_3 \), it will eventually reach \( \alpha_4 \) or \( \alpha_5 \) though without further information we cannot specify which of the two statements will be reached. To simplify the proof, this assumption is extended to \( \text{remi} \) (\( \alpha_i \) and \( \beta_i \)). In the exercises we indicate the modifications needed if we allow \( P_1 \) to terminate in \( \text{remi} \).

Note that if \( P_1 \) is at \( \alpha_3 \) and \( c_2 = 1 \), we cannot conclude that eventually \( P_1 \) is at \( \alpha_5 \). The assumption only guarantees that \( P_1 \) eventually tests the value of \( c_2 \); by then the value of \( c_2 \) could have been changed. To conclude that \( \alpha_5 \) implies eventually \( \alpha_8 \), we would have to show that \( \alpha_3 \) and that the value of \( c_2 \) is held at 1 indefinitely. Thus, when by assumption the test is eventually done, the value of \( c_2 \) will in fact be 1.

Since the only assignments to \( c_i \) are in \( P_n \), we can deduce the values of \( c_i \) from the \( \alpha \)'s and the \( \beta \)'s, respectively. We express these facts as invariants, i.e. statements that are always true.

11. \( c_1 = 0 \) if and only if \( \alpha_3 \) or \( \alpha_4 \) or \( \alpha_5 \) or \( \alpha_6 \) or \( \alpha_7 \).
12. \( c_2 = 0 \) if and only if \( \beta_3 \) or \( \beta_4 \) or \( \beta_5 \) or \( \beta_6 \) or \( \beta_7 \).
Fig. 3.9 Dekker's Algorithm. Initial values: $c_1 = 2, c_2 = \text{turn} = 1$.
Theorem (α₂ and never α₃) is false, that is α₂ implies eventually α₃.

Proof

1. (α₂ and never α₃) and (turn held at 2) imply eventually (c₁ held at 1).
   Since (never α₃), P₁ eventually passes α₅ and thence to α₄. Since (turn held at 2), P₁ reaches α₆ and α₈ and is then blocked in the loop at α₈. By I₁, as long as P₁ is at α₈, c₁ must equal 1.

2. (c₁ held at 1) and (turn held at 2) imply eventually (turn = 1).
   The truth of the two clauses concerning c₁ and turn together with the assumption that processes are not terminated implies that P₂ must eventually reach β₁ and assign the value 1 to turn.
   But (turn held at 2) and eventually (turn = 1) means that there will be a point of time when turn is simultaneously 1 and 2. This contradicts the consistency of the values in the common memory.
   From (α₂ and never α₃) and (turn held at 2) we have deduced a contradiction. Thus it must be that (α₂ and never α₃) implies eventually (turn is not 2). Since turn = 2 or turn = 1 we have proved.

3. (α₂ and never α₃) implies eventually (turn = 1).

4. (α₂ and never α₃) implies (never α₃) and (never α₇) and (never α₁).
   The only way to reach α₁ or α₇ from α₂ is to pass through α₅. But we assume that we never reach α₅.

5. (α₂ and never α₃) implies eventually (turn held at 1).
   Once the value of turn is 1 (as ensured by (3)) the only way that the value can change back to 2 is to execute α₇. By 4 this will never happen.

6. (α₂ and never α₃) implies eventually (P₁ loops forever at α₃-α₄).
   By (4) and (5), eventually [(turn held at 1) and (P₁ is never at α₅)].
   Hence since P₁ must reach α₃-α₄ from α₂, α₆ or α₈ it will then loop forever at α₃-α₄.

7. (α₂ and never α₃) implies eventually (c₁ held at 0).
   By (6), eventually we loop at α₃-α₄ which implies by I₁ that c₁ will be held at 0.

8. (c₁ held at 0) and (turn held at 1) imply eventually (c₂ held at 1).
   Similar to (1): P₂ must eventually loop at β₈. Then by I₂, c₂ is held at 1.

9. (α₂ and never α₃) implies eventually (c₂ held at 1).
   From (5), (7) and (8).
   But (8) contradicts (6): if c₂ is held at 1 then P₁ cannot be looping
at $\alpha_3 - \alpha_4$. From ($\alpha_2$ and never $\alpha_3$) we have deduced a contradiction. Thus ($\alpha_2$ and never $\alpha_3$) is false.

### 3.8 CONCLUSION

Mutual exclusion of two processes is about the simplest problem in concurrent programming. The difficulty of obtaining a correct solution to such a simple problem suggests that programming features more powerful than the common memory arbiter will be needed. In the exercises you can explore some other solutions of the type given here.

In particular, the solutions of the mutual exclusion problem for $n$ processes are so difficult that they are of more or less academic interest only, especially when compared with the trivial solution to the problem given, say, by semaphores.

There is another defect in the common memory arbiter and that is the busy wait that is used to achieve synchronization. The solutions all contain a statement: while condition do (* nothing *). Unless you have a dedicated computer doing the looping this is a waste of CPU computing power. Even if there is no CPU waste (as would be the case if the processes were I/O controllers) there is the severe overhead associated with cycle stealing. Thus the frequent accesses to turn in Dekker’s solution can prevent useful computation from being done by other processes.

The primitives discussed in the next chapters uniformly suspend the execution of the blocked processes. This is usually implemented by keeping a queue of processes, i.e. a queue of small blocks of memory containing essential information on the blocked processes. Thus the overhead is only a small amount of memory and the small amount of computation needed to manage the queue.

A final objection to Dekker’s algorithm is that it uses a common variable which is written into by both processes. In the exercises we discuss Lamport’s algorithms which have the advantage that each variable need only be written by one process. Thus his algorithms are suitable for implementation on distributed systems where the values of the variables can be transmitted and received but where each variable is written into only on the computer in which it physically resides.

### 3.9 EXERCISES

**3.1** (Dijkstra) Fig. 3.10 is a solution to the mutual exclusion problem for $n$ processes that is a generalization of Dekker’s solution.

(a) *Show that mutual exclusion holds.
(b) Show that deadlock does not occur.
(c) Show that lockout is possible.
program Dijkstra;
const  n = . . . ; (* number of processes *)
var    b, c: array [0 . . n] of boolean;
       turn: integer;
procedure process(i : integer);
var    j: integer;
       ok: boolean;
begin
  repeat
    b[i] := false;
  repeat
    while turn <> i do
      begin
        c[i] := true;
        if b[turn] then turn := i
      end;
    c[i] := false;
    ok := true;
    for j := 1 to n do
      if j <> i then
        ok := ok and c[j]
    until ok;
    crit;
    c[i] := true; b[i] := true;
    turn := 0;
  rem
  forever
end;
begin (* main program *)
  for turn := 0 to n do
    begin
      b[turn] := true;
      c[turn] := true
    end;
  turn := 0;
  cobegin
    process(1);
    process(2);
    . . .
    process(n)
  coend
end.

Fig. 3.10.

3.2 (Lamport) Fig. 3.11 is (what the Author calls) the Dutch Beer version of the Bakery Algorithm, restricted to two processes.

(a) Show safety and liveness. (Hint The variables are supposed to represent "ticket" numbers". The process with the lower ticket number enters its critical section. In case of a tie, it is arbitrarily resolved in favor of P1.)

(b) Show that the commands $n_i := 1$ are necessary.
(c) *Extend the algorithm to \( n \) processes. (Hint: Each process will choose a ticket number greater than the maximum of all outstanding ticket numbers. It will then wait until all processes with lower numbered tickets have completed their critical sections.)

```
program dutchbeer;
var n1, n2: integer;
procedure p1;
begin
  repeat
    n1 := 1;
    n1 := n2 + 1;
    while (n2 <=> 0) and (n2 < n1) do;
    crit1;
    n1 := 0;
    rem1
  forever
end;
procedure p2;
begin
  repeat
    n2 := 1;
    n2 := n1 + 1;
    while (n1 <=> 0) and (n1 <= n2) do;
    crit2;
    n2 := 0;
    rem2
  forever
end;
begin (* main program *)
  n1 := 0;
  n2 := 0;
  cobegin
    P1; P2
  coend
end.
```

Fig. 3.11.

3.3 Fig. 3.12 is Lamport’s Bakery Algorithm restricted to two processes.

(a) Show the safety and liveness of this solution.
(b) Generalize to \( n \) processes.
(c) Show that for \( n > 2 \) the values of the variables \( n_i \) are not bounded.
(d) *Suppose we allow a read (i.e. Load) of a variable \( n_i \) to return any value if it takes place simultaneously with a write (Store) of \( n_i \) by the \( i \)th process. Show that the correctness of the algorithm is not affected. Note, however, that we require the write to execute correctly. Similarly, all reads which do not overlap writes to the same variable must return the correct values.
(e) Show that the correctness of the Dutch Beer version of the algorithm is not preserved under the malfunction described in (d).
program bakery;
var c_1, c_2, n_1, n_2: integer;
procedure p_1;
begin
repeat
c_1 := 1;
n_1 := n_2 + 1;
c_1 := 0;
while c_2 <> 0 do;
while (n_2 <> 0) and (n_2 < n_1) do;
crit1;
n_1 := 0;
rem1
forever
end;
procedure p_2;
begin
repeat
c_2 := 1;
n_2 := n_1 + 1;
c_2 := 0;
while c_1 <> 0 do;
while (n_1 <> 0) and (n_1 <= n_2) do;
crit2;
n_2 := 0;
rem2
forever
end;
begin (* main program *)
c_1 := 0;
c_2 := 0;
n_1 := 0;
n_2 := 0;
cobegin
p_1; p_2
coend
end.

Fig. 3.12.

3.4 Fig. 3.13 is a solution to the mutual exclusion problem for two processes. Discuss the correctness of the solution: if it is correct, then prove it. If not, write scenarios that show that the solution is incorrect.

Several synchronization primitives that have been used are based on hardware instructions that enable several assignment statements to be executed as one (indivisible) primitive instruction. The solutions to the mutual exclusion problem using these primitives are very simple, but they remain busy wait algorithms in contrast to algorithms using the primitives to be studied in the next chapter.
program attempt;
var c1, c2: integer;
procedure p1;
begin
repeat
rem1;
repeat
  c1 := 1 - c2
until c2 <> 0;
crit1;
c1 := 1
forever
end;
procedure p2;
begin
repeat
rem2;
repeat
  c2 := 1 - c1
until c1 <> 0;
crit2;
c2 := 1
forever
end;
begin (* main program *)
c1 := 1;
c2 := 1;
cobegin
  p1; p2
coend
end.
end.

Fig. 3.13.

3.5 The IBM 360/370 computers have an instruction called TST (Test and Set). There is a system global variable called c (Condition Code). Executing TST(l) for local variable l is equivalent to the following two assignments:

\[ l := c; \]
\[ c := 1. \]

(a) Discuss the correctness (safety, deadlock, lockout) of the solution of the mutual exclusion problem shown in Fig. 3.14.

(b) Generalize to n processes.

(c) What would happen if the primitive TST instruction were replaced by the two assignments?

(d) *Modify the implementation kit to include the TST instruction.
program testandset;
var c: integer;
procedure p1;
var l: integer;
begin
  repeat
    rem1;
    repeat
      TST(l)
    until l = 0;
    crit1;
    c := 0
  forever
end;
procedure p2;
var l: integer;
begin
  repeat
    rem2;
    repeat
      TST(l)
    until l = 0;
    crit2;
    c := 0
  forever
end;
begin (* main program *)
c := 0;
cobegin
  p1; p2
coend
end.

Fig. 3.14.

3.6 The EX instruction exchanges the contents of two memory locations. EX(a,b) is equivalent to an indivisible execution of the following assignment statements:

\[
temp := a; \\
a := b; \\
b := temp.
\]

(a) Discuss the correctness (safety, deadlock, lockout) of the solution for mutual exclusion shown in Fig. 3.15.

(b) Generalize to n processes.

(c) What would happen if the primitive EX instruction were replaced by the three assignments?

(d) *Modify the implementation kit to include the EX instruction.
program exchange;
var c: integer;
procedure p1;
var l: integer;
begin
l := 0;
repeat
  rem1;
  repeat
    EX (c,l)
  until l = 1;
  crit1;
  EX (c,l)
forever
end;
procedure p2;
var l: integer;
begin
l := 0;
repeat
  rem2;
  repeat
    EX (c,l)
  until l = 1;
  crit2;
  EX (c,l)
forever
end;
begin (* main program *)
c := 1;
cobegin
  p1; p2
coend
end.

Fig. 3.15.

3.7*If we allow \( P_2 \) to terminate in \( rem2 \), what changes need to be made in the proof of the liveness of Dekker’s algorithm? (Hint If \( P_2 \) is terminated in \( rem2 \), then it is true by I2 that \( c_2 \) is held at 1).
4 SEMAPHORES

4.1 INTRODUCTION

The scientific study of concurrent programs was given a decisive thrust with
the introduction of the semaphore by Dijkstra. Semaphores are easy to
implement and yet sufficiently powerful that they can be used to give elegant
solutions to concurrent programming problems. They can be used to define
or implement more powerful structured primitives.

A semaphore $s$ is an integer variable which can take on only non-zero
values. Once $s$ has been given its initial value, the only permissible opera-
tions on $s$ are to call the procedures $\text{wait}(s)$ and $\text{signal}(s)$ which are primitive
operations (the original notation is $P(s)$ for $\text{wait}(s)$ and $V(s)$ for $\text{signal}(s)$,
which are the first letters of the corresponding words in Dutch). The defini-
tion of these operations is as follows:

$\text{wait}(s)$: If $s > 0$ then $s := s - 1$ else the execution of the process that called
$\text{wait}(s)$ is suspended.

$\text{signal}(s)$: If some process $P$ has been suspended by a previous $\text{wait}(s)$ on this
semaphore $s$ then wake up $P$ else $s := s + 1$.

Remark 1 If the semaphore only assumes the values 0 and 1, it is called
a binary semaphore. A semaphore which can take arbitrary non-negative
integer values is called a general semaphore.

Remark 2 $\text{wait}$ and $\text{signal}$ are the only operations allowed. In particular,
assignments to $s$ or tests of the value of $s$ are prohibited except for an
assignment to $s$ of an initial non-negative value in the main program. (The
implementation kit does not enforce this restriction nor does it distinguish
binary from general semaphores.)

Remark 3 We have defined the procedures as primitive operations.
This means that they exclude one another just as Load and Store to the same
memory word exclude one another. (Semaphore operations on distinct semaphores need not exclude one another). Hence if a wait and a signal (or two wait's or two signal's) occur simultaneously they are executed one at a time though we do not know in what order they are executed.

Remark 4 The definition of signal does not specify which process is woken if more than one process has been suspended on the same semaphore. For the purpose of constructing a scenario you may assume that any process you wish is in fact selected. A FIFO semaphore which maintains a first-in, first-out queue of suspended processes could also be defined. There are more sophisticated definitions of fairness but that is a slightly more advanced topic and we suggest that you skip it on the first reading.

(Advanced) Remark 5 The classical (busy-wait) definition of semaphores is even weaker:

\textit{wait}(s): \textbf{when} \ s > 0 \ \textbf{then} \ s := s - 1.

Read this as: whenever the value of \( s \) is greater than zero, the process may execute \( s := s - 1 \) and continue.

\textit{signal}(s): \ s := s + 1.

Suppose that process \( P \) executes \textit{signal}(s) when the queue contains the blocked processes \( Q_1, \ldots, Q_k \). This definition does not guarantee that any of the \( Q_1, \ldots, Q_k \) are woken. The interleaving of execution sequences allows any process (even \( P \)) to execute \textit{wait}(s) and decrement \( s \) before any of \( Q_1, \ldots, Q_k \) have a chance to do so.

Another definition is that of the strongly fair semaphore which is assumed to have the following property:

If \( P \) is suspended on \( s \) and \( s \) becomes greater than zero infinitely often then eventually \textit{signal} will choose to wake \( P \).

(End of Remark 5)

4.2 MUTUAL EXCLUSION

Figure 4.1 is a solution to the mutual exclusion problem using semaphores.

\begin{verbatim}
program mutualexclusion;
var s: (* binary *) semaphore;
procedure p1;
beginn
repeat
    wait (s);
    crit1;
    signal(s);
    rem1
forever
end;
\end{verbatim}
procedure $p_2$;
begin
repeat
    wait(s);
    crit2;
    signal(s);
    rem2
forever
end;
begin (* main program *)
    $s := 1$;
    cobegin
        $p_1; p_2$
    coend
end.

Fig. 4.1.

All the synchronization is veiled by the powerful features of the semaphore. That is the way it should be. Language features are defined; compiler writers and systems programmers figure out how to implement it; and everyone else uses the feature with a reasonable assurance that it will work.

Let us examine this algorithm in detail with the aid of the igloo model. Our igloo (Fig. 4.2) now has in addition to its blackboard a deep-freezer. A process enters and performs a wait: if there is a 1 on the board it can enter its critical section; otherwise, it goes into hibernation in the freezer. Note that once a process enters the freezer it has cleared the interior of the igloo and
another process can enter even though the first process has not actually "completed" the execution of the wait. As an implementation detail, the freezer (= queue of suspended processes) must be large enough to contain the number of processes in the system or at least the number of processes that may be waiting on the semaphore s.

Upon completion of the critical section, the signalling process enters the igloo and releases a process from the freezer. If there are no such processes, it simply chalks up a one to indicate that the critical section is free. In the case of a binary semaphore, a signalling process will always find a zero on the board (why?). If the blackboard of a general semaphore has any non-zero number written on it, the process can deduce that the freezer is empty (why?).

This solution to the mutual exclusion problem is very similar to one of our earliest attempts in the previous chapter in which we had the processes pass the key to the critical section back and forth. We are saved from trouble here by the fact that the testing of s and the setting of s to zero are encapsulated in one primitive instruction. Thus if P₁ notes that s is 1, it will set s to 0 before P₂ has a chance to test the value of s.

Mutual exclusion and absence of deadlock are easy to show from the following property of the program: s will have the value zero if and only if exactly one process is in its critical section. This can be formally proved as follows. Consider the value of the expression \( E = s + \text{the number of processes in a critical section} \). Certainly \( E = 1 \) at the start of the concurrent program since \( s = 1 \) and no process is in a critical section.

Now use the following inductive argument. Assume that \( E = 1 \) at any point in any interleaved execution sequence. The execution sequence continues by choosing to execute either a step of P₁ or a step of P₂. We argue by inspecting the program that in any case the truth of \( E = 1 \) is preserved. Hence by induction, \( E = 1 \) is always true because any execution sequence is constructed starting from the initial state by successively choosing either a step of P₁ or of P₂. For example, if \( E = 1 \) because there are no processes in the critical section and \( s = 1 \), P₁ can choose to enter the critical section by executing wait(s). It leaves \( s = 0 \) and number of processes in the critical section = 1, i.e. \( E = 1 \).

The formula \( E = 1 \) is called an invariant of the computation. Invariants are proved by induction. The initial state of the computation satisfies the invariant and every transition between possible states of the computation preserves the truth of the invariant. To prove this, we assume the truth of the invariant as an induction hypothesis and then check that the invariant is still true in the new state resulting from the transition.

Note that, even in this simple case, the full proof is rather tedious since the induction step must be proved for every pair: (location of P₁'s program counter, location of P₂'s program counter). Of course, most steps are trivial.
The only ones needing any reasoning are executions of the semaphore instructions.

We are now in a position to prove the liveness of the solution.

**Theorem** \((P_1 \text{ wishes to enter } \text{crit}1) \implies \text{eventually } (P_1 \text{ enters } \text{crit}1)\).

**Proof**

1. \((P_1 \text{ wishes to enter } \text{crit}1) \implies \text{eventually } (P_1 \text{ enters } \text{crit}1) \text{ or } (P_1 \text{ is indefinitely suspended because } s=0)\).
2. \((P_1 \text{ is indefinitely suspended because } s=0) \implies (P_2 \text{ is in } \text{crit}2)\).
   This follows from the invariant \(E=1\) and the fact that there are only two processes \(P_1\) and \(P_2\).
3. \((P_2 \text{ is in } \text{crit}2) \implies \text{eventually } (P_2 \text{ executes } \text{signal}(s))\).
   We assume that no process is terminated in its critical section.
4. \((P_2 \text{ executes } \text{signal}(s)) \text{ and } (P_1 \text{ is indefinitely suspended because } s=0) \implies (P_1 \text{ enters } \text{crit}1)\).
   See the definition of the \text{signal} operation.
5. \((P_1 \text{ wishes to enter } \text{crit}1) \implies \text{eventually } (P_1 \text{ enters } \text{crit}1)\).
   The possibility that \(P_1\) is indefinitely suspended on \(s=0\) has led to a contradiction.

**Remark** Note that in (4) we have tacitly used the fact that there are only two processes. Otherwise we could not prove that \(P_1\) enters its critical section and not some other process.

*(Advanced) Remark* (4) of course does not hold under the busy-wait definition of semaphores. In fact lockout is possible under that definition if the signalling process executes another \text{wait} before the suspended process notes that \(s > 0\). However, fair semaphores are sufficient to prove absence of lockout though a proof such as ours would have to be invoked inductively so that eventually some \text{signal} would in fact wake \(P_1\).

(End of Advanced Remark).

The mutual exclusion problem for \(n\) processes is solved by the identical program (Fig. 4.3).

```plaintext
procedure mutualexclusion;
const n = \ldots ; (* number of processes *)
var s: (* binary *) semaphore;
procedure process(i: integer);
begin
    repeat
        wait(s);
        crit;
```
\begin{verbatim}
signal(s);
rem
forever
end;
begin (* main program *)
s := 1;
cobegin
  process(1);
  process(2);
  \ldots
  process(n)
coend
end.
\end{verbatim}

Fig. 4.3.

In this case lockout is a possibility. Suppose there are three processes and that the arbitrary choice of a process woken by signal is such that the process with the lowest index is always chosen. Then \( P_3 \) could be indefinitely delayed as \( P_1 \) and \( P_2 \) conspire to wake each other up.

(Advanced) Remark Morris has found a lockout-free solution to the mutual exclusion problem for \( n \) processes. The solution is very complex and uses additional variables and semaphores to set a limit on the size of a "batch" of processes that may simultaneously wait on the semaphore used for mutual exclusion. Since every process eventually completes its critical section and leaves the batch, all these processes will be eventually processed before a new batch is allowed to compete for mutual exclusion. The solution depends on the definition of semaphores that requires a signalling process to wake a waiting process.

(End of Advanced Remark).

Consider the problem of allowing at most \( k \) out of the \( n \) processes to simultaneously access the critical section. For example, a computer with two printers could allow two jobs to be printed simultaneously. The only change needed is to initialize the semaphore to \( k \). \( k \) processes will successfully decrement \( s \) until its value is zero. Then a process must wait until one of these \( k \) processes completes its critical section and signals. We can see here that it is necessary for signal also to be a primitive instruction. Otherwise if \( k = 3 \), \( s = 1 \) and two processes leave their critical sections simultaneously then the concurrent execution could leave \( s = 2 \) even though all processes are now out of their critical sections.

Can this be done using binary semaphores only? The answer is yes, but the solution is difficult. In the Exercises you can study the solution found by Kessels and Martin (1979).
4.3 THE PRODUCER–CONSUMER PROBLEM

Along with mutual exclusion, the producer–consumer problem is an abstraction of applications of concurrent programming that are found throughout operating systems. We choose to introduce this problem here because the semaphore has a natural interpretation in terms of the producer–consumer problem and because Dijkstra’s presentation offers another elegant series of solutions to a concurrent programming problem.

The producer–consumer problem arises because the producer of data must have somewhere to store it until the consumer is ready and the consumer must not try to consume data that is not there. It is perfectly valid to require that a rendezvous between the two must take place. Then the producer produces if and only if the consumer is ready to consume. If either process arrives early then it is required to wait. The rendezvous is the reasonable thing to do unless the two processes have a common memory. It is the basis of the Ada synchronization primitives.

If, however, the data rates of the producer or the consumer vary during the execution of the program then buffering is necessary. An example is the type-ahead feature found on most terminal systems. The user is allowed to produce several commands without waiting for the computer to consume each command. Similarly, the computer may produce more information than can be conveniently presented on the terminal screen. A buffer is used to average out such peak data rates.

A buffer is a segment of memory common to both the producer and the consumer. If the buffer is large enough to handle peaks of data production, both producer and consumer maintain a steady high average rate of data transfer without fearing a malfunction because of occasional peaks. The operation of a buffer is the same as that of a shock absorber in a car which stores a peak of energy and then releases it slowly so that both the car and its occupants can tolerate this input of energy. If a bump is hit which is beyond the capacity of the shock absorber or if the bumps are produced at a rate too rapid to allow the shocks to be consumed by a slow release of energy, then the result is unfortunate for the owner of the car.

A related use of buffers is to accommodate I/O equipment that accepts only aggregates of data. Disks and tapes can read and write only blocks of

\[
\text{repeat}
\]
\[
\begin{align*}
    & \text{produce record } v; \\
    & b[\text{in}] := v; \\
    & \text{in} := \text{in} + 1 \\
\end{align*}
\]

\text{forever;}

Fig. 4.4.
data. Many terminal systems require that complete messages be transmitted instead of individual characters. Even though both the producer and the consumer may be working at the same average rate, the artificial imbalance caused by blocking the data requires that buffering be used.

For now, let us assume that we have an infinite buffer. In programming notation this can be expressed as an infinite array: \( b[0], b[1], \ldots \). The producer can then simply pour his data into the buffer (Fig. 4.4) (\( in \) is a global variable that counts the number of records produced). The consumer on the other hand must assure that it is not consuming from an empty buffer (Fig. 4.5) (\( out \) is a variable that counts the number of records consumed). Initially we set \( in = out = 0 \). Note that we have abstracted away many details of the actual buffering process, in particular the structure of the records and the processing to be done with them. However, the main idea of buffering is captured.

\[
\text{repeat} \\
\quad \text{wait until } in > out; \\
\quad w := b[out]; \\
\quad out := out + 1; \\
\quad \text{consume record } w \\
\text{forever;}
\]

Fig. 4.5.

![Buffer Diagram](image)

Fig. 4.6.

Let \( s = in - out \) (Fig. 4.6). \( s \) is then the number of records in the buffer. What values can \( s \) take? \( s \) is initially 0. \( s \) can increase and then decrease arbitrarily except that if \( s \) reaches 0 then the consumer will refuse to reduce \( s \) below 0. Instead it waits until the producer places another value in the buffer. If we arrange for the producer to force the consumer into immediate consumption of this new value then \( 0 = in - out = (in + 1) - (out + 1) \).

\( s \) behaves like a semaphore. In fact the statement \( \text{wait until } in > out \) in the consumer can easily be implemented by \( \text{wait}(s) \) assuming that \( \text{signal}(s) \) is added to the producer to wake up the consumer. Thus a solution to the producer–consumer problem can be written as shown in Fig. 4.7 (where we have further abstracted the buffer manipulations by \( \text{append} \) (to buffer) and \( \text{take} \) (from buffer)).
program producerconsumer;
var n: semaphore;
procedure producer;
begin
  repeat
    produce;
    append;
    signal(n)
  forever
end;
procedure consumer;
begin
  repeat
    wait(n);
    take;
    consume
  forever
end;
begin (* main program *)
  n := 0;
  cobegin
    producer; consumer
  coend
end.

Thus the semaphore can be viewed as counting the difference between the number of signals sent by signal and the number of signals received by wait. It is the mere fact of signalling that is being counted and not the content of the signal. A semaphore can be implemented by a message passing system though it is wasteful to use the fixed size message element to transmit a null message.

4.4 MORE ON THE PRODUCER–CONSUMER PROBLEM

We now describe a series of solutions to the producer–consumer problem under a different hypothesis than in the previous section. Let us assume that the statements append and take are critical sections that must not overlap.

(Advanced) Remark A buffering system may be implemented as a chain of small buffers linked together. Obtaining or releasing a small buffer is usually a critical section to ensure the consistency of the pool of free buffers. Another common situation that requires mutual exclusion is the case of multiple producers or consumers. For example, all the terminals in a transaction processing system might place their request in a single queue;
this would be an instance of multiple producers. If a second processor were
added to the system to improve its performance, we would have multiple
consumers.
(End of Advanced Remark).
In the program in Fig. 4.8, a (binary) semaphore s is used in addition to
the general semaphore n to achieve mutual exclusion.

\begin{verbatim}
program producerconsumer;
var n: semaphore;
s: (* binary *) semaphore;
procedure producer;
begin
  repeat
    produce;
    wait(s);
    append;
    signal(s);
    signal(n)
  forever
end;
procedure consumer;
begin
  repeat
    wait(n);
    wait(s);
    take;
    signal(s);
    consume
  forever
end;
begins (* main program *)
  n := 0;
  s := 1;
  cobegin
    producer; consumer
  coend
end
\end{verbatim}

Fig. 4.8.

Suppose that a programming bug was made and that instead of
signal(s); signal(n) was written signal(n); signal(s). This shouldn’t affect the
safety of the solution because the solution must be safe even if the interleav-
ing is such that the two signal’s are executed successively with no intervening
statements from other processes. It is conceivable that the liveness could be
affected since the release of one waiting process out of turn could allow it to
conspire against other processes. There is an example of this in the lockout-
free algorithm of Morris mentioned earlier. In this case, fortunately, such a
bug does not affect the liveness. The consumer must wait on both
semaphores before consuming. Since a signal is never blocked and there is
only one waiting process, it does not matter in which order the signals are
issued. If the consumer is released from the wait(n) by signal(n) it will still be
prevented from taking prematurely by wait(s).

On the other hand, exchanging the waits is fatal. Consider the following
simple scenario: the consumer executes wait(s) which is successful (because s
is initially 1) and then it is blocked by wait(n) (because n is initially 0). But
now s is 0 and the producer will never be able to append to the buffer. Thus
the system is deadlocked.

This shows up a serious weakness of semaphores. There is no way to
conditionaly enter or leave a wait; nor is there a way to examine the value of
the semaphore without executing a wait and becoming vulnerable to being
blocked. A more powerful primitive which does not have this weakness is the
conditional critical region. This region evaluates an expression on the ordi-
nary program variables unlike the semaphore variable which is not freely
accessible. For the time being, we continue our discussion of the low level
semaphore and later we return to more powerful primitives.

An advantage of semaphores is that they are easy to implement; in
particular, binary semaphores are simple to implement because we do not
have to worry about the maximum value that needs to be provided for as is
the case with the general semaphore. One bit is enough. The next solution
(Fig. 4.9) to the producer–consumer problem is by binary semaphores only.
Of course we will need an integer variable n to count the number of elements
in the buffer since that information will no longer be stored in the
semaphore. The semaphore delay will block the consumer if the buffer is
empty.

```plaintext
program producerconsumer;
var
  n: integer;
  s: (* binary *) semaphore;
  delay: (* binary *) semaphore;
procedure producer;
begin
  repeat
    produce;
    wait(s);
    append;
    n := n + 1;
    if n = 1 then signal(delay);
    signal(s)
  forever
end;
```
procedure consumer;
var   m: integer; (* a local variable *)
begin
    wait(delay);
    repeat
        wait(s);
        take;
        n := n - 1;
        m := n;
        signal(s);
        consume;
        if m=0 then wait(delay)
    forever
end;
begin (* main program *)
    n := 0;
    s := 1;
    delay := 0;
    cobegin
        producer; consumer
    coend
end.

Fig. 4.9.

Note the initial wait(delay) so that the consumer does not begin to execute while the buffer is empty. Also, if the processes are running at more or less the same speed, neither is ever blocked on the semaphore delay. This is because wait(delay) is executed only if the buffer is emptied which need not occur frequently. The wait(delay) has been taken out of the wait(s) ... signal(s) bracket to avoid the previously discussed deadlock.

The new feature in the solution is the use of the local variable m to allow the consumer to test the value of n as it was inside the critical section. If the statement in the consumer had read: if n=0 then wait(delay) then the following scenario shows that a superfluous signal can occur which leads to consumption from an empty buffer—a flagrant breach of safety. Define a cycle of the producer (consumer) as execution of the statements of the producer (consumer) process from one occurrence of the produce (consume) to the next.

In the line marked (*) the consumer has skipped the wait in the statement if n=0 then wait(delay) because even though it noted that n=0, the producer has meanwhile incremented n. The notation n = −1 means that the consumer has just consumed an element that is not there: −1 = n = in − out so out = in + 1, i.e. the consumer has consumed its (in + 1)st element while the producer has produced only in elements.
Action  \hspace{1cm} n \hspace{1cm} delay
Initially \hspace{1cm} 0 \hspace{1cm} 0
Producer cycles \hspace{1cm} 1 \hspace{1cm} 1
Consumer executes to consume \hspace{1cm} 0 \hspace{1cm} 0
Producer cycles \hspace{1cm} 1 \hspace{1cm} 1
Consumer cycles \hspace{1cm} 0 \hspace{1cm} 1(*)
Consumer cycles \hspace{1cm} -1 \hspace{1cm} 0

Using the local variable \( m \), this bug will not occur (Check!). It is true that the consumer is making a decision based on stale information: it could be the case that, meanwhile, the producer has produced a new element. Then the consumer will execute \textit{wait}(delay) and immediately pass it if the producer has already signalled. The overhead of a superfluous \textit{wait} is certainly preferable to a violation of safety.

4.5 THE SLEEPING BARBER

There is another slight improvement that can be made to this program. The point of this discussion is not so much the improvement itself which may or may not be significant. What is interesting is how a careful analysis of the synchronization requirement in a problem can lead to a different and better solution. The moral of the story will be that before you decide to wait on a semaphore, you must clearly understand what you are waiting for.

Suppose we have the (common) case where the producer and consumer are running at roughly the same speed. The scenario could be:

Producer: \textit{append}; \textit{signal}; \textit{produce}; \ldots ; \textit{append}; \textit{signal}; \textit{produce}; \ldots
Consumer: \textit{consume}; \ldots ; \textit{take}; \textit{wait}; \textit{consume}; \ldots ; \textit{take}; \textit{wait}; \ldots

The producer always manages to append a new element to the buffer and signal during the consumption of the previous element by the consumer. This is not unreasonable since the processing to be done with the data is assumed to be significant compared with the buffer manipulation and the synchronization. The producer is always appending to an empty buffer and the consumer is always taking the last element in the buffer; hence the execution of \textit{signal} and \textit{wait} on every cycle. Thus even though the consumer will never block on the semaphore, the processes nevertheless are executing a large number of calls to the semaphore mechanism which does involve non-negligible overhead.

In the program in Fig. 4.10, we allow \( n \) to have the value \( -1 \) which is to mean that not only is the buffer empty but that the consumer has detected this fact and is going to block until the producer supplies fresh data.
program sleepingbarber;
var n: integer;
s: (* binary *) semaphore;
delay: (* binary *) semaphore;

procedure producer;
begin
repeat
produce;
wait(s);
append;
n := n + 1;
if n = 0 then signal(delay);
signal(s)
forever
end;

procedure consumer;
begin
repeat
wait(s);
n := n - 1;
if n = -1 then
begin
signal(s);
wait(delay);
wait(s)
end;
take;
signal(s);
consume
forever
end;
begin (* main program *)
n := 0;
s := 1;
delay := 0;

cobegin
  producer; consumer
coend
end.

Fig. 4.10.

Before the consumer waits on delay it is careful to release mutual exclusion by signalling s to allow the producer to append a new element to
the buffer. The structure of the consumer shows an alternative programming
construct to the use of a local variable as in the previous program. The test on
n is made inside the critical section and the waiting outside. Since the test is
made inside, there is no chance for the producer to change the value of n
between the decrement of n and the test.

Once the delay is completed we are careful to ask for the return of
mutual exclusion, hence the extra wait(s). If we try the scenario sketched at
the beginning of this section we find that even if there was only a single
element in the buffer, after \( n := n - 1 \) the value of n will be zero so the
consumer falls through to consume. If the producer can append a new
element fast enough, the consumer need never execute the wait(delay).

The two solutions can be illustrated by the model of the Sleeping
Barber. A barber has a two-room shop as shown in Fig. 4.11. One room with
the barber-chair and a waiting room. The three doors shown are: from the
street to the waiting room, from the waiting room to the chair and from there
back to the street. The doors are assumed to be narrow and allow at most one
person to pass at a time (the common memory arbiter). Let us now model the
stream of customers as a data elements which the barber must “consume”.
The waiting room is the buffer. We now write algorithms for both the barber
and the customers.
Algorithm 4.1

Barber When you have finished with a customer, show him out and check the waiting room. If there is a customer, escort him to the chair; otherwise, go to sleep in the chair.

Customer When you enter the waiting room: if there are other customers then join them. If not, open the door to see if the barber is busy; if so, close the door and wait your turn. If the barber is asleep then wake him.

In Algorithm 4.1, if the rate at which customers enter matches the rate of the barber’s work then every customer will find himself alone in the waiting room and will vainly open the door only to find the barber at work. This corresponds to the more obvious solution to the producer–consumer problem.

Algorithm 4.2

Barber As before, except that if the waiting room is empty then go to sleep on the bench in the waiting room.

Customer If there are other customers or if the waiting room is empty then wait your turn. If the barber is sleeping in the waiting room then wake him.

In Algorithm 4.2, a customer will wait without opening the door to no avail. Eventually the barber will finish with the previous customer and invite the new one in. Only if the barber is actually waiting (sleeping) will a customer have to wake him.

4.6 THE BOUNDED BUFFER

An infinite buffer is not realistic. There are two basic techniques to bound the size of a buffer. The first is the circular buffer where the index of the array \( b \) is computed modulo the finite size of the array. That is, the data is wrapped around from the end of the array to its start. The code for a circular buffer is shown in Fig. 4.12 where \( n \) is the size of the array \( b \). See Fig. 4.13 to understand the boolean conditions that define empty and full buffers.

(* producer *)
produce;
wait until ( (in>=out) and (in-out<n) 
or (in<out) and (out-in>1) );
append;
if in=n then in := 1 else in := in+1;
(* consumer *)
wait until (in <> out);
take;
if out=n then out := 1 else out := out+1;
consume;

Fig. 4.12.
There is always at least one free space in $b$ so that $in = out$ can be unambiguously identified as an empty buffer, not a full one.

The other method of bounding the size of buffers is to use two or more distinct buffers, usually of the same size. When one is filled by the producer it is passed on to the consumer which for its part promises to return the empty buffers to the producer for re-use. The circular buffer is very easy to program and very thrifty of space since there is only one buffer element of overhead. The multiple buffers need to be programmed with some care since a mutual exclusion mechanism must be invoked during the transfer of a buffer from one process to another. Multiple buffers can waste space. Suppose the producer has filled $b_1$ but the consumer still has a few elements left to consume in buffer $b_2$ (Fig. 4.14). Then the producer must wait for the consumer even though almost half of the overall buffer space is currently empty.
Multiple buffering is used in several situations. I/O equipment that uses direct memory access may not have the ability to work with a circular buffer. Typically such equipment accepts commands that consist of an address and a length of a memory segment into which the data is to be written. This translates nicely into a discrete buffer to be filled and passed to the program. Another important use for multiple buffers is in communication systems where the buffer requirements are highly variable in time. Rather than allocate a large circular buffer permanently to each terminal, it is better to construct a “pool” of many small buffers. An inactive terminal need not be assigned any buffers; active terminals can be assigned a large number of buffers from the pool to be returned once the data transfer is completed.

To change the producer–consumer problem to handle bounded buffers is very simple. Just as the general semaphore \( n \) counts the number of elements of the buffer currently filled by data, the program in Fig. 4.15 uses another semaphore \( e \) to count the number of empty spaces! When \( e \) reaches zero there are no empty spaces and the producer blocks until the consumer removes some of the data. The solution has a pleasantly symmetric form.

```plaintext
program boundedbuffer;
const sizeofbuffer = . . . ;
var s: (* binary *) semaphore;
n: semaphore;
e: semaphore;

procedure producer;
begin
  repeat
    produce;
    wait(e);
    wait(s);
    append;
    signal(s);
    signal(n)
  forever
end;

procedure consumer;
begin
  repeat
    wait(n);
    wait(s);
    take;
    signal(s);
    signal(e);
    consume
  forever
end;
```
begin (* main program *)
  s := 1;
  n := 0;
  e := sizeofbuffer;
  cobegin
    produce; consume
  coend
end

Fig. 4.15.

4.7 EXERCISES

4.1 Write several tests until you thoroughly understand the difference between Figs. 4.9 and 4.10.

4.2 Conway's Problem: Write a program to read 80-column cards and write them as 125-character lines with the following changes. After every card image an extra blank is inserted. Every adjacent pair of asterisks ** is replaced by \&.

Of course Conway's problem can be solved by a single sequential program. However, it is difficult to be sure that you have taken care of all of the special cases such as pairs of asterisks at the end of a card and so on.

The problem has an elegant solution as three concurrent processes. One process read reads the cards and passes characters through a one character buffer to a process squash. read also passes the extra blank at the end of every card image; squash, which knows nothing about 80-column cards, simply looks for double asterisks and passes a stream of modified characters to a process print. print takes the characters and prints them as 125-character lines.

4.3 Write a program to solve Conway's problem with the additional requirement that there be a 10-character buffer between each pair of processes: read and squash; squash and print. Use mutual exclusion on the bounded buffer as shown in Fig. 4.15.

4.4 In Fig. 4.12, simplify the condition in the producer's wait until clause.

4.5 Write a scenario that shows that signal must be a primitive instruction and not simply s := s+1.

4.6 Add a semaphore to program increment (Fig. 1.5) so that it always prints 40.

4.7 Write sortprogram so that merge is a third concurrent process.

4.8 Write a scenario showing lockout for the semaphore solution to mutual exclusion of three processes.
4.9 If you want to pass a semaphore as a parameter, should it be passed as a value parameter or a reference parameter (var in Pascal), or does it not make any difference? If you think that there is a difference, what happens if you make the wrong choice?

4.10 Why is the program in Fig. 4.16 not a solution to the problem of allowing at most \( k \) processes into a critical region (using binary semaphores only)?

(a) Show that if \( k = 2 \) and \( n = 4 \) it is possible to have \( \text{delay} = 2 \) contrary to the requirement that \( \text{delay} \) is a binary semaphore.

(b) *Show this even for \( k = 2 \) and \( n = 3 \).

```pascal
program mutual_exclusion;
const
  n = ...; (* number of processes *)
  k = ...; (* number in critical section *)
var
  count: integer;
  s: (* binary *) semaphore;
  delay: (* binary *) semaphore;
procedure process (i: integer);
var
  m: integer;
begin
  repeat
    wait(s);
    count := count - 1;
    m := count;
    signal(s);
    if m <= -1 then wait(delay);
    crit;
    wait(s);
    count := count + 1;
    if count <= 0 then signal(delay);
    signal(s)
  forever
end;
begin (* main program *)
  count := k;
  s := 1;
  delay := 0;
  cobegin
    process(1);
    process(2);
    ...
    process(n)
  coend
end.
```

Fig. 4.16.

4.11 (Kessels and Martin) A split binary semaphore is a pair of binary semaphores \( x \) and \( y \) such that the formula \( 0 \leq x + y \leq 1 \) is always true (i.e., is an invariant). Study the simulation (Fig. 4.17) of general semaphore \( s \) by the split binary semaphore.
A program using the general semaphore $s$ should now declare $s$ as an integer, assign it an initial non-negative value and then use the procedures genwait($s$) and gensignal($s$) below to simulate wait and signal for a general semaphore. The program must also declare and initialize global variables as shown.

```plaintext
count: integer; (* initially 0 *)
x: (* binary *) semaphore; (* initially 1 *)
y: (* binary *) semaphore; (* initially 0 *)

procedure genwait(var s: integer);
begin
  wait(x);
  while $s <= 0$ do
    begin
      count := count + 1;
      signal(x); wait(y);
      count := count - 1;
      if count=0 then signal(x) else signal(y);
      wait(x)
    end;
  s := s - 1
  if count=0 then signal(x) else signal(y)
end;

procedure gensignal(var s: integer);
begin
  wait(x);
  s := s + 1;
  if count=0 then signal(x) else signal(y)
end;
```

Fig. 4.17.

4.12 (Manna and Pnueli) Write a concurrent program to compute the binomial coefficient $(n \ k) = n(n-1) \ldots (n-k+1) / 1(2) \ldots (k)$, for $0 \leq k \leq n$. Let process $P_1$ multiply $n$ then $n-1$ then $n-2$ and so on into a global variable $x$ while process $P_2$ multiplies 1 and 2 and so on into a local variable $y$. Synchronize $P_1$ and $P_2$ so that $P_2$ executes $x := x \div y$ when $y$, in fact, divides $x$. (Hint: $i!$ always divides $j(j+1) \ldots (j+i-1).$

4.13 *(Roussel)* Write a concurrent program to test if two binary trees have the same leaves. There will be three processes: $P_i$, $i=1, 2$, will find the next leaf of tree $i$. When two "next" leaves have been found, $P_3$ will test them for equality. The trees can be declared in Pascal–S as follows:

```plaintext
const
  maxnodes = 40;
  lefson = 0;
  rightson = 1;
  nodevalue = 2;

type
  node = array[0..2] of integer;
  treetype = array[1..maxnodes] of node;

var
  tree: array[1..2] of treetype;
```
4.14 Study the implementation kit and describe the changes that must be made so that the kit will catch misuse of a semaphore: tests and assignments (except in the main program). What changes must be made to differentiate general from binary semaphore?

4.15 (Parnas) Figure 4.18 is a solution to a problem called the Cigarette Smoker’s problem. Each one of the three agents supplies two of three possible resources. There are three smokers each of which needs exactly the pair of resources supplied by one of the agents. Study (and test) the solution and answer the following questions.

(a) What is the function of the helper processes?
(b) Explain how termination of the tasks is accomplished. What is the purpose of \( t := 0 \) in procedure forcetermination?
(c) Even though the program terminates, there are certain bugs that may occur on the final execution of each process. Write examples for these bugs and a better program that terminates correctly.
(d) Do you see a problem that might occur with the semaphores \( s[1], s[2], s[4] \)? How can this problem be solved?

```plaintext
program cigarette;
const trips = 20;
var resource: array[1 . . 3] of (* binary *) semaphore;
    s: array[1 . . 6] of semaphore;
    mutex, sem: (* binary *) semaphore;
    t: integer;
    finished: array[1 . . 3] of boolean;
procedure forcetermination;
var i: integer;
begin
    t := 0;
    for i := 1 to 3 do signal(resource[i]);
    for i := 1 to 6 do signal(s[i])
end;
procedure agent(n, res1, res2: integer);
var i: integer;
begin
    for i := 1 to trips do
    begin
        wait(sem);
        signal(resource[res1]);
        signal(resource[res2]);
        writeln('agent', n)
        finished[n] := true
    end;
procedure helper(n, increment: integer);
begin
    repeat
        wait(resource[n]);
        wait(mutex);
        t := t + increment;
        signal(s[t]);
        signal(mutex)
```
until finished[1] and finished[2] and finished[3];
forcetermination
end;
procedure smoker(n, index: integer);
begin
  repeat
    wait(s[index]);
    t := 0;
    writeln ('smoker', n);
    signal(sem)
  until finished[n]
end;

begin (* main program *)
  for t := 1 to 3 do resource[t] := 0;
  for t := 1 to 6 do s[t] := 0;
  for t := 1 to 3 do finished[i] := false;
  t := 0;
  mutex := 1;
  sem := 1;
  cobegin
    agent(1,2,3); helper(1,1); smoker(1,6);
    agent(2,1,3); helper(2,2); smoker(2,5);
    agent(3,1,2); helper(3,4); smoker(3,3)
  coend;
  writeln('smoking is dangerous')
end.

Fig. 4.18.
5 MONITORS

5.1 INTRODUCTION

While the semaphore is an elegant low level synchronization primitive, an operating system built on semaphores alone is subject to disaster if even one occurrence of a semaphore operation is omitted or mistaken anywhere in the system. We should like to have a more structured synchronization tool. In sequential programming, one can write procedures out of simple statements and (hopefully) use the procedures by external specification only—by knowing the name and parameters of the procedure. The monitor is designed to allow concurrency while retaining the advantage of a structured construct.

The monitor grew out of two distinct ideas that are in common use. The first is the monolithic monitor used in current operating systems. Most of these systems are in effect single programs that centralize all critical functions. If a message must be passed from $P_1$ to $P_2$ then $P_1$ passes it to "big brother" monitor $M$ with a request to forward it to $P_2$, or at least $P_1$ requests permission to pass the message. Similarly, resource allocation is centralized in $M$. Such monitors are supported by hardware facilities that ensure the privileged position of the monitor: $M$ runs in an uninterruptable mode thus guaranteeing mutual exclusion; only $M$ can access certain areas of memory; only $M$ can execute certain instructions such as I/O instructions.

The monitors we study are decentralized versions of the monolithic monitor. Each monitor will be entrusted with a specific task and in turn it will have its own privileged data and instructions. Thus if $M_1$ is the only monitor that can access variable $v_1$ then we are ensured of mutual exclusion of access to $v_1$ because $M_1$ will be uninterruptable or as we say in the abstraction: entry to a monitor by one process excludes entry by any other process. In addition, since the only processing that can be done on $v_1$ is the processing programmed into the monitor, we are assured that no other assignments or tests
are accidently made on \(v_1\). We can design different monitors (or even different instances of the same monitor) for different tasks. Thus the system is both more efficient because execution of distinct monitors can be done concurrently, and more robust because a change in one monitor cannot surreptitiously change a variable in another monitor.

The other idea behind monitors is that of structuring data and structuring accesses to data in a programming language. Pascal was the first language specifically designed to structure data by typing. The purpose of data typing is to prevent indiscriminate mixing of data that have no purpose being mixed even though their representation may be identical. For example, even though it might occasionally be convenient to add a number to a character (and PL/I will be happy to do so), Pascal takes the view that such a statement is almost certainly in error and refuses to compile the statement. If this is what you really want then you must placate the compiler by writing an explicit conversion.

While typing is successful as far as it goes, it applies only to the data itself. There is no way in Pascal to define a type which consists of integers that may only be added or subtracted. There is no way of asking the compiler to flag a multiplication as unreasonable (in an accounting system, it might not make sense to multiply two sums of money—only to add and subtract them or to multiply a sum by an interest rate or a time period). The idea of typing by the operations performed is found in the language Simula 67. A class in Simula 67 is a data declaration together with a set of procedures which define the only legal operations that may be performed on the data. The Simula class has been combined with the Pascal data type in the Ada package feature which provides a carefully designed mechanism that allows the programmer to structure his program to reflect his knowledge of the properties of the data.

A monitor is a class that can be executed in turn by several processes. For example, even though the buffer is an array, there is no reasonable thing to do with a buffer except to append a new element or extract an old one. A random access to a buffer array is probably a mistake. To sort the elements of a buffer simply contradicts the definition of a buffer as an area of memory from which data is extracted in the same order that it was appended. In the monitor notation, once the buffer monitor has been written, there is no way to even express such a mistake. The compiler will refuse any access by a process to a buffer except through procedures append and take.

In this chapter we formally define the monitor as a programming primitive and give examples of its use. We show how to implement monitors on a system with semaphores. Monitors have been used very successfully in concurrent programming languages such as Concurrent Pascal and CSP/k.
5.2 DEFINITION OF MONITORS

A monitor is written as a set of (global) variable declarations followed by a set of procedures (which may be parameterized). The monitor has a body (begin . . . end) which is a sequence of statements that is executed immediately when the program is initiated. The body is used to give initial values to the monitor variables. Thereafter, the monitor exists only as a package of data and procedures.

The variables in the monitor are directly accessible only within the monitor procedures. Communication between a monitor and the outside world is through the parameters of the procedures. In the usual vocabulary of programming languages, the scope of the monitor variables is the monitor (= set of monitor procedures). Since the monitor is a static object: variable declarations and procedure declarations, the only way to execute the monitor is for a process to call a monitor procedure.

```pascal
program producerconsumer;
const    sizeofbuffer = . . . ;
monitor boundedbuffer;
b: array [0 . . sizeofbuffer] of integer;
in, out: integer;
n: integer;
procedure append (v: integer);
begin
  if n = sizeofbuffer+1 (* the buffer is full *)
    then “wait until not full”,
      b[in] := v;
      in := in+1;
      if in = sizeofbuffer+1 then in := 0;
      n := n+1;
      “signal that the buffer is not empty”
end;
procedure take (var v: integer);
begin
  if n=0 (* the buffer is empty *)
    then “wait until not empty”;
      v := b[out];
      out := out+1;
      if out = sizeofbuffer+1 then out := 0;
      n := n - 1;
      “signal that the buffer is not full”
end;
```
\begin{verbatim}
begin (* monitor body *)
in := 0;
out := 0;
n := 0
end;
(* end of monitor boundedbuffer *)
procedure producer;
var v: integer;
begin
  repeat
    produce (v);
    append (v)
  forever
end;
procedure consumer;
var v: integer;
begin
  repeat
    take (v);
    consume (v)
  forever
end;
begin (* main program *)
cobegin
  producer; consumer
coend
end.
\end{verbatim}

Fig. 5.1.

Figure 5.1 shows a solution to the producer–consumer problem using a bounded buffer. It consists of a program—\textit{producerconsumer}—which contains a monitor—\textit{boundedbuffer}—and two concurrent processes—\textit{producer} and \textit{consumer}. When the program is initiated, the monitor body is first executed. Then the main program is executed which causes the initiation of the concurrent processes. The monitor procedures \textit{append} and \textit{take} sit passively until called from a process.

If a producer wishes to append an element \(v\) to the buffer, all it need do is call the monitor procedure \textit{append}(v). Similarly, the consumer can call \textit{take}(v) to obtain the next element. We require that entry to a monitor be done under mutual exclusion. Thus either the producer is executing \textit{append} or the consumer is executing \textit{take} (or neither). Then the operations on the variable \(n\) by both processes do not interfere with each other.

This solution has certain advantages over the unstructured semaphore solution aside from the mere fact of the protection of the variables from
outside interference and the structuring of the accesses. Since the mutual
exclusion is automatically guaranteed by the monitor, there is no counter-
part to a bug caused by omitting a signal to release mutual exclusion. If you
forget the end statement of monitor procedure, that is a compilation error
just as it would be in an ordinary program. In addition, the waiting and
signalling is programmed within the monitor. The users of the monitor need
only call a procedure. Thus once a monitor is correct, it will be correct for
every instance used by every set of processes. In the case of the unstructured
semaphore, the correctness depends upon semaphore operations that must
be explicitly programmed into every process.

For synchronization we need some sort of wait–signal commands. The
semaphore commands served two purposes. One is to provide a
block–wakeup facility and the other to maintain a count. Since the counts
can now be explicitly contained as integer variables in the protected monitor
data, it is sufficient to provide a block–wakeup facility. Just as several
semaphores may be needed in one program, so one monitor may need
several wait–signal pairs. We define a new type of variable called a condition
variable. If c is a condition variable then there are two commands that can be
applied to c: wait(c) and signal(c) (these will now be defined for monitors;
they are not to be confused with the commands of the same name for
semaphores—alternatively call the semaphore commands P and V):

\begin{description}
\item[wait(c)] The calling process is blocked and is entered on a queue of pro-
cesses blocked on this condition, i.e. have also executed wait(c)
commands. Unlike semaphores we assume that the queues are
FIFO.
\item[signal(c)] If the queue for c is not empty then wake the first process on the
queue.
\end{description}

Executing signal(c) when there are no processes waiting in the queue for c is
a no-operation and leaves no traces (again unlike the semaphore). The
commands may be worded: “I am waiting for c to occur” and “I am
signalling that c has occurred”. Of course it is the responsibility of the
monitor programmer to ensure that c has occurred when the signal is issued.

The execution of wait(c) releases the mutual exclusion on the entry to
the monitor. That this must be true is obvious. If \( P_1 \) is blocked waiting for c to
occur, some process \( P_2 \) must do the signalling. If \( P_1 \) is not assumed to release
the mutual exclusion then \( P_2 \) can never enter and the system is deadlocked. If
we model the monitor as an igloo, the blocked processes can be considered
to be in a deep-freezer in the basement. They do not take up room in the
igloo so other processes can move around. Of course when a process signals,
we must arrange either for the signalling process to leave the igloo immedi-
ately or for the blocked process to wait temporarily until the signalling
process does leave. This ensures that there is only one process at a time in the
igloo.
In the meantime we make the restriction that there be at most one signal per procedure and that it be the last statement in the procedure. Thus the signalling process leaves the monitor immediately after the signal. This evades the question raised in the last paragraph; we shall return to it in the last section.

**Immediate Resumption Requirement** Let a process execute signal(c) and suppose that there are processes in the queue for c as well as processes waiting to enter the monitor by a normal procedure call. Then the process on the head of the queue for c is the next process to enter the monitor; in particular it has priority over the processes which are trying to enter the monitor by procedure call.

Let us see why this requirement is needed. Suppose that process P₁ has noted that the condition is fulfilled and signals. If a process P₃ is allowed to enter the monitor (by a procedure call) before a process P₂ (which is waiting on condition c), then conceivably P₃ could cause c to become false. For example, if P₁ is a producer signalling buffer-not-empty and both P₂ and P₃ are consumers, then it would be fatal if the interloper P₃ consumed the single data element before the awakened process P₂ is allowed to proceed. Under the Immediate Resumption Requirement, however, P₂ can assume that whatever P₁ checked immediately before issuing the signal is still true because no interloper could falsify it between the signal and the resumption of the first blocked process.

Finally, to complete the bounded buffer example, we must declare two conditions in the variable declaration part of the monitor:

```
notempty, notfull: condition;
```

and replace the phrases in quotes by the commands:

```
wait(notfull)
signal(notempty)
wait(notempty)
signal(notfull),
```

respectively.

## 5.3 SIMULATION OF THE SEMAPHORE

The second example we describe is the implementation of a binary semaphore by a monitor. This is important theoretically since it shows that we have not lost any expressive power in the transition from semaphores to monitors. Practically, systems based on monitors are relatively common. If you have a ready-made semaphore algorithm you might want to run it as is on the monitor-based system.
The monitor (Fig. 5.2) will use a boolean variable busy which will indicate whether or not a wait operation has been completed on the semaphore (and hence that the critical section is "busy"). If the semaphore is busy, we must wait until it is not busy so according to the wording of the monitor operations we might as well call the condition notbusy. The two procedures will be called $P$ and $V$ to avoid confusion here with the monitor operations.

```plaintext
program mutualexclusion;
monitor semaphoresimulation;
var busy: boolean;
   notbusy: condition;
procedure P;
begin
   if busy then wait(notbusy);
   busy := true
end;
procedure V;
begin
   busy := false;
   signal(notbusy)
end;
begin (* monitor *)
   busy := false
end;
procedure $p_1$;
begin
   repeat
      $P$;
      crit1;
      $V$;
      rem1
   forever
end;
procedure $p_2$;
begin
   repeat
      $P$;
      crit2;
      $V$;
      rem2
   forever
end;
```
begin (* main program *)
cobegin
   p_1; p_2
coend
end.

Let us check that the various requirements are fulfilled. There is at most one signal in every procedure and when it does occur, it is the last statement in V. If a signal is executed when there are blocked processes then it is executed when busy is false; hence, a blocked process which is awakened need not check that busy is now false and can proceed to set it true. Note how the mutual exclusion of the monitor entry prevents the bugs we once had when two processes simultaneously checked a variable such as busy and then set it.

This implementation of a semaphore is the strongest implementation possible because of the FIFO assumption on the queue of processes blocked on a condition. The semaphore definition does not require FIFO but it certainly does not forbid it as a scheduling strategy. Thus any semaphore algorithm proved correct under a weaker assumption is still correct.

A condition variable does not have a value in the usual sense of the word and hence no initialization is needed. To be more precise, every condition variable is implicitly initialized to the empty queue of processes blocked on it.

It seems that we need a different monitor for each semaphore. In practice, systems using monitors allow one to declare multiple instances and even parameterized sets of monitors. If the monitor procedures are written as re-entrant\(^\dagger\) procedures (Pascal procedures are automatically re-entrant), it is sufficient to allocate new instances of the global variables for each instance of a monitor. In the case of the semaphore monitor, this means a new boolean variable busy and a new queue for the condition notbusy. But that is exactly the amount of storage needed for a semaphore under the direct definition!

5.4 THE READERS AND WRITERS PROBLEM

A generalization of the mutual exclusion problem is the problem of the readers and writers. The prototype for the abstract problem is an on-line

\(^\dagger\) A procedure is called reentrant if its code can be used simultaneously by several processes. This is accomplished by writing pure code: code which is not self-modifying and which accesses all its data indirectly from an address usually kept in a register. Thus by merely changing the address in the register and remembering the current location of the program counter, the same code can be switched among several programs. In Pascal, procedures are always pure code and data is accessed by stack pointers. Hence by changing the stack pointers, a procedure can be forced to work on a different set of data.
transaction system such as a banking system not requiring mutual exclusion among several processes which only read the data. However, an update or any operation that writes data must be considered to be a critical section to avoid the type of bugs which should be thoroughly familiar by now. A monitor to solve this problem is given in Fig. 5.3.

```
program readers_and_writers;
monitor readwrite;
var readers: integer;
writing: boolean;
oktoread, oktowrite: condition;

procedure startread;
begin
  if writing or nonempty (oktowrite) then wait(oktoread);
  readers := readers+1;
  signal(oktoread)
end;
procedure endread;
begin
  readers := readers-1;
  if readers = 0 then signal(oktowrite)
end;
procedure startwrite;
begin
  if readers <> 0 or writing then wait(oktowrite);
  writing := true
end;
procedure endwrite;
begin
  writing := false;
  if nonempty(oktoread) then signal(oktoread)
else signal(oktowrite)
end;
begin (* monitor *)
  readers := 0;
  writing := false
end;
```
procedure readprocess;
begin
  repeat
    startread;
    readthedata;
    endread
  forever
end;
procedure writeprocess;
begin
  repeat
    startwrite;
    writethedata;
    endwrite
  forever
end;
begin (* main program *)
cobegin
  readprocess; readprocess; (* . . . *)
  writeprocess; writeprocess; (* . . . *)
coend
end.  Fig. 5.3.

We have introduced a new primitive procedure into the monitor abstraction: nonempty(condition) which is a boolean valued function that returns true if and only if the queue for condition has blocked processes. If you examine the definition of signal(condition) you can see that it needs such an auxiliary function anyway so it is not unreasonable to require the implementer of monitors to provide the function for the programmer to use.

The number of readers that are reading or wish to read is counted by readers. Some process is writing if and only if writing is true. The two conditions are intended to mean literally what they say, e.g. "I am waiting for it being OK to read". We assume, of course, that the reading and the writing take a finite amount of time and that the processes do not accidentally terminate during reading and writing.

With the exception of the signal in startread, the monitor should not now be difficult to understand. The task of this signal is to perform what is known as a cascaded wake-up. If no readers are waiting when the signal is executed, then by definition it has no effect.

On the other hand, suppose that several readers $R_1, R_2, \ldots$ are blocked on oktoread because they began to execute startread during a write (and thus they found that the variable writing was true). When the write terminates, it will execute endwrite which signals oktoread. Since $R_1$ is at the head of the
queue, it will be awakened and complete procedure startread. Obviously at this time, no one is writing and we might as well let in $R_3$ and all the other readers to execute concurrently with $R_1$. To accomplish this, $R_1$ executes signal (oktoread) which wakes $R_2$. But the same consideration applies to $R_2$ which proceeds to wake $R_3$. This cascade of signals thus wakes all the readers in the queue for oktoread. The final reader will execute a signal on an empty queue but of course this has no effect.

The problem of the readers and the writers leaves much room for imaginative variations on the question of priority. Consider the following possible sequence of requests: $R_1, R_2, W_1, R_3, \ldots$. Obviously $R_1$ and $R_2$ can read concurrently and $W_1$ has to wait for the termination of the reads, but what about $R_3$? It seems a pity to have $R_3$ wait both for the readers to finish and for the writer $W_1$ to finish. Thus we might let $R_3$ have priority over waiting writers ($W_1$) and let it read concurrently with $R_1$ and $R_2$. But now suppose that the scenario continues with a long sequence of readers: $R_4, R_5, \ldots$. If new readers arrive in rapid succession, $W_1$ will be indefinitely delayed. This is what we have called lockout.

In the current solution the rule is:

1. If there are waiting writers then a new reader is required to wait for the termination of a write.
2. If there are readers waiting for the termination of a write, they have priority over the next write.

The test on the condition nonempty( oktowrite ) in startread ensures that if there are waiting writers (even if no-one is actually writing) then the new readers are blocked.

The if statement in endwrite ensures that if there are waiting readers at the termination of a write, they are given priority and awakened. The cascaded wakeup in startread will then wake up all currently waiting readers as required by the second clause of the rule. By the monitor requirement of immediate resumption, all the waiting readers will be awakened before any new readers are even allowed to enter the monitor. When new readers enter then they will block if there are waiting writers.

The selection of a priority scheme must be dictated by the application and no one scheme can be unreservedly recommended. In the exercises you can study programs which implement other schemes.

5.5 PROVING PROPERTIES OF MONITORS

Let us now give semi-formal proofs of some of the properties of this solution to the problem of the readers and the writers. Let $R$ be the number of processes currently reading and let $W$ be the number of processes currently writing.
When no process is currently executing a monitor procedure, the following formulae are true (i.e. the formulae are invariant outside the monitor).

(a) \( R = \text{readers}; \)
(b) \( W > 0 \) if and only if \( \text{writing} = \text{true}; \)
(c) \( \text{nonempty(oktoread)} \) only if \( \text{writing or nonempty(oktowrite)}; \)
(d) \( \text{nonempty(oktowrite)} \) only if \( \text{readers} \neq 0 \) or \( \text{writing}; \)

Each of these statements is initially true and it must be checked (Exercise 5.7 (a)) that, if a statement is true upon entry into a monitor procedure, it is still true when the process exits the procedure.

Points to remember are: execution of a \textit{wait} is also a way of exiting a monitor procedure; if a statement is true immediately before the execution of a \textit{signal} then, by the immediate resumption of an awakened process, the truth of the statement is transferred to the resumed process.

The basic safety property required of a solution to the problem of the readers and the writers will be proven if we can show that the following formula I is invariant:

If \( R > 0 \) then \( W=0 \) and if \( W > 0 \) then \( (W=1 \) and \( R=0). \)

In words: if there are (active) readers then there are no writers, and if there are (active) writers then there is only one writer and no readers.

I is initially true since \( R=W=0. \) We show that I is always true by showing that any attempt to describe an execution sequence which falsifies I is unsuccessful.

1. Suppose \( R > 0 \) and \( W=0 \) (so that I is true) and then I is falsified by some process starting to write (so \( W \) will become 1).

By (a), \( R > 0 \) implies \( \text{readers} > 0 \) so the process that wishes to write will \textit{wait} in procedure \textit{startwrite}. The only way this scenario could falsify I is if a \textit{signal(oktowrite)} occurs. The \textit{signal} in \textit{endread} is executed only if \( \text{readers}=0 \), contrary to assumption. The \textit{signal} in \textit{endwrite} will also not be executed since there are no writers by the assumption \( W=0. \)

2. Suppose \( R=0 \) and \( W > 0 \) and then some process starts reading so that \( R=1 \), falsifying I.

\( W > 0 \) implies \( \text{writing} = \text{true} \) by (b), so any process executing \textit{startread} will \textit{wait} on \textit{oktoread}. Since \( R=0 \), there are no readers so \textit{signal(oktoread)} is not executed in \textit{endread}. Now I is assumed true so \( W > 0 \) implies \( W=1. \) Thus executing \textit{signal(oktoread)} in \textit{endwrite} upon termination of writing occurs when \( W=0 \) contradicting the assumption of this scenario.

3. \( W=1, R=0 \) and then some process starts writing to falsify the second clause of I.
This is impossible by the code in startwrite. The only signal possible is the one from endwrite, but then \( R = W = 0 \) so I is not falsified.

The liveness properties of the solution are: if \( P \) wishes to read (or write) then eventually it will be allowed to do so. Let us prove the liveness of reading and leave the proof for writing as an exercise (see Exercise 5.7 (b)).

If \( P \) wishes to read then, it must successfully complete the execution of startread. If it cannot do so, it must become enqueued indefinitely on oktoread. We prove that oktoread is signalled indefinitely often. Since the queue is FIFO and the number of processes \( P_1, \ldots, P_k \) ahead of \( P \) is finite, eventually \( P \) must be awakened and allowed to read.

By (c) above, either writing = true or nonempty( oktowrite ). If writing = true then by (b), \( W > 0 \) so some process \( Q \) is writing.

(i) \( (Q \text{ is writing}) \text{ implies eventually (} Q \text{ executes endwrite}) \) by the assumption on critical sections that writing terminates.

(ii) \( (Q \text{ is in endwrite}) \text{ implies eventually (} Q \text{ executes signal( oktoread ))} \), by the assumption that \( P \) is indefinitely enqueued on oktoread so that nonempty( oktoread ) is true.

(iii) \( (Q \text{ executes signal ( oktoread ))} \text{ implies eventually (} P_1 \text{ executes signal( oktoread ))} \), by the immediate resumption of a waiting process and the code in startread.

(iv) \( (P_1 \text{ executes signal ( oktoread ))} \text{ implies eventually (} P_2 \text{ executes signal( oktoread ))} \), by immediate resumption and the code in startread.

(v) \( (Q \text{ is writing}) \text{ implies eventually (} P_k \text{ executes signal( oktoread ))} \), by (i)–(iv) and induction.

It easily follows that eventually \( P \) must successfully complete startread and commence reading.

Suppose now that writing = false but nonempty( oktowrite ) = true. By (d) and the assumption that writing = false, readers \( \neq 0 \) and thus by (a) there must be \( P_1, \ldots, P_k \) currently reading.

(i) \( (P_1, \ldots, P_k \text{ are all the reading processes}) \text{ implies eventually ((some } P_i \text{ executes endread) and } (P_1, \ldots, P_{i-1}, P_{i+1}, \ldots, P_k \text{ are all the reading processes))}, \text{ since reading terminates and nonempty( oktowrite ) blocks new readers.}

(ii) \( (P_1, \ldots, P_k \text{ are all the reading processes}) \text{ implies eventually ((some } P_j \text{ executes endread) and (there are no reading processes))}, \text{ by induction.}

(iii) \( (P_1, \ldots, P_k \text{ are all the reading processes}) \text{ implies eventually (} P_j \text{ executes signal( oktowrite ))} \text{ and then writing = true}, \text{ using immediate resumption and nonempty( oktowrite ) = true.}

This reduces to the previous case for which we have already shown liveness.
5.6 THE SIMULATION OF MONITORS BY SEMAPHORES

We now give an algorithm for transforming a program using monitors into a program that uses semaphores. This will show that monitors are no more powerful than semaphores and hence that the decision to use monitors can be made solely on the basis of their contribution to the clarity and reliability of the resulting system. This transformation is concerned only with the dynamic behavior of the concurrent system. The static protection of monitor variables should still be implemented, if possible, by a facility such as the Simula 67 class or the Ada package.

The mutual exclusion of the monitor procedures is easily simulated by a binary semaphore. There will be a semaphore \( s \) (initially 1) for each different monitor and each procedure of a monitor will commence with \( \text{wait}(s) \) and terminate with \( \text{signal}(s) \) just as we solved the critical section problem with semaphores. For each condition \( \text{cond} \) we need an integer variable \( \text{condcount} \) to count the number of waiting processes and a binary semaphore \( \text{condsem} \) to actually block the waiting processes. The initial value of \( \text{condcount} \) is 0. That of \( \text{condsem} \) is also 0 because a process executing the monitor \( \text{wait} \) always blocks. Each command \( \text{wait(} \text{cond} \text{)} \) of the monitor is now coded:

\[
\text{condcount} := \text{condcount} + 1; \\
\text{signal}(s); \\
\text{wait(} \text{condsem} \text{)}; \\
\text{condcount} := \text{condcount} - 1;
\]

The \( \text{signal} \) on the semaphore \( s \) is to release the mutual exclusion on the entry to the monitor in order to allow other processes to enter, including (hopefully) one which will eventually signal.

Remember that we have restricted the \( \text{signal(} \text{cond} \text{)} \) to be the last command of a procedure. Hence the release of a blocked process from the semaphore \( \text{condsem} \) can be combined with the release of the mutual exclusion in the following code:

\[
\text{if condcount} > 0 \text{ then signal (condsem) else signal(s)}
\]

This implements our restriction that, if there are processes waiting on a condition, they have priority over processes waiting at the monitor entry points. The blocked processes are waiting on \( \text{condsem} \); the processes wishing to enter are waiting on \( s \). So only if there are no blocked processes (\( \text{condcount}=0 \)) is the monitor entry freed. Note that the signalling process must have passed a \( \text{wait}(s) \) semaphore upon entry. Thus the awakened process inherits the outstanding mutual exclusion from the signalling process. The debt is made good when the awakened process terminates and executes \( \text{signal(s)} \). Of course it could avoid this by awakening still another process.
It is interesting that, according to our definition of semaphores, the value of the semaphore-condsem is never 1. It is initially 0 and signal(condsem) is only executed if some process is waiting on condsem. Thus condsem is never incremented.

The only feature of the monitor that we cannot implement is the FIFO assumption on the queue because the semaphores are not FIFO.

In Fig. 5.4, we show how this translation can be carried out for the producer-consumer program in Fig. 5.1.

```plaintext
program producerconsumer;
const sizeofbuffer = . . . ,
var b: array[0 . . sizeofbuffer] of integer;
in, out: integer;
n: integer;
s: (* binary *) semaphore; (* for mutual exclusion *)
notemptysem, notfullsem: (* binary *) semaphore;
notemptycount, notfullcount: integer;
procedure append (v: integer);
begin
    wait(s);
    if n = sizeofbuffer + 1 then
        begin
            notemptycount := notemptycount + 1;
signal(s);
            wait(notemptysem);
            notemptycount := notemptycount - 1
        end;

        if notfullcount > 0 then signal(notfullsem)
            else signal(s)
    end;
procedure take(var v: integer);
begin
    wait(s);
    if n = 0 then
        begin
            notfullcount := notfullcount + 1;
signal(s)
            wait(notfullsem);
            notfullcount := notfullcount - 1;
        end;

        if notemptycount > 0 then signal(notemptysem)
            else signal(s)
    end;
```
procedure producer;

procedure consumer;

begin (* main program *)
in := 0; out := 0; n := 0;
s := 1;
notemptycount := 0; notfullcount := 0;
notemptysem := 0; notfullsem := 0;
cobegin
    producer; consumer
coend
end.

Fig. 5.4.

5.7 UNRESTRICTED SIGNALS

If we allow signal(c) to appear anywhere in a monitor procedure then we face the following dilemma. A primary advantage of the monitor is the immediate resumption of a signalled process while the condition is guaranteed. This saves needless looping and re-testing that is characteristic of semaphore algorithms. Thus we cannot let a signalling process continue after the signal because it might change the condition or execute another signal causing a third process to be immediately resumed.

On the other hand, the signalling process is not waiting for anything so it seems a pity to block it. Nevertheless, immediate resumption is so central to monitor programming that we retain it and instead block the signalling process. However, the signalling process is kept close at hand so that when the awakened process releases the monitor (by exiting or executing another wait) it has priority over other processes wishing to enter. Of course, nothing prevents the awakened process itself from signalling and thus joining the previous signaller.

In the igloo model (see Fig. 5.5), the igloo has only room for one process at a time. It has deep freezers in the basement for processes to wait on conditions. We add a closet with a spring loaded door.

Entering and exiting the igloo is on the basis of mutual exclusion—one at a time. If a process waits then it enters the freezer for the appropriate condition. If a process signals, it invites a frozen process to enter the igloo. The signalling process itself enters the closet so as not to interfere with the privacy of the awakened process. When the igloo is cleared, either because the process has exited or entered another freezer, the spring-loaded door flies open, thrusting the signaller into the igloo before a new process can enter. If awakened processes signal, they will be stacked in the closet on top
of the previous processes.

We can now appreciate the simplification obtained by restricting the signal to being the last statement in a procedure. In the more general model, the signaller would emerge from the closet only to exit immediately. The signaller might just as well exit immediately after the signal and we need not build the closet into the igloo.

The simulation of the unrestricted monitor by semaphores is more complicated (Fig. 5.6). We need a new variable urgent and a new semaphore usem to count and block the signallers. In the simulation of wait(cond) and exit, the release of the monitor now checks urgent to see if there are waiting signallers. urgent > 0 will signify that there is some waiting signaller that is demanding to be released (by signal(usem)) before any new processes can be allowed to enter (by signal(s)).

In the simulation of signal(cond), condcount > 0 signifies that there is in fact a process waiting for this condition. The process is awakened (by signal(condsem)) and then the signaller suspends itself (by wait(usem)).

entry: wait(s);
wait(cond): condcount := condcount+1;
    if urgent > 0
        then signal(usem)
        (* if waiting signallers *)
        else signal(s);
        (* free a signaller *)
    wait(condsem);
    (* let a new process in *)
    condcount := condcount−1;
signal(cond) : urgent := urgent+1;
    if condcount > 0 then
        begin
            signal(condsem);
            wait(usem)
        end;
        urgent := urgent−1;
    exit : if urgent > 0
        then signal(usem)
        else signal(s);

Fig. 5.6.

5.8 EXERCISES

5.1 Suppose that signals are not restricted but that some particular signal is in fact the last statement in its procedure. Code a simplification to simulation of monitors by semaphores for this case.

5.2 Show that even if the implementation of the semaphore is FIFO, the simulation of the monitor by semaphores is not.

5.3 Translate the monitor solution to the problem of the readers and the writers (Fig. 5.3) to a semaphore solution.

5.4 (Courtois et al.) Fig. 5.7 is a solution to the problem of the readers and the writers using semaphores. It is easy to see that r counts the number of readers, s guarantees mutual exclusion to variable r and wsem guarantees mutual exclusion to writing.

(a) Discuss the priority scheme of this solution.
(b) Suppose that you have a FIFO implementation of semaphores. How would that affect the answer?

program readersandwriters;
var r: integer;
    s, wsem: (* binary *) semaphore;
procedure readprocess;
begine
repeat
    wait(s);
    r := r+1; if r=1 then wait(wsem);
    signal(s);
    readthedata;
    wait(s);
    r := r−1; if r=0 then signal(wsem);
    signal(s)
forever
end;
procedure writeprocess;
begin
repeat
    wait(wsem);
    writethedata;
    signal(wsem)
forever
end;

begin (* main program *)
    r := 0;
    s := 1;
    wsem := 1;
cobegin
    readprocess; (* . . . *)
    writeprocess; (* . . . *)
coend
end.

Fig. 5.7.

5.5 (Courtois et al.) The solution in Fig. 5.8 uses a somewhat symmetrical code for both the readers and the writers except that in the writer, wsem is used to guarantee mutual exclusion in the execution of the write itself while, in the reader, rsem is used only by the writer to prevent readers from entering the critical section bracketed by s1.

(a) Discuss the priority scheme of this solution.
(b) How would the solution change if the semaphores were FIFO?
(c) What would happen if s3 were omitted? (Hint Show that s3 ensures that rsem = 0 implies that there is exactly one process waiting for signal(rsem)).

program readersandwriters;
var r,w: integer;
    s1, s2, s3: (* binary *) semaphore;
    wsem, rsem: (* binary *) semaphore;
procedure readprocess;
begin
repeat
    wait(s3);
    wait(rsem);
    wait(s1);
    r := r + 1;
    if r = 1 then wait(wsem);
    signal(s1);
    signal(rsem);
    signal(s3);
    readthedata;
    wait(s1);
    r := r - 1;
    if r = 0 then signal(wsem);
    signal(s1)
forever
end;
procedure writeprocess;
begin
repeat
    wait(s_2);
    \text{if } w=1 \text{ then } wait(rsem);
    signal(s_2);
    wait(wsem);
    writethedata;
    signal(wsem);
    wait(s_2);
    \text{if } w=0 \text{ then } signal(rsem);
    signal(s_2)
forever
end;
begin (* main program *)
    r := 0; w := 0;
    s_1 := 1; s_2 := 1; s_3 := 1;
    rsem := 1; wsem := 1;
cobegin
    readprocess; (* . . . *)
    writeprocess; (* . . . *)
coend
end.

Fig. 5.8.

5.6 For each of the priority schemes (Section 5.4 and Exercises 5.4 and 5.5) try to think of an application in which that scheme is the reasonable one to require.

5.7 Complete the semi-formal proof of the solution to the problem of the readers and the writers.

(a) Prove the invariants (a)-(d).
(b) Prove the liveness of writing.
(c) Prove the following statement $S$ which expresses the priority scheme claimed for the solution.

$S$: If $Q$ enters \textit{startwrite} before $P$ enters \textit{startread} then $(Q$ writes before $P$ reads).

Hint: How to prove precedences:
Let $p$ and $q$ be any two properties of programs. Then $(p \text{ before } q)$ is equivalent to $(p \text{ is now true})$ or $(q \text{ is now false and after executing a step of the program then } p \text{ before } q)$. Similarly, the negation of $(p \text{ before } q)$ is equivalent to $(p \text{ is now false})$ and $(q \text{ is now true or after a step then } p \text{ before } q)$ is false.

Show that the negation of $S$ is inductive, that is, if $S$ is assumed false then after executing a step of the program $S$ must still be false. Deduce that $(Q$ enters \textit{startwrite}) but never $(Q$ writes) thus contradicting the liveness of writing shown in (b).
6

THE ADA RENDEZVOUS

6.1 INTRODUCTION

The semaphore and the monitor are centralized facilities. A process executing a monitor procedure has access to the single copy of the monitor variables and thus there must be an arbiter to enforce mutual exclusion. While these requirements are natural in a single computer (or any common memory system), they are difficult to implement in a distributed system. By a distributed system we mean a set of totally independent computers whose only connection is by sending and receiving messages. There may be no synchronization between sending and receiving a message. Messages may "pass" each other in transit. What we need is some sort of self-enforcing protocol. A process will decide to wait on its own initiative as in the busy wait algorithms of Chapter 3.

In those algorithms, each process agrees to enter a while loop if it needs to block itself. Each process decides by itself when to leave. This contrasts with the semaphore and the monitor signals which are required to wake another process.

Lamport's bakery algorithms discussed in the exercises of Chapter 3 are designed for distributed systems. Each process writes only into a single local variable. The test \( n_1 > n_2 \) in process \( P_1 \) can be interpreted as follows. Send a request to process \( P_2 \) to read the value of \( n_2 \). Wait until \( P_2 \) replies. Compare the received value with the current value of the local variable \( n_1 \).

Each process needs to be augmented with polling statements that periodically search for requests for data values from other processes. Alternatively this can be done by interrupts. The receipt of a message from the communication line will trigger an interrupt in the receiving process. This process will then identify the message and route it for appropriate action. If we examine the protocol suggested in the last paragraph we find that the essential idea is the transfer of information at a predetermined point in each process. We call this a rendezvous of the two processes. The essence of
any rendezvous is that the party which arrives earlier is required to wait. The alternative to a rendezvous is a buffered message system but aside from questions as to the size and number of buffers, we now have the question of who owns the buffers.

In classical systems the buffers belong to the "system", but in a distributed system, we do not want to single out any process as the boss. If that is what we want then the monitor formalism is sufficient. Since message passing systems are an obvious task for concurrent programming, we prefer to base the programs on an independent primitive such as a rendezvous.

The rendezvous was suggested by Hoare in a paper which is entitled "Communicating sequential processes" to contrast with Dijkstra's "Co-operating sequential processes" on which Chapters 3 and 4 are based. Instead of presenting Hoare's original work we choose to discuss the version that is used in the Ada programming language. Ada was designed specifically for real-time systems programming which inherently uses concurrency. The Ada facilities will probably become the dominant style for concurrent programming.

The examples will be written as executable Ada programs. However, we will try to use only Pascal-like features when possible and we will note the essential differences where necessary. This chapter is not a tutorial on Ada nor even on the full range of concurrent programming facilities in Ada. It is intended as an introduction to the rendezvous concept as used in Ada. Ada programmers can regard the previous chapters as a description of the scientific climate under which the Ada concurrent programming primitives were developed.

6.2 THE "ACCEPT" STATEMENT

The monitor has no life of its own. It is simply a collection of data and procedures that sit waiting to be invoked. In our model, the monitor is an igloo which is accessible to all processes that need it but which is just a building that does nothing on its own. Let us now imagine a story that will give us a feel for the rendezvous.

Several processes, \( P_i \), are riding around in the snow on their dog sleds (Fig. 6.1). Process \( Q \) owns a lodge "Ada's Place" which happens to be strategically placed at an intersection of all the tracks followed by the \( P_i \). Periodically, the \( P_i \) reach the lodge and wish to enter for a snack. If \( P_i \) arrives before \( Q \) has arrived to open the lodge then \( P_i \) crawls into his sleeping bag to wait for \( Q \). When \( Q \) arrives they open the lodge, go inside and \( P_i \) exchanges the fresh meat he has bagged for ready-to-eat meat sandwiches that \( Q \) prepares.

Unfortunately, \( Q \)'s investment capital was too small and the lodge can only hold two processes and one load of meat and bread. Thus, if several
processes arrive at the same time or if several processes arrive when a transaction is in progress, then only one process $P_1$ can be in the lodge with $Q$. The others must wait until $P_1$ leaves the lodge to resume his hunt and $Q$ leaves the lodge to ride his sled to the Bakery to replenish his supply of bread. When $Q$ returns he can complete a similar transaction with the other processes.

Suppose now that a sudden blizzard has delayed the arrival of the $P_i$. Then $Q$ must wait. Since it seems pointless to waste energy by heating the lodge when there are no customers, the lodge stays locked and $Q$ keeps warm in a sleeping bag outside.

The essential features to be abstracted from this story are:

(i) the symmetrical waiting of the rendezvous—whichever arrives first is required to wait;
(ii) the completion of a single transaction during the rendezvous;
(iii) the mutual exclusion of the transaction conducted in the confines of the lodge; and
(iv) the two-way exchange of information that is the method of communication between the processes in the rendezvous. Let us now examine the Ada program for this story (Fig. 6.2).

The accept statement has the syntax of a local procedure (without local data declarations) which can appear embedded within executable statements. The call to the accept statement is syntactically identical to a procedure call. This is done intentionally so that an operation can be implemented
as a sequential procedure or a concurrent program without informing the user. However, unlike a monitor procedure, the accept statement belongs to process Q. Q must accept something in order to continue execution. As described in the story, if some P_i executes a call before Q executes the accept then P_i is blocked pending the rendezvous. Conversely, if Q executes the accept and there are no waiting processes P_i then Q is blocked pending the rendezvous. Once Q and some P_i have executed the pair accept lodge and lodge then we say that the rendezvous has occurred.

procedure Adalodge is  
  numberofprocesses: constant := . . . ;
  task type process;
  task Q is  
    entry lodge(meat: in food; sandwiches: out food);
    end Q;
  task body process is  
    walrus, victuals: food;
  begin  
    loop  
      walrus := huntwalrus;
      lodge(walrus, victuals);
      eat(victuals);
    end loop;
  end process;
  task body Q is  
    bread: food;
  begin  
    loop  
      bread := visitbakery;
      accept lodge(meat: in food; sandwiches: out food) do
        cook(meat);
        sandwiches := meat + bread;
      end lodge;
    end loop;
  end Q;
end Adalodge;

P: array(1 . . numberofprocesses) of process;
begin
  null;
end Adalodge;

Fig. 6.2.

Remark To run this program, you will have to supply the value of numberofprocesses; a representation for food; subprograms for huntwalrus,
eat, visitbakery, cook, and finally, the loop should be terminating and some trace should be printed. (End of remark.)

The rendezvous is considered to be in force during the execution of the statements between the do of the accept statement and the corresponding end. In particular, the calling process is blocked for the duration of the rendezvous to prevent it from changing the values of the parameters until the exchange of information is complete. Thus the body of the accept acts like a critical section. Once the accept statement has terminated, the rendezvous has been completed and a fresh accept statement must be issued—during the next cycle of the loop—to effect another rendezvous (with the same process or with another). Of the two parameters, one is used to pass a value from the calling process and the other to return a value to the calling process. This is the two-way exchange of information between the processes.

That the rendezvous is suitable for distributed systems can be seen by the following sketch of how it might be implemented. \( P_i \) executes lodge by sending a signal to \( Q \) that it requests a rendezvous. \( P_i \) then suspends itself pending a reply from \( Q \). The processor running \( Q \) registers the signal from \( P_i \) by an interrupt or by polling. \( Q \) eventually executes the accept statement and notes that \( P_i \) has registered a signal. \( Q \) replies to \( P_i \) that rendezvous has occurred and remains blocked until \( P_i \) acknowledges the reply with a message containing the parameters of the call. \( Q \) receives the parameters, executes the statements following the do and then returns the result parameters. Upon receiving the results, \( P_i \) can unblock and continue computation. The program can even be implemented in a distributed manner because once the number and type of the parameters are agreed upon, the processes can be independently designed and programmed.

Let us now see how the binary semaphore can be simulated by a rendezvous (Fig. 6.3). Here it is important to note that while the mutual exclusion problem for two processes was solved by invoking passive semaphore procedures, with the rendezvous we need to create a new semaphore process to mediate between \( P_1 \) and \( P_2 \). On the other hand, \( P_1 \) and \( P_2 \) no longer need to access the same variable or queue.

```plaintext
procedure mutualexclusion is
task semaphore is
  entry wait;
  entry signal;
end semaphore;
task body semaphore is
begin
  loop
    accept wait;
    accept signal;
  end loop;
end semaphore;
```
task $P_1$;
task body $P_1$ is
begin
  loop
    rem1;
    wait;
    crit1;
    signal;
  end loop;
end $P_1$;

(task $P_2$;
task body $P_2$ is
begin
  loop
    rem2;
    wait;
    crit2;
    signal;
  end loop;
end $P_2$;
begin
  null;
end mutual exclusion;  \hfill Fig. 6.3.

When a process $P_1$ executes the call to \textit{wait}, it must block until the
semaphore process executes its \texttt{accept} statement and the rendezvous is
achieved. There are no parameters to be passed and no statements to be
executed within the critical section of the \texttt{accept} statement. Once $P_1$ has
terminated the rendezvous, it is free to enter its critical section.

$P_2$ however will block when it tries to call \textit{wait} because the semaphore
process is waiting for a rendezvous with a \texttt{signal} call. Thus until some process
(i.e. $P_1$) executes a call to \texttt{signal}, the semaphore process is blocked and hence
so is $P_2$. When $P_1$ completes its critical section, it accomplishes a rendezvous
with the semaphore process at \texttt{accept signal}. Then the semaphore process
can commence its next cycle and accomplish a rendezvous with $P_2$.

Since the queues for the \texttt{accept} statements are required to be
implemented as FIFO queues, this implements a FIFO semaphore: even if
$P_1$ overtakes $P_2$ after completing the critical section, it will be placed after $P_2$
on the queue of the same \texttt{accept wait} statement. Note that the queues are
FIFO in terms of time of arrival at the processor executing the \texttt{accept}
statement. Thus, in a physically distributed system, closer processes may be
able to overtake more remote ones. Lockout is not a problem, however,
because once a process does enter the queue, it need only wait for the finite number of processes ahead of it to complete.

We have shown how to implement a single semaphore. If the system is
to have several semaphores we will need multiple copies of the semaphore
process so that calls to wait and signal can be parameterized to indicate which
semaphore process to call. In Ada a task type can be defined and multiple
instances created by ordinary variable declarations. Thus an array of
semaphore tasks can be declared and accessed by a simple array index.

**Ada language notes**

1. Ada uses a "main" **procedure** where Pascal uses **program**.
2. The token **var** is not used before variable declarations.
3. **loop . . . end loop** is our **repeat . . . forever**.
4. Processes are called **tasks**. A **task** must have a specification part which
declares the **entries**: the name of the rendezvous, if any. The **body** is
declared separately and contains the data and code local to the **task**.
5. An **in** parameter is read-only. For simple parameters this can be
implemented by call-by-value: the actual parameter is evaluated and a
copy of the value is passed to the procedure, or in this case the body of
the **accept** statement. An **out** parameter is write-only. It can be used to
copy a value from the procedure to a variable in the calling program.
6. To declare several identical tasks, we declare a **task type**. Then multiple
instances may be declared in an **array**, as we have done.
7. The declaration of a task automatically initiates it. Thus the main
program body is **null**. No **cobegin . . . coend** is necessary, since the token
**task** calls for concurrent execution.

### 6.3 THE "SELECT" STATEMENT

Turning to the bounded buffer problem, we find that the **accept** statement
is insufficient. We might attempt a solution with the program fragments of
Fig. 6.4, using a buffer process between the producer and the consumer.

**Producer:**

```
    loop
        append(v);
    end loop;
```

**Consumer:**

```
    loop
        take(v);
    end loop;
```
Buffer:
\[
\begin{align*}
&\text{loop} \\
&\qquad \text{accept append}(v: \text{ in integer}); \\
&\qquad \text{accept take}(v: \text{ out integer}); \\
&\qquad \text{end loop}; \\
\end{align*}
\]  
Fig. 6.4.

The only execution sequence possible is append, take, append, take. This is the same as no buffer at all and we could just as well make the rendezvous directly between the producer and the consumer.

Producer:
\[
\text{loop append}(v); \text{ end loop;}
\]

Consumer:
\[
\text{loop} \\
\qquad \text{accept append}(v: \text{ in integer}); \\
\qquad \text{end loop;}
\]

If you examine the bounded buffer solutions by semaphores and monitors you find that what is needed is some way of conditionally achieving a rendezvous. If the buffer is full, the rendezvous must only be with the consumer; if empty, only with the producer. If the buffer is neither full nor empty then the rendezvous can be with whichever of the processes is currently waiting for the rendezvous. If both are waiting then we do not really care with whom the rendezvous is made as long as the buffer process is not unfair. With this background it should be possible to follow the Ada solution to the bounded buffer (Fig. 6.5). The program shows just the buffer task; the producer and consumer are straightforward loops.

\[
\text{task boundedbuffer is} \\
\quad \text{entry append}(v: \text{ in integer}); \\
\quad \text{entry take}(v: \text{ out integer}); \\
\quad \text{end boundedbuffer;}
\]

\[
\text{task body boundedbuffer is} \\
\quad \text{size: constant := \ldots ;} \\
\quad b: \text{array(0 .. size) of integer;} \\
\quad \text{inptr, outptr: integer;} \\
\quad n: \text{ integer;} \\
\quad \text{begin} \\
\quad \quad n := 0; \text{ inptr := 0; outptr := 0;} \\
\quad \quad \text{loop} \\
\quad \quad \text{select} \\
\quad \quad \quad \text{when } n <= \text{ size } => \\
\quad \quad \quad \quad \text{accept append}(v: \text{ in integer}) \text{ do} \\
\quad \quad \quad \quad \quad b(\text{inptr}) := v; \\
\quad \quad \quad \quad \quad \text{end append;} \\
\quad \quad \quad n := n+1; \\
\quad \quad \quad \text{inptr := (inptr+1) mod size;}
\]

or
    when \( n > 0 \) =>
    accept take(v: out integer) do
        v := b(outptr);
        end take;
    end select;
    n := n - 1;
    outptr := (outptr + 1) \mod size;
end boundedbuffer;

Before we discuss the new features of the select command, note that the critical section of the accept command does not encompass the entire buffer processing but only the physical exchange of data. The updating of the internal pointers need not block the producer nor the consumer who have no access to these local variables.

The select statement allows one to select between several alternatives separated by or. The alternatives are prefixed by when-clauses called guards. The guards are boolean expressions which establish what conditions must be true for an alternative to be a candidate for execution.

The execution of a select statement begins by evaluating all the guards. Then one of the open alternatives—alternatives with true guards—is selected for execution. In the bounded buffer if one of the guards is not true then the other must be \( n <= 0 \) implies \( n <= \text{size} \) and conversely, \( n > \text{size} \) implies \( n > 0 \) so there is always an open alternative. If the buffer is empty, only the first alternative can be selected. This is the alternative that receives data from the producer. Similarly if the buffer is full, only the second alternative is open to allow the consumer to remove data from the buffer. In either case, of course, the buffer process will block waiting for the relevant rendezvous. Nothing is lost by not rechecking a closed alternative since the only way to empty a full buffer is by consuming.

The difference between the select statement and an if statement is seen in the case that both guards are open. Then if both the consumer and the producer are waiting for a rendezvous, we don't care which rendezvous is accomplished. An if statement must specify which statement is to be executed in this case.

But the select statement is even smarter than that. Suppose that the buffer is neither empty nor full, but that only the consumer is waiting for a rendezvous. If a choice is made between both open alternatives then we could blunder into blocking on an accept append statement for which no producer process is waiting. Thus if both alternatives are open but only one accept statement has a process blocked on it waiting for a rendezvous, the select will choose to execute the alternative that leads to an immediate rendezvous.

There is another possibility, namely that both alternatives are open but
that neither process is ready. Rather than endlessly checking the guards (whose truth will not change) or arbitrarily blocking on one of the accept statements, the select statement will block simultaneously on both accept statements and execute the first rendezvous to be accomplished.

This is the essence of the "guarded commands" style of programming: avoid over-specification (as in an if statement) by allowing the computer as much freedom of choice as possible consistent with the correctness requirements of the program.

We now give a more formal description of the general select statement.

```
select
  when condition1 => accept entry1 do statements end;
  other statements
or
  when condition2 => accept entry2 do statements end;
  other statements
...
else statements
end select;
```

Remark 1 The else clause is optional (see below).

Remark 2 A guard may be identically true in which case the when true => can be omitted.

Semantics of the select statement:
1. Evaluate all the guards to determine which alternatives are open.
2. If there are open alternatives, determine which accept statements in open alternatives have processes currently waiting for rendezvous.
3. If there are such processes, execute one of these alternatives. If there are several open alternatives with processes waiting for rendezvous, the selection among them is done arbitrarily.
4. If there are no open alternatives or no waiting processes, execute the else clause if there is one.
5. If there are no waiting processes and no else clause, wait for the first process to attempt a rendezvous with an accept clause in one of the open alternatives.
6. In the absence of an else clause, it is an error for there to be no open alternative.

We can demonstrate the general select statement by assuming in our story that the owner of "Ada's Place" has independent suppliers of both bread and meat and that his only task is to make sandwiches. Then if there are no processes waiting at the lodge, he can profitably use the time to prepare sandwiches (Fig. 6.6).

The guards are exhaustive (at all times at least one is true) and disjoint (no two are ever simultaneously true) so exactly one is open. The else clause
is used to do some useful work if the second accept statement is open but
does not have a process waiting for the rendezvous. If the $P_i$ are fast eaters,
they will have to wait but if they are often held up in blizzards, they can count
on fast service when they do return to the lodge.

procedure Adalodge is
  task type process;
  task hunter;
  task bakery;
  task $Q$ is
    entry delivermeat(mt: in food);
    entry deliverbread(br: in food);
    entry lodge(snack: out food);
  end $Q$;

  task body process is
    victuals: food;
  begin
    loop
      explore;
      lodge(victuals);
      eat(victuals);
    end loop;
  end process;

  task body hunter is
    walrus: food;
  begin
    loop
      hunt(walrus);
      delivermeat(walrus);
    end loop;
  end hunter;

  task body bakery is
    rolls: food;
  begin
    loop
      bake(rolls);
      deliverbread(rolls);
    end loop;
  end bakery;

  task body $Q$ is
    bread, meat, sandwiches: food;
procedure makesandwiches is
begin
    cook(meat);
    sandwiches := bread + meat;
    bread := 0;
    meat := 0;
end makesandwiches;
begin
    bread := 0;
    meat := 0;
    sandwiches := 0;
loop
    select
    when bread = 0 =>
        accept deliverbread(br: in food) do
            bread := br
        end deliverbread;
    or
    when meat = 0 =>
        accept delivermeat(mt: in food) do
            meat := mt;
        end delivermeat;
    or
    when ((bread <> 0) and (meat <> 0)) or
    (sandwiches <> 0) =>
        accept lodge(snack: out food) do
            if sandwiches=0 then
                makesandwiches; end if;
            snack := sandwiches;
            sandwiches := 0;
        end lodge;
        else
            if (bread <> 0) and (meat <> 0)
            and (sandwiches=0)
            then makesandwiches; end if;
        end select;
    end loop;
end Q;

P: array(1 .. numberofprocesses) of process;
begin
    null;
end Adalodge;

Fig. 6.6.
6.4 PROVING PROPERTIES OF THE RENDEZVOUS

The development of a satisfactory proof theory for synchronization by communication is an area of current research. The concepts of invariants and eventuality propositions that have been so successful in proving synchronization by cooperation may need modification when applied to the rendezvous.

An important goal is to try to make the proofs distributed: the proof of one process ought not to require knowledge of the internal details of another process. It ought to be possible to construct communicating proofs: "If you promise to send me a message $M_1$ (I do not care how or why you do so) then I promise to send you a message $M_2$.”

Let us look at the bounded buffer task of Fig. 6.5. First note that, since the guards are exhaustive, there is no deadlock. Since the execution of one alternative makes true the guard of the other alternative, there is no lockout if we assume fair selection among open alternatives. Another way of showing eventuality is to note that if the producer produces indefinitely without the consumer consuming, the buffer must fill and the producer’s guard is falsified. The proof of liveness can thus be done by reasoning internal to the buffer task.

The safety property is that the elements must be consumed in the same order that they are produced. The internal behavior of the buffer task is very simple; what must be shown is that a value that is produced must become the newest element of the buffer and that the oldest element of the buffer is that which is consumed.

Suppose that the producer executes \textit{append(\nu)}. Upon achieving the rendezvous, we can conclude that the value of the actual parameter has been communicated to the formal parameter \nu of the \textbf{accept} statement. Upon completion of the rendezvous (completion of the \textbf{accept} statement), this value has been transferred to \textit{b[inptr]} and has become the newest element of the buffer.

The general rule is the transfer of information at the point of the rendezvous. For an \textbf{in} parameter \nu, whatever was true of \nu in the calling process before the rendezvous is true within the \textbf{accept} statement upon achieving rendezvous. For an \textbf{out} parameter (such as the \nu in \textit{take}), whatever is true of \nu upon completion of the \textbf{accept} statement (such as that \nu is the oldest buffer element) is true of the actual parameter in the calling task.

6.5 EXERCISES

6.1 Solve Conway’s problem in Ada.

6.2 Write programs for the reader–writer algorithms we have given.

6.3 Simulate a general semaphore in Ada.

6.4 Simulate a rendezvous by semaphores or monitors.
6.5 In Fig. 6.7 are two possibilities for a monitor-like \textit{wait/signal} facility. Specify the behavior of these solutions. Which is more like a monitor?

6.6 Discuss the priority scheme of the solutions to the problem of the readers and the writers shown in Fig. 6.8 and compare them with the solutions in Chapter 5.

6.7 Prove the correctness of the programs in Figs. 6.2 and 6.6.

6.8 (Dijkstra) Write a program for partition by communication. Two disjoint sets of numbers \( S \) and \( T \) are given. If \( s \) and \( t \) are the number of elements of \( S \) and \( T \), respectively, then upon completion of the program, \( S \) should contain the \( s \) smallest numbers in \( S \cup T \) and \( T \) should contain the \( t \) largest numbers in \( S \cup T \). A solution using two processes is outlined in Fig. 6.9. Prove its correctness. \textit{Note} The termination of the task \textit{upper} is not specified. If you program this solution in Ada, either learn about the \texttt{terminate} option in Ada or introduce explicit signals for termination.

```ada
    task monitorfacility1 is
        entry wait;
        entry signal;
    end monitorfacility1;
    task body monitorfacility1 is
        received: boolean;
    begin
        received := false;
        loop
            select
                accept signal;
                received := true;
            or
                when received =>
                    accept wait;
                    received := false;
            end select;
        end loop;
    end monitorfacility1;

    task monitorfacility2 is
        entry wait;
        entry signal;
    end monitorfacility2;
    task body monitorfacility2 is
    begin
        loop
            accept signal;
            select
                accept wait;
            else null;
            end select;
        end loop;
    end monitorfacility2;
```

Fig. 6.7.
task readersandwriters1 is
  entry startread;
  entry endread;
  entry startwrite;
  entry endwrite;
end readersandwriters1;
task body readersandwriters1; is
  readers: integer;
begin
  readers := 0;
  loop
    select
    accept startread,
    readers := readers + 1;
    or
    accept endread;
    readers := readers - 1;
    or
    when readers = 0 =>
    accept startwrite;
    accept endwrite;
end select;
end loop;
end readersandwriters1;

task readersandwriters2 is
  entry startread;
  entry endread;
  entry startwrite;
  entry endwrite;
end readersandwriter2;
task body readersandwriter2 is
  readers: integer;
begin
  readers := 0;
  loop
    select
    when startwrite'count = 0 =>
    accept startread;
    readers := readers + 1;
    or
    accept endread;
    readers := readers - 1;
    or
    when readers = 0 =>
    accept startwrite;
    accept endwrite;
    loop
      select
      accept startread;
      readers := readers + 1;
    else goto l;
    end select;
end loop;
end readersandwriter2;
end loop;
elsif (l) then select;
end loop;
end readersandwriters2;

\[\text{Fig. 6.8.}\]

**Ada Language Notes**

1. `startwrite'count` is a predefined function (called an attribute in Ada) that returns the number of tasks currently waiting to rendezvous with the `entry startwrite`.
2. `{l}` is a statement label that is the target of the corresponding `goto`.

```ada
task lower is
  entry sendmax(xx: in integer);
end lower;
task upper is
  entry sendmin(yy: in integer);
end upper;

task body lower is
  x, mx: integer;
begin
  mx := the maximum value in s;
  loop
    sendmax(mx);
    remove mx from S;
    accept sendmin(xx: in integer) do
      x := xx;
    end sendmin;
    add x to S;
    mx := the maximum value in S;
    exit when x = mx;
  end loop;
end lower;

task body upper is
  mn: integer;
begin
  loop
    accept sendmax(yy: in integer) do
      add yy to T;
    end sendmax;
    mn := the minimum value in T;
    sendmin(mn);
    remove mn from T;
  end loop;
end upper;
```

\[\text{Fig. 6.9.}\]
7 THE DINING PHILOSOPHERS

7.1 INTRODUCTION

The problem of the dining philosophers (posed by Dijkstra) is of great importance in concurrent programming research. The problem allows all of the pitfalls of concurrent programming to be demonstrated in a vividly graphical situation. It is a challenge to proposers of new primitives for concurrent programming. As a test of your understanding of concurrent programming principles we present several solutions using the various primitives we have learned.

The problem is set in a monastery whose five monks are dedicated philosophers. Each philosopher would be happy to engage only in thinking were it not occasionally necessary to eat. Thus the life of a philosopher is an endless cycle: **repeat think; eat forever**.

![Diagram of the Dining Philosophers](image_url)  

*Fig. 7.1.*
The communal dining arrangement is shown in Fig. 7.1. In the center of the table is a bowl of spaghetti that is endlessly replenished; there are five plates and five forks. A philosopher wishing to eat enters the dining room, takes a seat, eats and then returns to his cell to think. However, the spaghetti is so hopelessly entangled that two forks are needed simultaneously in order to eat. (It has been pointed out that this requirement is rather forced and that it would be more natural to set the problem in the Orient with a bowl of rice and chopsticks.)

The problem is to devise a ritual (protocol) that will allow the philosophers to eat. Each philosopher may use only the two forks adjacent to his plate. The protocol must satisfy the usual requirements: mutual exclusion (no two philosophers try to use the same fork simultaneously) and freedom from deadlock and lockout (absence of starvation—literally!) An additional safety property is that if a philosopher is eating then he actually has two forks.

7.2 FIRST ATTEMPT

program diningphilosophers;
var fork: array [0 .. 4] of (* binary *) semaphore;
i: integer;
procedure philosopher(i: integer);
begin
repeat
    think;
    wait(fork[i]);
    wait(fork[(i+1) mod 5]);
    eat;
    signal(fork[i]);
    signal(fork[(i+1) mod 5])
forever
end;
begin (* main program *)
    for i := 0 to 4 do fork[i] := 1;
cobegin
    philosopher(0);
    philosopher(1);
    philosopher(2);
    philosopher(3);
    philosopher(4)
coend
end.

Fig. 7.2.
The idea of the program in Fig. 7.2 is very simple. The binary semaphores ensure mutual exclusion in accessing the forks. The safety property is satisfied because eating is done only after two fork-semaphores have been successfully completed.

Unfortunately the solution deadlocks. Under perfect synchronization if the philosophers enter the protocol simultaneously and take the left forks then the state of the program is that all forks are 0 and all the philosophers are trying to complete \textit{wait(fork[i+1])}. Since there is no process that can \textit{signal}, the program is deadlocked.

### 7.3 SECOND ATTEMPT

```
program diningphilosophers;
monitor forkmonitor;
var fork: array[0..4] of integer;
oktoeat: array[0..4] of condition;
i: integer;
procedure takefork(i: integer);
begin
  if fork[i] <> 2 then wait(oktoeat[i]);
  fork[(i+1) mod 5] := fork[(i+1) mod 5]−1;
  fork[(i−1) mod 5] := fork[(i−1) mod 5]−1
end;
procedure releasefork(i: integer);
begin
  fork[(i+1) mod 5] := fork[(i+1) mod 5]+1;
  fork[(i−1) mod 5] := fork[(i−1) mod 5]+1;
  if fork[(i+1) mod 5]=2 then signal(oktoeat[(i+1) mod 5]);
  if fork[(i−1) mod 5]=2 then signal(oktoeat[(i−1) mod 5])
end;
begin (* monitor *)
  for i := 0 to 4 do fork[i] := 2
end;
procedure philosopher(i: integer);
begin
  repeat
    think;
    takefork(i);
    eat;
    releasefork(i)
  forever
end;
```
begin (* main program *)
cobegin
philosopher(0);
philosopher(1);
philosopher(2);
philosopher(3);
philosopher(4)
coend
end.

Fig. 7.3.

The previous solution failed because a philosopher is allowed to blindly take a free fork. In the present solution (Fig. 7.3), the array fork is now intended to represent the number of free forks available to a philosopher. Only if both forks are available will the philosopher take them (by completing procedure takefork). The mutual exclusion among monitor procedures and the immediate resumption of a signalled process ensure that the intended meaning holds since (i) no other process can access fork as long as a process is in the monitor, and thus (ii) the process that notes that two forks are available can update the status of fork[i−1] and fork[i+1] before its neighbors can continue.

Freedom from deadlock can be shown as follows. Let eating = the number of philosophers eating. Then when no process is in a monitor procedure, it is easy to see that

\[ I = \sum_{i=1}^{4} \text{fork}[i] = 10 - 2 \times \text{eating} \]

is invariant.

1. Initially eating = 0 and \( \sum \text{fork}[i] = 10 \).
2. \( \sum \text{fork}[i] \) is decreased by 2 and eating is incremented by 1 by every process completing takefork.
3. \( \sum \text{fork}[i] \) is increased by 2 and eating is decremented by 1 by every process completing releasefork.

For deadlock to occur, we must have all processes waiting, and so eating = 0. By I, \( \sum \text{fork}[i] = 10 \). Thus the last process, say j, to execute takefork and wait must have found \( \text{fork}[j] = 2 \) and would not have waited, contrary to the assumption.

Consider now the scenario in Fig. 7.4.

Philosopher 2 is going to starve to death because philosophers 1 and 3 are conspiring to cause a lockout. By our rules, if there is even one scenario that leads to lockout, the solution must be rejected. Note that we do not assume that a philosopher eats indefinitely as eating has the status of a
critical section. However, we can assume that two philosophers think very fast and eat very slowly.

<table>
<thead>
<tr>
<th></th>
<th></th>
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<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Initially</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>takefork[1]</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>takefork[3]</td>
<td>1</td>
<td>2</td>
<td>0</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>takefork[2] and wait</td>
<td>1</td>
<td>2</td>
<td>0</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>releasefork[1]</td>
<td>2</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>takefork[1]</td>
<td>1</td>
<td>2</td>
<td>0</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>releasefork[3]</td>
<td>1</td>
<td>2</td>
<td>1</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>takefork[3]</td>
<td>2</td>
<td>2</td>
<td>0</td>
<td>2</td>
<td>1</td>
</tr>
</tbody>
</table>

Fig. 7.4.

7.4 A CORRECT SOLUTION

program diningphilosophers;
var      fork: array [0 . . 4] of (* binary *) semaphore;
        room: semaphore;
        i: integer;
procedure philosopher(i: integer);
begin
  repeat
    think;
    wait(room);
    wait( fork[i] );
    wait( fork[(i+1) mod 5] );
    eat;
    signal( fork[i] );
    signal( fork[(i+1) mod 5] );
    signal(room)
  forever
end;
begin (* main program *)
  room := 4;
  for i := 0 to 4 do fork[i] := 1;
  cobegin
    philosopher(0);
    philosopher(1);
    philosopher(2);
    philosopher(3);
    philosopher(4)
  coend
end.

Fig. 7.5.
The solution in Fig. 7.5 is similar to the first attempted solution except for the additional enclosing semaphore *room*. The safety properties hold as before. Deadlock is not a problem since *room* ensures that at most 4 philosophers are attempting to access forks. By a simple application of the "pigeon-hole principle" any attempt to distribute the five forks in the circle among the 4 philosophers must result in at least one philosopher having two forks. The semaphore invariant for the *room* is: \( \text{room} + (\text{number of processes between wait(\text{room}) and signal(\text{room})}) = 4 \).

Let us now prove a series of lemmas that imply that this solution is starvation-free.

**Lemma 7.1** If \( P_i \) executes \( \text{wait(fork[i])} \), eventually it will complete the \( \text{wait} \).

*Proof*
If \( P_i \) does not complete the \( \text{wait} \) it is only because \( \text{fork[i]} = 0 \) which implies that \( P_{i-1} \) is eating (since this is \( P_{i-1} \)'s right-hand fork which was taken just before \( \text{eat} \)). Eventually \( P_{i-1} \) finishes eating and executes \( \text{signal(fork[i])} \) allowing \( P_i \) to proceed.

*(Advanced) Remark* We must assume some definition of semaphores (such as Morris') stronger than the weak definition to avoid elementary semaphore lockout even among two processes. What we are interested in is showing that lockout cannot be caused by conspiring processes. The previous attempt suffered from lockout even though the monitor uses the strong FIFO assumption on its queues.

**Lemma 7.2** If \( P_i \) is waiting indefinitely on \( \text{fork[i+1]} \) then \( P_{i+1} \) is waiting indefinitely on \( \text{fork[i+2]} \).

*Proof*
Only \( P_i \) and \( P_{i+1} \) "compete" for the semaphore \( \text{fork[i+1]} \). If \( P_{i+1} \) is terminated in \( \text{think} \) then \( \text{fork[i+1]} \) cannot block \( P_i \). Similarly, \( P_i \) and \( P_{i+1} \) cannot be simultaneously blocked on the same semaphore \( \text{fork[i+1]} \) (think of the semaphore invariant). Thus if \( P_i \) is blocked on \( \text{fork[i+1]} \) and \( P_{i+1} \) is assumed never to \( \text{signal} \) that semaphore, the only possibility left is for \( P_{i+1} \) to be blocked indefinitely on the other semaphore: \( \text{fork[i+2]} \).

**Lemma 7.3** If \( P_i \) executes \( \text{wait(fork[i+1])} \), eventually it will complete the \( \text{wait} \) (and eat).

*Proof*
By four successive applications of Lemma 7.2 we have that if \( P_i \) waits indefinitely on \( \text{fork[i+1]} \) then \( P_{i+j} \) waits indefinitely on \( \text{fork[i+j+1]} \), \( j=1, \ldots, 4 \) but this contradicts the semaphore invariant for *room*. 
7.5 CONDITIONAL CRITICAL REGIONS

A solution to the dining philosophers problem using semaphores is difficult to write because of the limited semantic content of the semaphore operations. A process can only test if an integer variable is zero and if so the process is suspended. Thus we have no way of making a compound test on the value of two "forks".

A synchronization primitive that does not suffer from this limitation is the conditional critical region. A critical region is a primitive for mutual exclusion. region r begin s_1, \ldots, s_n end executes the sequence of statements s_1, \ldots, s_n as a critical section. If several processes try to enter the critical region r simultaneously, then only one successfully enters and the others must wait on a queue. When a process leaves a critical region, another process from the queue is allowed to enter. Similarly, if a process attempts to enter a region while another process is within the region, the new process must join the queue.

Several regions can be declared to allow distinct critical sections to be entered simultaneously, just as several semaphores or monitors may be declared.

The solution to the mutual exclusion problem is immediate (Fig. 7.6).

```
program mutualexclusion;
procedure p_1;
begin
  repeat
    rem_1;
    region r begin crit_1 end
    forever
  end;
procedure p_2;
begin
  repeat
    rem_2;
    region r begin crit_2 end
    forever
  end;
begin (* main program *)
  cobegin
    p_1; p_2
  coend
end.
```

Fig. 7.6.
To solve more difficult problems, the conditional critical region is used. Competition for entry to the critical region is allowed only if an entry condition is satisfied. These are similar to the Ada guards.

The syntax is: `await b region r begin s₁; ...; sₙ end`. The semantics are: `b` is first evaluated. If `b` is true then the process may enter the competition to enter the critical region (and of course, succeed in entering if the region is free). If `b` is false, the process must enter the queue of waiting processes.

Whenever a process exits a critical region, all the processes waiting on its queue are released. Those processes having entry conditions must re-evaluate them. Processes with true conditions (including processes with no conditions) then compete to enter the critical region. The implementation should ensure that this competition is "fair", though FIFO is not specified as it is in the monitor.

We let each process evaluate its own condition—thus allowing expressions of arbitrary complexity, including those using local variables and procedures. The price we pay for this flexibility is the overhead of evaluating such expressions repeatedly as the process competes for entry into the critical section.

If we compare conditional critical regions with monitors, we see that the monitor has the flexibility of evaluating arbitrary expressions, but since the "condition" is named and explicitly signalled there is no busy wait overhead incurred by repeated evaluation.

Semaphores can be easily simulated:

```plaintext
wait(sem): await sem> 0 region r begin sem := sem−1 end.
signal(sem): region r begin sem := sem+1 end.
```

In Fig. 7.7 is a solution to the problem of the dining philosophers using conditional critical regions. The solution is similar to the monitor solution (Fig. 7.3). The conditional critical region primitive is here exactly what is needed to accomplish the compound test, something we could not do with semaphores.

```plaintext
program diningphilosophers;
var forks: array[0 .. 4] of integer;
i: integer;
procedure philosopher(i: integer);
begin
  repeat
    think;
    await forks[i]=2
    region r begin
      forks[(i+1) mod 5] := forks[(i+1) mod 5]−1;
      forks[(i−1) mod 5] := forks[(i−1) mod 5]−1
    end;
```
eat;
region r begin
    forks[(i+1) mod 5] := forks[(i+1) mod 5]+1;
    forks[(i-1) mod 5] := forks[(i-1) mod 5]+1
end forever end;
begin (* main program *)
    for i := 0 to 4 do forks[i] := 2;
    cobegin
      philosopher(0);
      philosopher(1);
      philosopher(2);
      philosopher(3);
      philosopher(4)
    coend
end.

Fig. 7.7.

Conditional critical regions do not have the theoretical appeal of the elementary semaphores. Practitioners have overwhelmingly preferred to implement the monitor. The effort involved is fully repaid by the flexibility of the concept and by the benefits obtained by the structuring of the data and procedures within a monitor. The Ada programming language, though it uses a different primitive, also encourages encapsulation of data and procedures in packages and tasks.

7.6 EXERCISES

7.1 Prove in greater detail the safety properties of the various algorithms.

7.2 Write one (or several) of the solutions in the chapter using the Ada rendezvous.

7.3 Program the following algorithm (in any formalism): a philosopher wishing to eat picks up his left fork; if his right fork is available, he picks it up and commences eating else he releases his left fork and repeats this cycle. Discuss the correctness of this algorithm.

7.4 All the solutions in this chapter are symmetrical, that is, all the philosophers execute the same code parameterized by the process number and furthermore no process explicitly uses its process number in the code. Try to find asymmetrical solutions: program them and discuss correctness. For example: change the first attempted solution so that one of the processes executes \texttt{wait(fork}[i+1]) and then \texttt{wait(fork[i])} instead of conversely.

7.5 *Discuss the solution sketched in Fig. 7.8. We have deviated from Ada by allowing a \texttt{select} statement with no \texttt{accept} clause. The effect is that of a non-deterministic choice between the two possibilities.
task body fork is
begin
  loop
    select
      (* become i's left fork *)
      leftfork(i);
      accept releaselleftfork(i);
    or
      (* become i+1's right fork *)
      rightfork(i+1);
      accept releaserightfork(i+1);
    end select;
  end loop;
end;

(task body philosopher is)
begin
  loop
    think;
    select
      accept leftfork(i);
      accept rightfork(i);
    or
      accept rightfork(i);
      accept leftfork(i);
    end select;
    eat;
    releaselleftfork(i);
    releaserightfork(i);
  end loop;
end.

Fig. 7.8.
APPENDIX: IMPLEMENTATION KIT

A.1 INTRODUCTION

Soon, perhaps, every student of computer science will have his own minicomputer and sufficient time to learn its hardware thoroughly so that he may exercise concepts of concurrent programming by building a real-time or operating system from scratch. Until then, the accepted solution to class exercise of concurrent programming is to simulate concurrent execution.

There are several serious implementations which are noted in the references. This appendix contains the listing and documentation of a very simple system which can exercise concurrent execution with synchronization by semaphores. This system can thus be used by any instructor who does not have access to one of the more serious systems. The system is not efficient and is not intended to be used for extensive concurrent programming but it has been successfully used to demonstrate (the hard way) to students the difficulties of concurrent programming. Note that even though the system is written in Pascal, it uses only a subset of the language that could easily be translated into any block structured language. Similarly, the machine dependencies (such as record packing to save space) are clearly noted and easily changed. This appendix, however, presumes a knowledge of Pascal.

The program in the listing (Section A.8) is a simplification and modification of the Pascal-S interpreter originally written by N. Wirth. Pascal-S compiles a subset of Pascal into pseudo-code (P-code) for a hypothetical machine and then proceeds to interpret (simulate the execution of) this code. The general structure of Pascal-S is shown in Fig. A.1.

```pascal
program pascals;
var code: array [1..codemax] of instructions;
procedure block;
```
begin
  Compile the Pascal-S program and store the compiled instructions in
  the array code.
end;
procedure interpret;
var stack: array [1 .. stackmax] of integer;
begin
  Simulate the instructions in code.
  The array stack serves as the memory of the simulated computer.
end;
begn (* main program *)
  initialize;
  block;
  interpret;
end.

Fig. A.1.

The object language P-code is for a stack machine. By this is meant that there are no registers or accumulators as on most computers. Instead, all operands are contained on a stack. A command such as Add needs no further specification since it automatically refers to the operands on the stack: Add the top two elements and replace them with the result as the top element in the stack. This architecture has actually been used on real computers (such as the Burroughs 6700) and even on pocket calculators (of the HP series).

In a stack machine \( A := B + C \) is compiled into the following sequence of instructions:

1. Load the address of \( A \) onto the stack.
2. Load the value of \( B \) onto the stack.
3. Load the value of \( C \) onto the stack.
4. Add: remove the top two elements from the stack. Add them together and store the result as the top element on the stack.
5. Store the top element in the address that appears just below it on the stack. Remove these two elements.

A.2 THE COMPILER

The subset of Pascal compiled is:

1. Simple data types: integer, boolean, char.
2. Structures: arrays (including multidimensional arrays)
3. Strings: Only in the form: write(# this is a title #).
4. Operators: integer (+, -, *, div, mod); boolean (not, and, or).
5. Relations: $=, <>, >, <=, ==$.

6. Declarations: **const**, **type**, **var**, **procedure**, **function**.

7. Statements:
   
   - assignment;
   - if $b$ then $s$;
   - if $b$ then $s_1$ else $s_2$;
   - while $b$ do $s$;
   - repeat $s_1 \ldots ; s_k$ until $b$;
   - for $i := e_1$ to $e_2$ do $s$;

8. Block structure: procedures and functions may be nested under the usual block structuring rules of Pascal. They may have both variable and value parameters.

9. Concurrency: in the main program, a single compound statement of the form **cobegin** $s_1; \ldots ; s_n$ **coend** is allowed to indicate concurrent execution of $s_1, \ldots, s_n$ which must be global procedure calls.

10. **wait(s)** and **signal(s)** are predefined semaphore operations looking for integer variables. The initial value of the semaphore should be set by an assignment statement in the main program. For pedagogical reasons, a **semaphore** type is provided. However, it is synonymous with **integer** and provides no protection.

The compilation is by top-down recursive descent. A similar compiler is extensively described in the book *Structured System Programming* by Welsh and McKeag (1980) and thus we do not discuss it further except as needed to understand the concurrent interpreter. The only point we feel obliged to note is the use of a simpler data structure for the identifiers. They are kept in an array **tab**; the entry for an identifier contains a **link** field which contains the index of the previous identifier in the same level of block nesting.

### A.3 THE P-CODE

The P-code instructions consist of an instruction field and possibly two operand fields $x$ and $y$. $x$ is used to point to the static level as described below and $y$ is used to pass operands to the instructions. The interpreter uses the following data passed to it by the compiler.

- **btab**—the block table, discussed below.

- **atab**—the array table which has an entry for each array. The entries contain the following fields:
  - **low, high**: the limits on the array index,
  - **elsize**: the size of an array element.

The following fields are used only by the compiler and will not concern us further:
size: the total size of the array,
elfyp, inxtype: the types of the elements and the index,
elref: a pointer to an entry in atab if the elements of the array are
temselves arrays.

code—the compiled P-code.

stab—a table containing all the strings in the program. A string is
identified by a starting index in stab and the number of characters.

The “memory” of the interpreter is the array s which is treated as a
stack. All data are stored as integers. Characters may be stored and retrieved
using Pascal functions ord and chr. For booleans we have written functions
booleantointeger and integertoBoolean.

The pseudo-instructions are summarized in the following table: x and y
refer to the operand fields of the instruction and t is an index in s for the top
of the stack. Instructions 0–7, 18–19, 32–33 will be further discussed later;
the others are straightforward.

0: Load Address
1: Load Value
2: Load Indirect
3: Update Display
4: Cobegin
5: Coend
6: Wait
7: Signal
8: End of Line and End of File
10: Jump to address y
11: Jump to address y if s[t] is false
14: Precedes the code of s in the for-loop:
    for i := e1 to e2 do s.
    y = the address of the instruction after the loop
    s[t] = e2; s[t−1] = e1; s[t−2] = address of i
15: Follows the code of s in the for-loop. y = address of s
18: Markstack
19: Procedure Call
21: Select an element of array atab[y] and push it onto the stack.
    s[t] = value of the index
22: Push y words from address s[t] onto the stack
23: Copy y words from address s[t] to address s[t−1]
24: Push the literal y onto the stack
27: Read a value of type y into the variable whose address is s[t]
28: Write s[t] characters from stab[y]
29: Write s[t]
31: Halt
32: Return from procedure
33: Return from function
34: \( s[t] \) is an address; replace it by its value
38: Store \( s[t] \) at address \( s[t-1] \)
35–36, 45–59: Arithmetic and boolean operations
62, 63: Readln, Writeln
Others: omitted in the simplification from Wirth’s Pascal-S

In a block-structured language the address of a variable is denoted by a pair (Level, Address) where Level is the depth of nesting of blocks when the variable was declared and Address is the offset of this variable within the memory segment associated with this level. Note that the rules of block structuring require that blocks be nested. Thus the memory segments can be stacked. To access a non-local variable, one simply follows the links which define the nesting until the proper level is reached (Fig. A.2, where \( s \) is a local procedure of \( r \) which in turn is local to main program \( p \)). These links are called static links.

![Diagram](attachment:image)

Fig. A.2.

If, however, we are going to execute the P-code, we need some faster way of accessing a variable. This is done by using a display which is an array indexed by levels whose elements point to the memory segments representing the current situation of block nesting. This is the same as saying that the
display holds the current static links. The address of a variable is calculated by computing \( \text{display}[x]+y \) where \((x, y) = (\text{Level}, \text{Address})\).

Instructions 0, 1, 2, in the interpreter can now be understood as 0: Load an address; 1: Load a value; and 2: Indirect loading of a value. 2 is used in the case of a \text{var} parameter where what is passed to the procedure is the address of the address of a variable.

There is a price that must be paid for the elegance of the display. Any change in the current block structure, i.e. a procedure or function call must update the display. Hopefully, this occurs infrequently relative to accesses to the variables.

### A.4 PROCEDURE CALLS

During the normal execution of a program by the interpreter, the two main pieces of dynamic information that must be maintained are \text{pc} (program counter) which points to the next instruction to be executed, and \(t\) which points to the current top of the stack. In addition, we maintain \(b\) which points to the bottom of the current stack segment and \text{stacksize} which points to the limit of the area allocated for the stack. Finally \text{display} keeps track of the addressing by nesting level.

Each time a procedure or function is called we need to allocate memory for the local variables as well as for certain additional information, such as the return address to jump to upon completion of the procedure. It is convenient to allocate this memory on the same stack that is used for the operands and to do the necessary adjustments upon the procedure call and return. The memory allocated upon procedure call is called an activation record.

In Pascal-S an activation record has a fixed part of five words:

\[
\begin{align*}
\text{ar}[0] &= \text{Function result;} \\
\text{ar}[1] &= \text{Return address;} \\
\text{ar}[2] &= \text{Static link;} \\
\text{ar}[3] &= \text{Dynamic link;} \\
\text{ar}[4] &= \text{Table pointer.}
\end{align*}
\]

When a function call is completed, the value of the function is left in place of the entire activation record. Conveniently, then, the effect of a function call is to push its result onto the stack just as if it were a normal operand. The return address contains the address of the instruction to be executed upon procedure exit. The table pointer contains the index into the identifier table \text{tab} for the procedure name. The \text{tab} field \text{adr} contains the index into the \text{code} table of the procedure code and \text{ref} contains the index into the block table to be described shortly.
If a procedure $p$ has called a procedure $q$ then the dynamic link of $q$ points to the start of the activation record of $p$. It is used upon procedure exit to reset the various stack pointers. The static link points to the start of the activation record of the procedure which textually encloses the called procedure. This defines the block structure of the language and can be either used directly to access variables or reflected in the display.

To understand the difference between a static and a dynamic link look at Figs. A.2 and A.3 which show the activation records at two points during the execution of the following program.

```
program $p$;
procedure $q$;
begin ... end;
procedure $r$;
    procedure $s$;
        begin ... $q$ ... end;
    begin ... $s$ ... end;
begin (* main program *) ... $r$ ... end.
```

![Diagram](image-url)  
Fig. A.3
In Fig. A.2, \( p \) has called \( r \) (which is local to \( p \)) and then \( r \) has called \( s \) (which is local to \( r \)). The dynamic links show the sequence of the calls. The static links are the same since \( s \) can access the variables of \( r \) (which called it) and in turn \( r \) can access the variables of \( p \) (which called it). The display reflects the nesting levels 0, 1, 2.

In Fig. A.3, \( s \) has now called \( q \), which is local to \( p \) and \( q \) cannot access the variables of \( r \) and \( s \). This is indicated by the static pointer of the activation record of \( q \) which is now pointing to the activation record of \( p \). Note that though the sequence of calls is longer, the display is now shorter.

As a check to see if you understand these concepts, draw the links for some recursive procedure \( rec \). There will be a large number of different dynamic links—one for each recursive call of \( rec \)—but the static links will all point to the same activation record: that of the procedure in which \( rec \) is embedded.

We now describe the mechanics of a procedure call. A procedure or function call is compiled into:

18: Markstack;
    Compile the parameters;
19: Call;
3: Update Display (if necessary).

The activation record consists of:

1. the five word fixed area;
2. an area for the actual parameters (whether values or addresses), and
3. an area for the local variables of the procedure.

The array \( btab \) contains an entry for each procedure with fields: \( psize \) which is the sum of the lengths of areas (1) and (2) and \( vsize \) which is the sum of \( psize \) and the length of area (3). \( vsize \) is thus the total size of the activation record for this procedure. (There are also two fields \( last = \) pointer to the last identifier in this procedure and \( lastpar = \) pointer to the last parameter in this procedure. These are used only during the compilation and not during the simulation). \( btab[1] \) is an entry for the "environment" block containing predefined identifiers like \( integer \). \( btab[2] \) is thus the entry for the main program.

The instruction Markstack is passed the index of the procedure name in the identifier table \( tab \). Since the actual parameter evaluation may involve arbitrarily complicated computation, the main purpose of the Markstack instruction is to advance the stack pointer by five words so as to leave room on the stack for the fixed area. Then the evaluation of the parameters may freely use the stack above the fixed area.
In addition, Markstack performs the following services. Since the procedure name is seen and compiled before the actual parameters, the procedure name (via a pointer to the identifier table) is conveniently passed at this point to the interpreter. Markstack stores this operand in \( ar[4] \) for subsequent use by the Call. Markstack also checks that there is sufficient room in the stack for the activation record (\( vsize \)) and temporarily stores \( vsize \) in the slot to be used by the dynamic link.

Now the actual parameters can be computed. The compiler has determined that when this has been completed, the stack pointer \( t \) will point to \( psize \) words beyond the start of the activation record and in fact \( psize \) (actually \( (v/p)size - 1 \) is stored to use as an offset) is passed as the operand to Call. The stack at the beginning of Call is shown in Fig. A.4.

![Diagram](image)

**Fig. A.4.**

With a slightly more descriptive notation than the bare listing, the code of Call is shown in Fig. A.5. Fig. A.6. shows the stack following the completion of the procedure call. Procedure exit is relatively simple (Fig. A.7).
oldb := b;  (* Save the previous bottom of stack for the dynamic link *)
b := t - y;  (* New bottom stack is computed from psize as passed in y *)
inx := s[b+4];  (* Retrieve index of procedure in tab as left by Markstack *)
t := s[b+3]+b;  (* Compute new top of stack from vsize left by Markstack *)
level := tab[inx].lev;  (* Get nesting level in which procedure is defined *)
s[b + 2] := display[level];  (* Static link is the bottom of the stack segment of the level of definition *)
display[level+1] := b;  (* The procedure executes one level up, so update the display *)
s[b + 3] := oldb;  (* Set the dynamic link *)
s[b + 1] := pc;  (* Return address *)
pc := tab[inx].adr;  (* Jump to the procedure code *)
\[ t := b - 1; \]  
\[ pc := s[b + 1]; \]  
\[ b := s[b + 3]; \]

(* Restore the old top of the stack. For a function exit this is \( t := b; \) *)  
(* Restore return address *)  
(* Restore bottom of stack from the dynamic link *)

Fig. A.7.

There is one more problem that must be solved. If the procedure call is to a procedure on a lower static level than that of the calling procedure, the display will not be correct upon exit. In Fig. A.3 when the execution of \( q \) terminates, only \( display[0] \) pointing to the activation record of the main program will be correct. \( display[1] \) and \( display[2] \) must be made to point to the activation records of \( r \) and \( s \), respectively. This is done by the interpreter instruction (3): Update \( display(x, y) \) which updates \( display[y] \) down to \( display[x] \) by following the static links. In this case, the compiler must insert Update \( display(1, 2) \) which will cause \( b \)—currently pointing to the bottom of the activation record of \( s \) to be stored in \( display[2] \) and then obtain from the static link the index of the bottom of the activation record of \( r \) to store in \( display[1] \).

This completes our discussion of Pascal-S as applied to sequential programs. Before reading further you might want to think of the problems that will be encountered in extending the system to concurrent execution.

### A.5 CONCURRENCY

To execute several processes concurrently we need to maintain: a stack for each process which will be used for the local data of the process (including the data of any procedures called by the process) and a set of register images for each process. To execute a particular process, its images are loaded into the physical registers before execution.

In the case of Pascal-S "registers" are \( pc \), the stack pointers \( b \), \( t \) and \( stacksize \) and \( display \). We maintain a table \( ptab^\dagger \) with one entry for each process containing this information as well as two further pieces of information: \( active \) indicating whether this process is active (as opposed to terminated) and a pointer \( suspend \) which points to a semaphore if the process is suspended on a semaphore. The register images are "loaded" into the interpreter by the \textbf{with ptab[curpr]} statement which makes all references to the above variables take their values from the entry for the current process—\textit{curpr}.

\( \dagger \) The constant \( pmax \) controls the size of \( ptab \) and hence the number of concurrent processes allowed. For most efficient use of central memory, it is best to tailor a version of the kit for each class exercise. Conway's problem (Exercise 4.2) runs with \( pmax = 3 \) but Parnas' problem (Exercise 4.15) needs \( pmax = 9 \).
Similarly we should have a set of stacks—one for the main process (which contains all the global variables) and one for each concurrent process. If this is done, however, the interpreter would have to be passed an index to the stack table on each memory access. A simpler solution is to divide the single physical stack (the array $s$) into several logical segments—one for each process. Then as long as the displays are correct, all accessing is done normally. See Fig. A.8.

For simplicity, the stacks are pre-allocated. The use of dynamic allocation does not involve any conceptual difficulties but for our purposes it seems unnecessary. Various versions of this system can be tailored to suit each assigned exercise.
program p;
procedure q;
begin . . . end;
procedure r_1;
begin . . . q . . . end;
procedure r_2;
  procedure s;
  begin . . . q . . . end;
begin . . . s . . . end;
begin (* p *)
cobegin r_1; r_2 coend
end.
The semantics of **cobegin** ... **coend** are as follows: The concurrent processes are prepared for execution: Their parameters are evaluated and stored in the stack segments and the values of their register images are computed. Upon execution of the **coend** statement, the main process is set to inactive and the concurrent processes are activated. When all the concurrent processes have terminated (become inactive) the main process is reactivated.

This is accomplished by preferring the execution of the main process if it is active (**if ptab[0].active then curpr := 0 else ...**) and by having **coend** set the main process to inactive. At this point the choice of the current process to execute will always be made among the concurrent processes. The exit procedure instruction performed for a concurrent process will decrement the number of active processes and if this count reaches zero the main process is set to active.

The implementation of **cobegin** is to have it set a flag (**pflag**) which is used during the calling sequence to decide whether this is a concurrent process call. If so, the Markstack instruction allocates a **ptab** entry (by incrementing **npr**) and marks the stack segment assigned for the new process. This stack segment was defined during initialization of **ptab**. During the actual parameter evaluation, **pflag** ensures that the stack segment upon which the parameters are pushed is in fact this new segment (**if pflag then ...**). In the Call, the only difference is that the initialized activation record happens to belong to the called process and not the main process. Upon execution of the **coend**, **pflag** is reset so that if a concurrent process calls a procedure, the normal calling sequence is done.

Exit procedure uses a dummy return address to detect that this is the termination of a concurrent process. It deactivates the process and if this is the last concurrent process, it reactivates the main process.

Figure A.9 shows the stack at two instances during the execution of the program in Fig. A.10.

### A.6 SEMAPHORES

The interpreter allows easy implementation of semaphores because the entire operation can be done as one pseudo-instruction and does not require that the testing and incrementing be done as separate operations. **wait(s)** and **signal(s)** are compiled as standard procedures being passed the address of the parameter. **wait** is implemented as: **if s > 0 then s := s - 1 else suspend := address of s. signal** is implemented as: Search for a **ptab** entry with **suspend = address of s. if found then suspend := 0 else s := s + 1.**

**Remark** This is the definition of semaphores suggested by Morris and is the one that has the most natural implementation.


A.7 RANDOMIZATION

A random number generator is used to give the illusion of concurrency. chooseproc searches from a random starting point in ptab for a process which is active and not suspended. If there are no such processes, you can let the interpreter run to the computer's time limit or, as shown, explicitly declare a deadlock to the student.

Randomization is also used in signal to ensure that the awakened process will not be predetermined. stepcount is used to reduce the number of executions of chooseproc by allowing a process to execute a (random) number of consecutive steps before a process switch is done. Note that if a process becomes inactive or suspended, then stepcount is zeroed to force a process switch.

A.8 PROGRAM LISTING

program pascals(input, output);
(*author: N. Wirth, E. T. H. ch—8092 Zurich, 1. 3. 76*)
(*modified: M. Ben-Ari, Tel Aviv Univ., 1980*)
label 99;
const nkw=26; (*no. of key words*)
    alng=10; (*no. of significant chars in identifiers*)
    llng=121; (*input line length*)
    kmax=15; (*max no. of significant digits*)
    tmax=70; (*size of table*)
    bmax=20; (*size of block-table*)
    amax=10; (*size of array table*)
    cmax=500; (*size of code*)
    lmax=7; (*maximum level*)
    smax=150; (*size of string-table*)
    omax=63; (*highest order code*)
    xmax=131071; (*2**17 - 1*)
    nmax=281474976710655; (*2**48-1*)
    lineleng=132; (*output line length*)
    linelimin=400; (*max lines to print*)
    stmax=1400; (*stacksize*)
    stkincr=200; (*stacksize for each process*)
    pmax=3; (*max concurrent processes*)


```plaintext
type symbol = (intcon, charcon, string, 
notsy, plus, minus, times, idiv, imod, andsy, orsy, 
eql, neq, gtr, geq, lss, leq, 
lparent, rparent, lbrack, rbrack, comma, semicolon, 
period, 
colon, becomes, conssy, typesy, varsy, functionsy, 
proceduresy, arraysy, programsy, ident, 
beginsy, ifsy, repeatsy, whilesy, forsy, 
endsy, elsesy, untilsy, ofsy, dosy, tosy, thensy);

index = -xmax .. + xmax;
alpha = packed array [1 .. alng] of char;
object = (konstant, variable, type1, procedure, funktion);
types = (notyp, ints, bools, chars, arrays);
er = (erid, ertyp, erkey, erpun, erpar, ernf, erdup, erch, ersh, erln);
symset = set of symbol;
typset = set of types;
item = record 
  typ: types; ref: index;
end;
order = packed record 
  f: -omax .. +omax;
  x: -lmax .. +lmax;
  y: -nmax .. +nmax;
end;

var sy: symbol;               (*last symbol read by insymbol*)
id: alpha;                  (*identifier from insymbol*)
inum: integer;               (*integer from insymbol*)
num: real;                   (*real number from insymbol*)
sleng: integer;              (*string length*)
ch: char;                    (*last character read from source program*)
line: array [1 .. llng] of char;          (*character counter*)
cc: integer;                 (*program location counter*)
lc: integer;                 (*length of current line*)
errs: set of er;
errpos: integer;
progrname: alpha;
skipflag: boolean;
constbegsys, typebegsys, blockbegsys, facbegsys, statbegsys:
symset;
key: array [1 .. nkw] of alpha;
ksy: array [1 .. nkw] of symbol;
sps: array [char] of symbol;        (*special symbols*)
```
\text{t, a, b, sx, c_1, c_2: integer;} \quad (*\text{indices to tables}*)
\text{stantyps: typset;}
\text{display: array [0 \ldots lmax] of integer;}

\text{tab: array [0 \ldots tmax] of} \quad (*\text{identifier table}*)
\text{packed record}
\quad \text{name: alfa; link: index;}
\quad \text{obj: object; typ: types;}
\quad \text{ref: index; normal: boolean;}
\quad \text{lev: 0 \ldots lmax; adr: integer;}
\quad \text{end;}
\text{atab: array [1 \ldots amax] of} \quad (*\text{array-table}*)
\text{packed record}
\quad \text{inxtyp, eltyp: types;}
\quad \text{elref, low, high, elsize, size: index;}
\quad \text{end;}
\text{btab: array [1 \ldots bmax] of} \quad (*\text{block-table}*)
\text{packed record}
\quad \text{last, lastpar, psize, vsize: index}
\quad \text{end;}
\text{stab: packed array [0 \ldots smax] of char;}
\text{code: array [0 \ldots cmax] of order;}

\text{procedure erromsg;}
\text{var k: er;}
\text{msg: array [er] of alfa;}
\text{begin}
\text{msg[erid] := \#identifier\#; msg[ertyp] := \#type \#;}
\text{msg[erkey] := \#keyword \#; msg[erpun] := \#punctuation\#;}
\text{msg[erpar] := \#parameter \#; msg[ernf] := \#not found \#;}
\text{msg[erdup] := \#duplicate\#; msg[erch] := \#character \#;}
\text{msg[ersh] := \#too short \#; msg[erln] := \#too long \#;}
\text{message(\# compilation errors\#);}
\text{writeln; writeln(\# key words\#);}
\text{for k := erid to erln do if k in errs then}
\text{writeln(ord(k), \# \#, msg[k])}
\text{end (*erromsg*);}

\text{procedure endskip;}
\text{begin (*underline skipped part of input*)}
\text{while errpos < cc do}
\text{begin write(\#\#); errpos := errpos + 1}
\text{end;}
\text{skipflag := false}
\text{end (*endskip*);}
procedure nextch; (*read next character; process line end*)
begin if cc=ll then
    begin if eof(input) then
        begin writeln;
            writeln(# program incomplete#);
            errormsg; goto 99
        end;
        if errpos <> 0 then
            begin if skipflag then endskip;
                writeln; errpos := 0
            end;
        write(lc:5, # #);
        ll := 0; cc := 0;
        while not eoln(input) do
            begin ll := ll+1; read(ch); write(ch); line[ll] := ch
                end;
            writeln; ll := ll+1; read(line[ll])
        end;
        cc := cc+1; ch := line[cc];
    end (*nextch*);

procedure error(n: er);
begin if errpos = 0 then write(# ****#);
    if cc > errpos then
        begin write(# #: cc-errpos, '#', ord(n):2);
            errpos := cc+3; errs := errs+[n]
        end
    end (*error*);

procedure fatal(n: integer);
    var msg: array [1 .. 6] of alfa;
begin writeln; errormsg:
    writeln(# compiler table for #, msg[n], # is too small#);
    goto 99 (* terminate compilation*)
end (*fatal*);

(* ----------------------------------------------------------------------------------------------------insymbol-*)

procedure insymbol; (*reads next symbol*)
    label 1,2,3;
    var i, j, k, e: integer;
begin (*insymbol*)
1: while ch= # # do nextch;
   case ch of
   #a#, #b#, #c#, #d#, #e#, #f#, #g#, #h#, #i#, 
   #j#, #k#, #l#, #m#, #n#, #o#, #p#, #q#, #r#, 
   #s#, #t#, #u#, #v#, #w#, #x#, #y#, #z#:
   begin (*identifier or wordsymbol*) k := 0; id := # #;
     repeat if k < alng then
       begin k := k + 1; id[k] := ch
     end;
   nextch
   until not (ch in [#a#..#z#, #0#..#9#]);
   i := 1; j := nkw; (*binary search*)
   repeat k := (i+j) div 2;
     if id <= key[k] then j := k - 1;
     if id >= key[k] then i := k + 1
   until i > j;
   if i - 1 > j then sy := ksy[k] else sy := ident
end;
#0#, #1#, #2#, #3#, #4#, #5#, #6#, #7#, #8#, #9#:
begin (*number*) k := 0; inum := 0; sy := intcon;
   repeat inum := inum*10 + ord(ch) - ord(#0#);
     k := k + 1; nextch
   until not (ch in [#0#..#9#]);
   if (k > kmax) or (inum > nmax) then
     begin error(elln); inum := 0; k := 0
     end;
end;

#:#, col: begin nextch;
   if ch = #==# then
     begin sy := becomes; nextch
     end else sy := colon
end;
#<# : begin nextch;
   if ch = #==# then begin sy := leq; nextch end else
   if ch = #># then begin sy := neq; nextch end else
     sy := lss
end;
#># : begin nextch;
   if ch = #==# then begin sy := geq; nextch end else
     sy := gtr
end;
.#.# : begin nextch;
   if ch = #.# then
begin sy := colon; nextch
end else sy := period
end;

### #: begin k := 0;
2: nextch;
  if ch = ### then
    begin nextch; if ch <> ### then goto 3
    end;
  if sx+k = smax then fatal(3);
  stab[sx+k] := ch; k := k+1;
  if cc = 1 then
    begin (*end of line*) k := 0;
    end
  else goto 2;
3: if k = 1 then
  begin sy := charcon; inum := ord(stab[sx])
  end else
  if k = 0 then
    begin error(ersh); sy := charcon; inum := 0
    end else
    begin sy := string; inum := sx; sleng := k; sx := sx+k
    end
end;

### #: begin nextch;
  if ch <> ### then sy := lparent else
  begin (*comment*) nextch;
    repeat
      while ch <> ### do nextch;
      nextch
    until ch = #);
  nextch; goto 1
end
end;

### #, #-, #*, #)%, #=%, #, #, #[##, #], #;# :
begin sy := sps[ch]; nextch
end;

### $%, #!%, #@%, #\%, #:%, #_;%, #?%, #', #", #&%, #]|% :
begin error(erch); nextch; goto 1
end
end
end (*insymbol*);

(* ------------------------------- enter ---*)
procedure enter (x₀: alfa; x₁: object;
  x₂: types; x₃: integer);
begin t := t + 1; (*enter standard identifier*)
  with tab[t] do
    begin name := x₀; link := t - 1; obj := x₁;
      typ := x₂; ref := 0; normal := true;
      lev := 0; adr := x₃
    end
end (*enter*);

procedure enterarray(tp: types; l,h: integer);
beginc if l > h then error(ertyp);
  if (abs(l) > xmax) or (abs(h) > xmax) then
    begin error(ertyp); l := 0; h := 0;
      end;
  if a = amax then fatal(4) else
    begin a := a + 1;
      with atab[a] do
        begin inxtyp := tp; low := l; high := h
          end
    end
end (*enterarray*);

procedure enterblock;
beginc if b = bmax then fatal(2) else
  begin b := b + 1; btab[b]. last := 0; btab[b]. lastpar := 0
    end
end (*enterblock*);

procedure emit(fct: integer);
beginc if lc = cmax then fatal(6);
  code[lc]. f := fct; lc := lc + 1
end (*emit*);

procedure emit1(fct, b: integer);
beginc if lc = cmax then fatal(6);
  with code[lc] do
    begin f := fct; y := b end;
    lc := lc + 1
end (*emit1*);

procedure emit2(fct, a, b: integer);
beginc if lc = cmax then fatal(6);
  with code[lc] do
    begin f := fct; x := a; y := b end;
    lc := lc + 1
end (*emit2*);
procedure block(fs: symset; isfun: boolean; level: integer);

    type conrec =
        record tp: types; i: integer end;

    var dx: integer; /*data allocation index*/
        prti: integer; /*t–index of this procedure*/
        prbi: integer; /*b–index of this procedure*/
        x: integer;

    procedure skip(fs: symset; n: er);
    begin error(n); skipflag := true;
        while not (sy in fs) do insymbol;
        if skipflag then endskip
    end (*skip*);

    procedure test(s1, s2: symset; n: er);
    begin if not (sy in s1) then
        skip(s1 + s2, n)
    end (*test*);

    procedure testesemicolon;
    begin
        if sy = semicolon then insymbol else error(erpun);
            test([ident]+blockbegsys, fsys, erkey);
    end (*testesemicolon*);

    procedure enter(id: alfa; k: object);
    var j, l: integer;
    begin if t = imax then fatal(1) else
        begin tab[0]. name := id;
            j := bab[display[level]]. last; l := j;
                while tab[j]. name <> id do j := tab[j]. link;
            if j <> 0 then error(erdup) else
                begin t := t+1;
                    with tab[t] do
                    begin name := id; link := l;
                        obj := k; typ := notyp; ref := 0; lev := level; adr := 0
                    end;
                    btab[display[level]]. last := t
                end
        end
    end (*enter*);
function loc(id: alfa): integer;
  var i, j: integer; (*locate id in table*)
begin i := level; tab[0]. name := id; (*sentinel*)
  repeat j := htab[display[i]]. last;
    while tab[j]. name <> id do j := tab[j]. link;
      i := i-1;
  until (i<0) or (j<>0);
  if j = 0 then error(errn); loc := j
end (*loc*);

procedure entervariable;
begin if sy = ident then
  begin enter(id, variable); insymbol
  end
else error(eric)
end (*entervariable*);

procedure constant(fsx: symset; var c: conrec);
  var x, sign: integer;
begin c. tp := notyp; c.i := 0;
  test(constbega, fsx, erkey);
if sy in constbega then
begin
  if sy = charcon then
    begin c. tp := chars; c. i := inum; insymbol
    end
else
  begin sign := 1;
    if sy in [plus, minus] then
      begin if sy = minus then sign := -1;
        insymbol
      end;
    if sy = ident then
      begin x := loc(id);
        if x <> 0 then
          if tab[x]. obj <> konstant then error(ertyp) else
            begin c. tp := tab[x]. typ;
              c. i := sign*tab[x]. adr
            end;
        insymbol
      end
else
  if sy = intcon then
begin c. tp := int; c. i := sign*inum; insymbol end
else skip(fsys, erkey)
end;
test(fsys, [], erkey);
end
end (*constant*);

procedure typ(fsys: symset; var tp: types; var rf, sz: integer);
var x: integer;
elp: types; elrf: integer;
elsz, offset, t0, t1: integer;

procedure arraytyp(var aref, arsz: integer);
var eltp: types;
low, high: conrec;
elrf, elsz: integer;
begin constant([colon, rbrack, ofsy]+fsys, low);
if sy = colon then insymbol else error(erpun);
constant([rbrack, comma, ofsy]+fsys, high);
if high. tp <> low. tp then
begin error(ertyp); high. i := low. i
end;
enterarray(low. tp, low. i, high. i); aref := a;
if sy = comma then
begin insymbol; eltp := arrays; arraytyp(elrf, elsz)
end else
begin
if sy = rbrack then insymbol else error(erpun);
if sy = ofsy then insymbol else error(erpkey);
typ(fsys, eltp, elrf, elsz)
end;
with atab[aref] do
begin arsz := (high−low+1)*elsz; size := arsz;
elpyp := eltp; elref := elrf; elseize := elsz
end;
end (*arraytyp*);

begin (*typ*) tp := notyp; rf := 0; sz := 0;
test(typebegasys, fsys, erid);
if sy in typebegasys then
begin
if sy = ident then
begin $x := \text{loc}(id)$;
if $x <> 0$ then
with $\text{tab}[x]$ do
  if $\text{obj} <> \text{type1}$ then $\text{error}(ertyp)$ else
  begin $tp := \text{typ}; rf := \text{ref}; sz := \text{adr}$;
    if $tp = \text{notyp}$ then $\text{error}(ertyp)$
  end;
end symbol
end else
if $sy = \text{arraysy}$ then
begin $\text{insymbol}$;
  if $sy = lbrack$ then $\text{insymbol}$ else $\text{error}(erpun)$;
  $tp := \text{arrays}; \text{arraytyp}(rf, sz)$
end else
$\text{test}(fsys, [ ], \text{erkey})$
end
end (*typ*)

procedure $\text{parameterlist}$; (*formal parameter list*)
var $tp$: types;
  $rf, sz, x, t_0$: integer;
valpar: boolean;
begin $\text{insymbol}$; $tp := \text{notyp}; rf := 0; sz := 0$
  $\text{test}([\text{ident, varsy}], fsys+[\text{parent}], \text{erpar})$;
while $sy$ in [ident, varsy] do
  begin if $sy <> \text{varsy}$ then $\text{valpar} := \text{true}$ else
    begin $\text{insymbol}$; $\text{valpar} := \text{false}$
    end;
    $t_0 := t$; $\text{entervariable}$;
  end;
while $sy$ = comma do
  begin $\text{insymbol}$; $\text{entervariable}$;
  end;
if $sy = \text{colon}$ then
  begin $\text{insymbol}$;
    if $sy <> \text{ident}$ then $\text{error}(erid)$ else
      begin $x := \text{loc}(id)$; $\text{insymbol}$;
      if $x <> 0$ then
        with $\text{tab}[x]$ do
          if $\text{obj} <> \text{type1}$ then $\text{error}(ertyp)$ else
            begin $tp := \text{typ}; rf := \text{ref}$;
            if $\text{valpar}$ then $sz := \text{adr}$ else $sz := 1$
            end;
end;
end;
    test([semicolon, rparent], [comma, ident]+fsys, erpun)
    end
else error(erpun);
while t₀ < t do
begin t₀ := t₀ + 1;
    with tab[t₀] do
    begin typ := tp; ref := rf;
        normal := valpar; adr := dx; lev := level;
        dx := dx + sz
    end
end;
if sy <> rparent then
begin if sy = semicolon then insymbol else error(erpun);
    test([ident, varsy], [rparent]+fsys, erkey);
end (*while*);
if sy = rparent then
begin insymbol;
    test([semicolon, colon], fsys, erkey);
end
else error(erpun)
end (*parameterlist*);

procedure constantdeclaration;
    var c: conrec;
begin insymbol;
    test([ident], blockbegsys, erid);
while sy=ident do
    begin enter(id, konstant); insymbol;
        if sy=eql then insymbol else error(erpun);
        constant([semicolon, comma, ident]+fsys, c);
        tab[i]. typ := c. tp; tab[i]. ref := 0;
        tab[i]. adr := c. i;
        testsemicolon
    end
end (*constantdeclaration*);

procedure typeddeclaration;
    var tp: types; rf, sz, t₁: integer;
begin insymbol;
    test([ident], blockbegsys, erid);
while sy=ident do
    begin

end;
begin enter(id, type1); t₁ := t; insymbol;
  if sy=eql then insymbol else error(erpun);
  typ([semicolon, comma, ident]+fsys, tp, rf, sz);
  with tab[t₁] do
    begin typ := tp; ref := rf; adr := sz
    end;
  testsemicolon
end
end (*typedeclaration*);

procedure variabledeclaration;
  var t₀, t₁, rf, sz: integer;
  tp: types;
begin insymbol;
  while sy = ident do
    begin t₀ := t; entervariable;
      while sy = comma do
        begin insymbol; entervariable;
        end;
    if sy = colon then insymbol else error(erpun);
    t₁ := t;
  typ([semicolon, comma, ident]+fsys, tp, rf, sz);
  while t₀ < t₁ do
    begin t₀ := t₀+1;
      with tab[t₀] do
        begin typ := tp; ref := rf;
          lev := level; adr := dx; normal := true;
          dx := dx+sz
        end;
    end;
  testsemicolon
end
end (*variabledeclaration*);

procedure procdeclaration;
  var isfun: boolean;
begin isfun := sy = functionsy; insymbol;
  if sy <> ident then
    begin error(erd); id := # # end;
  if isfun then enter(id, funktion) else enter(id, prozedure);
  tab[t₁]. normal := true;
  insymbol; block([semicolon]+fsys, isfun, level+1);
```plaintext
if sy = semicolon then insymbol else error(erpun);
emit(32 + ord(isfun)) (*exit*)
end (*proceduredeclaration*)

(*---------------------------------------------------------------------
statement--*)

procedure statement(fsys: symset);
var i: integer; x: item;
procedure expression(fsys: symset; var x: item); forward;
procedure selector(fsys: symset; var v: item);
var x: item; a, j: integer;
begin
if sy <> lbrack then error(ertyp);
repeat insymbol;
expression(fsys+[comma, rbrack], x);
if v. typ <> arrays then error(ertyp) else
begin a := v. ref;
if atab[a], inxtyp <> x. typ then error(ertyp) else
emit(21, a);
v. typ := atab[a]. eltyp; v. ref := atab[a]. elref
end
until sy <> comma;
if sy = rbrack then insymbol else error(erpun);
test(fsys, [ ], erkey);
end (*selector*)

procedure call(fsys: symset; i: integer);
var x: item;
lastp, cp, k: integer;
begin emit1(18, i); (*markstack*)
lastp := btab[tab[i]. ref]. lastpar; cp := i;
if sy = lparent then
begin (*actual parameter list*)
repeat insymbol;
if cp >= lastp then error(erpar) else
begin cp := cp + 1;
if tab[cp]. normal then
begin (*value parameter*)
expression(fsys+[comma, colon, rparent], x);
if x. typ = tab[cp]. typ then
begin
if x. ref <> tab[cp]. ref then error(ertyp) else
if x. typ = arrays then emit1(22, atab[x. ref]. size)
end else if x. typ <> notyp then error(ertyp);
```

end else
begin (*variable parameter*)
  if sy <> ident then error('erid) else
  begin k := loc(id); insymbol;
    if k <> 0 then
      begin if tab[k]. obj <> variable then error('erpar);
          x. typ := tab[k]. typ; x. ref := tab[k]. ref;
          if tab[k]. normal then emit2(0, tab[k]. lev, tab[k]. adr)
            else emit2(1, tab[k]. lev, tab[k]. adr);
        if sy=lbrack then
          selector(fsys+[comma, colon, rparent], x);
        if (x. typ<>tab[cp]. typ) or (x. ref<>tab[cp]. ref)
          then error(ertyp)
      end
    end
  end;
until sy <> comma;
if sy = rparent then insymbol else error(erpun)
end;
if cp < lastp then error(erpars); (*too few actual parameters*)
emit1(19, btab[tab[i]. ref]. psize–1);
if tab[i]. lev < level then emit2(3, tab[i]. lev, level)
end (*call*);

function resulttype(a, b: types): types;
begin
  if (a=ntyp) or (b=ntyp) then
    begin error(ertyp); resulttype := notyp
  end else
  if (a=ntyp) or (b=ntyp) then resulttype := notyp else
    resulttype := ints
end (*resulttype*);

procedure expression;
  var y: item; op: symbol;

procedure simpleexpression(fsys: symset; var x: item);
  var y: item; op: symbol;

procedure term(fsys: symset; var x: item);
  var y: item; op: symbol; ts: typset;
procedure factor(sys: symset; var x: item);
var i, f: integer;

begin (*factor*) x. typ := notyp; x. ref := 0;
test(facbegsys, sys, erpun);
while sy in facbegsys do
  begin
    if sy = ident then
      begin i := loc(id); insymbol;
        with tab[i] do
        case obj of
          konstant: begin x. typ := typ; x. ref := 0;
            emit1(24, adr)
          end;
          variable: begin x. typ := typ; x. ref := ref;
            if sy = lbrack then
              begin if normal then f := 0 else f := 1;
                emit2(f, lev, adr);
                selector(sys, x);
                if x. typ in stantyps then emit(34)
              end else
              begin
                if x. typ in stantyps then
                  if normal then f := 1 else f := 2
                else
                  if normal then f := 0 else f := 1;
                emit2(f, lev, adr)
              end
            end;
        end;
    type1, procedure: error(ertyp);
    funktion: begin x. typ := typ;
      if lev <> 0 then call(sys, i)
        else emit1(8, adr)
    end
  end (*case, with*)
end else
if sy in [charcon, intcon] then
  begin if sy = charcon then x. typ := chars
        else x. typ := ints;
    emit1(24, inum);
    x. ref := 0; insymbol
  end else
if sy = lparent then
begin insymbol; expression(fsys+[rparent], x);
    if sy = rparent then insymbol else error(erpun)
end else
if sy = notsy then
    begin insymbol; factor(fsys, x);
        if x. typ=bools then emit(35) else
            if x. typ<>notyp then error(ertyp)
    end;
test(fsys, facbegsys, erkey);
end (*while*)
end (*factor*);

begin (*term*)
    factor(fsys+[times, idiv, imod, andsy], x);
while sy in [times, idiv, imod, andsy] do
    begin op := sy; insymbol;
        factor(fsys+[times, idiv, imod, andsy], y);
        if op = times then
            begin x. typ := resulttype(x. typ, y. typ);
                if x. typ = ints then emit(57)
            end else
                if op = andsy then
                    begin if (x. typ=bools) and (y. typ=bools) then emit(56) else
                        begin if (x. typ<>notyp) and (y. typ<>notyp)
                            then error(ertyp);
                            x. typ := notyp
                        end
                    end else
                        begin (*op in [idiv, imod]*)
                            if (x. typ=ints) and (y. typ=ints) then
                                if op=idiv then emit(58)
                                    else emit(59) else
                                        begin if (x. typ<>notyp) and (y. typ<>notyp) then
                                            error(ertyp);
                                            x. typ := notyp
                                        end
                            end
                    end
            end
        end
end (*term*);

begin (*simpleexpression*)
    if sy in [plus, minus] then
\begin{verbatim}
begin op := sy; insymbol;
term(fsyz+[plus, minus], x);
if x. typ > ints then error(ertyp) else
  if op = minus then emit(36)
end else
  term(fsyz[plus, minus, orsy], x);
while sy in [plus, minus, orsy] do
  begin op := sy; insymbol;
term(fsyz+[plus, minus, orsy], y);
  if op = orsy then
    begin
      if (x. typ=bools) and (y. typ=bools) then emit(51) else
        begin
          if (x. typ<>notyp) and (y. typ<>notyp) then
            error(ertyp);
          x. typ := notyp
        end
    end
  end
  begin x. typ := resulttype(x. typ, y. typ);
    if x. typ = ints then if op = plus then emit(52)
      else emit(53)
  end
end
end (*simpleexpression*);

begin (*expression*);
simpleexpression(fsyz+[eql, neq, lss, leq, gtr, geq], x);
if sy in [eql, neq, lss, leq, gtr, geq] then
  begin
    op := sy; insymbol; simpleexpression(fsyz, y);
    if (x. typ in [notyp, ints, bools, chars])
      and (x. typ = y. typ) then
      case op of
        eql: emit(45);
        neq: emit(46);
        lss: emit(47);
        leq: emit(48);
        gtr: emit(49);
        geq: emit(50);
      end
    else error(ertyp);
    x. typ := bools
  end
end (*expression*);
\end{verbatim}
procedure assignment(lv, ad: integer);
  var x, y: item; f: integer;
  (*tab[i]. obj in [variable, prozedure]*)
begin x. typ := tab[i]. typ; x. ref := tab[i]. ref;
  if tab[i]. normal then f := 0 else f := 1;
  emit2(f, lv, ad);
  if sy = lbrack then
    selector([becomes, eqf] + fsys, x);
  if sy = becomes then insymbol else error(erpun);
  expression(fsys, y);
  if x. typ = y. typ then
    if x. typ in stantyps then emit(38) else
    if x. ref<> y. ref then error(ertyp) else
    if x. typ = arrays then emit1(23, atab[x. ref]. size)
  else error(ertyp)
end (*assignment*);

procedure compoundstatement;
begin insymbol;
  statement([semicolon, endsy] + fsys);
  while sy in [semicolon] + statbegsys do
    begin if sy = semicolon then insymbol else error(erpun);
      statement([semicolon, endsy] + fsys)
    end;
    if sy = endsy then insymbol else error(erkkey)
end (*compoundstatement*);

procedure ifstatement;
  var x: item; lc1, lc2: integer;
begin insymbol;
  expression(fsys + [thensy, dosy], x);
  if not (x. typ in [bools, notyp]) then error(ertyp);
  lc1 := lc; emit(11); (*jmpc*)
  if sy = thensy then insymbol else error(erkkey);
  statement(fsys + [elsesy]);
  if sy = elsesy then
    begin insymbol; lc2 := lc; emit(10);
      code[lc1]. y := lc; statement(fsys); code[lc2]. y := lc
    end
  else code[lc1]. y := lc
end (*ifstatement*);

procedure repeatstatement;
  var x: item; lc1: integer;
begin \( lc_1 := lc \);
insymbol; statement([semicolon, unilsy]+fsys);
while \textbf{sy in} [semicolon]+stabegsys \textbf{do}
begin \textbf{if} \textbf{sy =} semicolon \textbf{then} insymbol \textbf{else} error(erpun);
statement([semicolon, unilsy]+fsys)
end;
\textbf{if} \textbf{sy =} unilsy \textbf{then}
begin insymbol; expression(fsys, x);
\textbf{if} \textbf{not} (x. typ \in [bools, notyp]) \textbf{then} error(ertyp);
emit1(11, lc_1)
end
\textbf{else} error(erkey)
end (*repeatstatement*);

procedure \textbf{whilestatement};
\textbf{var} x: item; \textbf{lc}_1, \textbf{lc}_2: integer;
begin insymbol; \textbf{lc}_1 := lc;
expression(fsys+[dosy], x);
\textbf{if} \textbf{not} (x. typ \in [bools, notyp]) \textbf{then} error(ertyp);
\textbf{lc}_2 := lc; emit(11);
\textbf{if} \textbf{sy =} dosy \textbf{then} insymbol \textbf{else} error(erkey);
statement(fsys); emit1(10, \textbf{lc}_1); code[\textbf{lc}_2]. y := \textbf{lc}
end (*whilestatement*);

procedure \textbf{forstatement};
\textbf{var} cvt: types; x: item;
i, \textbf{lc}_1, \textbf{lc}_2: integer;
begin insymbol;
\textbf{if} \textbf{sy =} ident \textbf{then}
begin i := loc(id); insymbol;
\textbf{if} \textbf{i =} 0 \textbf{then} cvt := intsize \textbf{else}
\textbf{if} \textbf{tab}[i]. obj = variable \textbf{then}
begin cvt := \textbf{tab}[i]. typ;
\textbf{if} \textbf{not} \textbf{tab}[i]. normal \textbf{then} error(ertyp) \textbf{else}
emit2(0, \textbf{tab}[i]. lev, \textbf{tab}[i]. adr);
\textbf{if} \textbf{not} (cvt \in [notyp, intsize, bools, chars]) \textbf{then} error(ertyp)
end \textbf{else}
begin error(ertyp); cvt := intsize
end
\textbf{end else} skip([becomes, tosy, dosy]+fsys, erid);
\textbf{if} \textbf{sy =} becomes \textbf{then}
begin insymbol; expression([tosy, dosy]+fsys, x);
\textbf{if} \textbf{x. typ} \textbf{<>} cvt \textbf{then} error(ertyp);
\textbf{end else} skip([tosy, dosy]+fsys, erpun);
if $sy = \text{t}osy$ then
begin
\begin{verbatim}
insymbol; expression([dosy]+fsys, x);
if $x$. typ <> cvt then error(ertyp)
end else skip([dosy]+fsys, erkey);
$lc_1 := lc$; emit(14);
if $sy = \text{dosy}$ then insymbol else error(erkey);
$lc_2 := lc$; statement(fsys);
emit1(15, $lc_2$); code[$lc_1$]. y := lc
end (*forstatement*);
\end{verbatim}

procedure standproc($n$: integer);
\begin{verbatim}
var i, f: integer;
x, y: item;
begin
\end{verbatim}
\begin{verbatim}
case $n$ of
1, 2: begin (*read*)
if $sy = \text{i}parent$ then
begin
\end{verbatim}
\begin{verbatim}
repeat insymbol;
if $sy <> \text{ident}$ then error(erid) else begin
\end{verbatim}
\begin{verbatim}
i := loc(id); insymbol;
if $i <> 0$ then
if tab[i]. obj <> variable then error(ertyp) else begin
\end{verbatim}
\begin{verbatim}
x. typ := tab[i]. typ; x. ref := tab[i]. ref;
if tab[i]. normal then $f := 0$ else $f := 1$;
emit2($f$, tab[i]. lev, tab[i]. adr);
if $sy = \text{l}brack$ then
selector(fsus+[comma, rparent], x);
if x. typ in [ints, chars, notyp] then
emit1(27, ord(x. typ)) else error(ertyp)
end
end;
test([comma, rparent], fsys, erkey)
\end{verbatim}
\begin{verbatim}
until $sy <> \text{comma}$;
if $sy = \text{r}parent$ then insymbol else error(erpun)
end;
if $n = 2$ then emit(62)
end;
3, 4: begin (*write*)
if $sy = \text{l}parent$ then
begin
\end{verbatim}
\begin{verbatim}
repeat insymbol;
if $sy = \text{string}$ then
\end{verbatim}
begin emit1(24, sleng); emit1(28, inum); insymbol
end else
begin expression(fsys+[comma, colon, rparent], x);
if not (x. typ in stantyps) then error(ertyp);
emit1(29, ord(x. typ))
end
until sy <> comma;
if sy = rparent then insymbol else error(erpun)
end;
if n = 4 then emit(63)
end;
5, 6: (*wait, signal*)
if sy <> lparent then error(erpun) else
begin insymbol; if sy <> ident then error(erid) else
begin i := loc(id); insymbol;
if i <> 0 then if tab[i]. obj <> variable
then error(ertyp)
else
begin x. typ := tab[i]. typ; x. ref := tab[i]. ref;
if tab[i]. normal then f := 0 else f := 1;
emit2(f, tab[i]. lev, tab[i]. adr);
if sy = lbrack then selector(fsys+[rparent], x);
if x. typ = ints then emit(n+1) else error(ertyp)
end
end;
if sy = rparent then insymbol else error(erpun)
end;
end (*case*)
end (*standproc*);

begin (*statement*)
if sy in statbegsys+[ident] then
case sy of
ident: begin i := loc(id); insymbol;
if i <> 0 then
case tab[i]. obj of
konstant, type1: error(ertyp);
variable: assignment(tab[i]. lev, tab[i]. adr);
prozedure:
if tab[i]. lev <> 0 then call(fsys, i)
else standproc(tab[i]. adr);
funktion:
if tab[i]. ref = display[level] then
assignment(tab[i]. lev+1, 0) else error(ertyp)
end
begin(*block*) $dx := 5; \ ptt := t;$
if \text{level} > \text{lmax} \text{ then} \text{fatal}(5); test([lparent, colon, semicolon], fsys, erpun);
enterblock; display[level] := b; prb := b;
tab[prt].typ := notyp; tab[prt].ref := prb;
if \text{(sy = lparent) and (level > 1)} \text{ then parameterlist;\
biab[prb].lastpar := t; biab[prb].psize := dx;\
if isfun then\
if sy = colon then
begin insymbol; (*function type*)
if sy = ident then
begin $x := \text{loc(id)};\ insymbol;$
if $x \neq 0$ then
if tab[$x].obj \neq \text{type1} \text{ then error(ertyp)} \text{ else} \text{\
if tab[$x].typ in stantyps then tab[prt].typ := tab[$x].typ\
else error(ertyp)\
end else skip([[semicolon]+fsys, erid)\
end else error(erpun);
if sy = semicolon then insymbol else error(erpun);
repeat\
if sy = constsy then constantdeclaration;
if sy = typesy then typedeclaration;
if sy = varsy then variabledeclaration;
btab[prb].vsize := dx;
while sy in [proceduresy, functionsy] do procdeclaration;
test([beginsy], blockbegsys+statbegsys, erkey)
until sy in statbegsys;
tab[prt].adr := lc;
insymbol; statement([semicolon, endsy]+fsys);
while sy in [semicolon]+statbegsys do
begin if sy = semicolon then insymbol else error(erpun);
statement([semicolon, endsy]+fsys)
end;
if sy = endsy then insymbol else error(erkelay);
etest(fsys+[period], [ ], erkey);
end (*block*);

(*------------------------------------------------------------- interpret----*)

procedure interpret;
label 97, 98,
const
stepmax = 8; (*max steps before process switch*)
tru = 1; (*integer value of true*)
fals = 0; (*integer value of false*)
charl = 0; (*lowest character ordinal*)
charh = 63; (*highest character ordinal*)
type ptype = 0.. pmax; (*index over processes*)
var ir: order; (*instruction buffer*)
   ps: (*processor status*)
      (run, fin, divchk, inxchk, stkchk, linchk, lngchk, redchk, deadlock);
lncnt, (*number of lines*)
   chrcnt: integer; (*number of characters in line*)
h1, h2, h3, h4: integer; (*local variables*)
s: array[1.. stmax] of integer; (*the stack*)

(*process table—one entry for each process*)
ptab: array[ptype] of record
t,b, (*top, bottom of stack*)
   pc, (*program counter*)
   stacksize: integer; (*stack limit*)
   display: array[1.. lmax] of integer; (*0 or index of semaphore*)
   suspend: integer; (*procedure active flag*)
   active: boolean
end;
npr, (*number of concurrent processes*)
curpr: ptype; (*current process executing*)
stepcount: integer; (*number of steps before switch*)
   seed: integer; (*random seed*)
pflag: boolean; (*concurrent call flag*)

procedure setran(seed: integer); extern;
function ran: real; extern;
procedure chooseproc;
(*from a random starting point search for a process that is active and not suspended. d aborts the interpreter if a deadlock occurs.*)
var d: integer;
begin
  d := pmx + 1;
  curpr := (curpr + \text{trunc}(\text{ran}\cdot \text{pmx})) \mod \ (\text{pmx} + 1);
  \textbf{while} \ ((\text{not} \ \textit{ptab}[\textit{curpr}]. \ \textit{active})
               \ \textbf{or} \ (\textit{ptab}[\textit{curpr}]. \ \textit{suspend}<>)0))
       \ \textbf{and} \ (d >= 0) \ \textbf{do}
  \ \begin{array}{l}
    d := d - 1; \ \textit{curpr} := (\textit{curpr} + 1) \ \mod \ (\text{pmx} + 1) \ \textbf{end};
  \end{array}
  \textbf{if} \ d < 0 \ \textbf{then}
  \ \begin{array}{l}
    \textit{ps} := \text{deadlock}; \ \textbf{goto} \ 98 \ \textbf{end}
    \ \begin{array}{l}
      \textbf{else} \ \text{stepcount} := \text{trunc}(\text{ran} \cdot \text{stepmax})
    \end{array}
  \end{array}
end;

(*functions to convert integers to booleans and conversely*)
\textbf{function} \ \textit{itob}(i: \ \text{integer}): \ \text{boolean};
\begin{array}{l}
  \textbf{begin} \ \textit{i} = \text{tru} \ \textbf{then} \ \textit{itob} := \text{true} \ \textbf{else} \ \textit{itob} := \text{false} \ \textbf{end};
\end{array}
\textbf{function} \ \textit{btoi}(b: \ \text{boolean}): \ \text{integer};
\begin{array}{l}
  \textbf{begin} \ \textit{b} \ \textbf{then} \ \textit{btoi} := \text{tru} \ \textbf{else} \ \textit{btoi} := \text{fals} \ \textbf{end};
\end{array}

\textbf{begin} \ (*\ \text{interpret}*)
  \textbf{with} \ \textit{ptab}[0] \ \textbf{do} \ \textbf{begin}
  b := 0; \ \textit{suspend} := 0 \ \textit{display}[1] := 0;
  t := \textit{btab}[2]. \ \text{vs} \ - \ 1; \ \textit{pc} := \textit{tab}[s[4]]. \ \text{adr};
  \ \textit{active} := \text{true}; \ \textit{stacksize} := \text{stmax} - \text{pmx} \cdot \text{stkincr}
  \ \end{array}
\begin{array}{l}
  \textbf{end};
  \textbf{for} \ \textit{curpr} := 1 \ \textbf{to} \ \text{pmx} \ \textbf{do} \ \textbf{with} \ \textit{ptab}[\textit{curpr}] \ \textbf{do}
  \begin{array}{l}
    \textbf{begin} \ \textit{active} := \text{false}; \ \textit{display}[1] := 0; \ \textit{pc} := 0;
    \ \textit{suspend} := 0;
    b := \textit{ptab}[curpr - 1]. \ \text{stacksize} + 1; \ \textit{stacksize} := b + \text{stkincr} - 1;
    t := t - 1
  \end{array}
\end{array}
\begin{array}{l}
  \textbf{end};
  \textit{npr} := 0; \ \textit{curpr} := 0; \ \textit{pflag} := \text{false};
  \textit{seed} := \text{clock}; \ \textit{setran}(	ext{seed}); \ \textit{stepcount} := 0;
  \textit{ps} := \text{run}; \ \textit{lnct} := 0; \ \textit{chrct} := 0;
  \textbf{repeat}
  \begin{array}{l}
    \textbf{if} \ \textit{ptab}[0]. \ \textit{active} \ \textbf{then} \ \textit{curpr} := 0
    \ \begin{array}{l}
      \ \textbf{else} \ \textbf{if} \ \text{stepcount} = 0 \ \textbf{then} \ \textit{chooseproc}
    \end{array}
    \ \begin{array}{l}
      \ \textbf{else} \ \text{stepcount} := \text{stepcount} - 1;
    \end{array}
  \end{array}
  \textbf{with} \ \textit{ptab}[\textit{curpr}] \ \textbf{do} \ \textbf{begin} \ \textit{ir} := \text{code}[\textit{pc}]; \ \textit{pc} := \textit{pc} + 1 \ \textbf{end};
\textbf{if} \ \textit{pflag} \ \textbf{then}
  \begin{array}{l}
    \ \textbf{begin} \ \textbf{if} \ \textit{ir}. \ f = 18 \ (*\text{markstack}*) \ \textbf{then} \ \textit{npr} := \textit{npr} + 1;
    \ \textit{curpr} := \textit{npr}
  \end{array}
\end{array}
\textbf{end};
\textbf{with} \ \textit{ptab}[\textit{curpr}] \ \textbf{do}
\textbf{case} \ \textit{ir}. \ f \ \textbf{of}
0: begin (*load address*) \( t := t+1; \)
    if \( t > \text{stacksize} \) then \( ps := \text{stkchk} \)
    else \( s[t] := \text{display[ir.x]} + \text{ir.y} \)
    end;
1: begin (*load value*) \( t := t+1; \)
    if \( t > \text{stacksize} \) then \( ps := \text{stkchk} \)
    else \( s[t] := s[\text{display[ir.x]} + \text{ir.y}] \)
    end;
2: begin (*load indirect*) \( t := t+1; \)
    if \( t > \text{stacksize} \) then \( ps := \text{stkchk} \)
    else \( s[t] := s[s[\text{display[ir.x]} + \text{ir.y}]] \)
    end;
3: begin (*update display*)
    \( h_1 := \text{ir.y}; h_2 := \text{ir.x}; h_3 := b; \)
    repeat \( \text{display}[h_1] := h_3; h_1 := h_1 - 1; h_3 := s[h_3 + 2] \)
    until \( h_1 = h_2 \)
    end;
4: (*cobegin*) \( pflag := \text{true}; \)
5: (*coend*) begin \( pflag := \text{false}; \text{ptab[0].active} := \text{false} \) end;
6: begin (*wait*)
    \( h_1 := s[t]; t := t - 1; \)
    if \( s[h_1] > 0 \) then \( s[h_1] := s[h_1] - 1 \)
    else begin \( \text{suspend} := h_1; \text{stepcount} := 0 \) end
    end;
7: begin (*signal*)
    \( h_1 := s[t]; t := t - 1; h_2 := pmax + 1; h_3 := \text{trunc(ran*}h_2); \)
    while \( (h_3 > 0) \) and \( (\text{ptab[h_3].suspend} <> h_1) \) do
    begin \( h_3 := (h_3 + 1) \mod (pmax + 1); h_2 := h_2 - 1 \) end;
    if \( h_2 < 0 \) then \( s[h_1] := s[h_1] + 1 \) else \( \text{ptab[h_3].suspend} := 0 \)
    end;
8: case \text{ir.y} of
17: begin \( t := t+1; \)
    if \( t > \text{stacksize} \) then \( ps := \text{stkchk} \)
    else \( s[t] := \text{btoi(eof(input))} \)
    end;
18: begin \( t := t+1; \)
    if \( t > \text{stacksize} \) then \( ps := \text{stkchk} \)
    else \( s[t] := \text{btoi(eoln(input))} \)
    end;
end;
10: \( \text{pc} := \text{ir.y}; (*jump*) \)
11: begin (*conditional jump*)
    if \( s[t] = \text{false} \) then \( \text{pc} := \text{ir.y}; t := t-1 \)
    end;
14: begin (*for1up*) $h_1 := s[t-1];$
   if $h_1 <= s[t]$ then $s[s[t-2]] := h_1$ else
   begin $t := t-3; \text{pc} := \text{ir. y}$
   end
   end;
15: begin (*for2up*) $h_2 := s[t-2]; h_1 := s[h_2] + 1;$
   if $h_1 <= s[t]$ then
   begin $s[h_2] := h_1; \text{pc} := \text{ir. y}$ end
   else $t := t-3;$
   end;
18: begin $h_1 := \text{bitab[tab[ir. y]. ref]. vsize};$
   if $t+h_1 > \text{stacksize}$ then $ps := \text{stkchk}$ else
   begin $t := t+5; s[t-1] := h_1-1; s[t] := \text{ir. y}$
   end
   end;
19: begin active := true; $h_1 := t-\text{ir. y};$
   $h_2 := s[h_1+4]; \text{(*h_2 points to tab*)}$
   $h_3 := \text{tab[h_2]. lev}; \text{display[h_3+1]} := h_1;$
   $h_4 := s[h_1+3] + h_1;$
   $s[h_1+1] := \text{pc}; s[h_1+2] := \text{display[h_3]};$
   if $\text{pflag}$ then $s[h_1+3] := \text{ptab[0]. b}$ else $s[h_1+3] := b;$
   for $h_3 := t+1$ to $h_4$ do $s[h_3] := 0;$
   $b := h_1; t := h_4; \text{pc} := \text{tab[h_2]. adr}$
   end;
21: begin (*index*) $h_1 := \text{ir. y}; \text{(*h_1 points to atab*)}$
   $h_2 := \text{atab[h_1]. low}; h_3 := s[t];$
   if $h_3 < h_2$ then $ps := \text{inxchk}$ else
   if $h_3 > \text{atab[h_1]. high}$ then $ps := \text{inxchk}$ else
   begin $t := t-1; s[t] := s[t] + (h_3-h_2)\ast atab[h_1]. elsize$
   end
   end;
22: begin (*load block*) $h_1 := s[t]; t := t-1;$
   $h_2 := \text{ir. y + t};$ if $h_2 > \text{stacksize}$ then $ps := \text{stkchk}$ else
   while $t < h_2$ do
   begin $t := t+1; s[t] := s[h_1]; h_1 := h_1+1$
   end
   end;
23: begin (*copy block*) $h_1 := s[t-1];$
   $h_2 := s[t]; h_3 := h_1 + \text{ir. y};$
   while $h_1 < h_3$ do
   begin $s[h_1] := s[h_2]; h_1 := h_1+1; h_2 := h_2+1$
   end;
   $t := t-2$
   end;
24: begin (*literal*) \( t := t + 1; \)
    if \( t > \text{stacksize} \) then \( ps := \text{stkchk} \) else \( s[t] := \text{ir}. y \)
    end;
27: begin (*read*)
    if \( \text{eof(input)} \) then \( ps := \text{redchk} \) else
        case \( \text{ir}. y \) of
            1: \( \text{read}(s[s[t]]) \);
            3: begin \( \text{read}(ch) \); \( s[s[t]] := \text{ord}(ch) \) end;
        end;
    \( t := t - 1 \)
end;
28: begin (*write string*)
    \( h_1 := s[t] \); \( h_2 := \text{ir}. y \); \( t := t - 1 \);
    \( \text{chrcnt} := \text{chrcnt} + h_1 \); if \( \text{chrnt} > \text{lineleng} \) then \( ps := \text{lnghck} \);
    repeat \( \text{write}(\text{stab}[h_2]) \); \( h_1 := h_1 - 1 \); \( h_2 := h_2 + 1 \)
    until \( h_1 = 0 \)
end;
29: begin (*write1*)
    if \( \text{ir}. y = 3 \) then \( h_1 := 1 \) else \( h_1 := 10 \);
    \( \text{chrnt} := \text{chrnt} + h_1 \);
    if \( \text{chrnt} > \text{lineleng} \) then \( ps := \text{lnghck} \) else
        case \( \text{ir}. y \) of
            1: \( \text{write}(s[t]) \);
            2: \( \text{write}(\text{itob}(s[t])) \);
            3: if \( (s[t]<\text{charl}) \) or \( (s[t]>\text{charh}) \) then \( ps := \text{inxc}! \kappa \)
                else \( \text{write}(\text{chr}(s[t])) \)
        end;
    \( t := t - 1 \)
end;
31: \( ps := \text{fin} \);
32: \( t := b - 1 \); \( pc := s[b + 1] \);
    if \( pc <> 0 \) then \( b := s[b + 3] \) else
        begin \( \text{npr} := \text{npr} - 1 \); \( \text{active} := \text{false} \);
            \( \text{stepcount} := 0 \); \( \text{ptab}[0]. \text{active} := (\text{npr} = 0) \)
        end
end;
33: begin (*exit function*)
    \( t := b \); \( pc := s[b + 1] \); \( b := s[b + 3] \)
end;
34: \( s[t] := s[s[t]] \);
35: \( s[t] := \text{btob}(\text{not}(\text{itob}(s[t]))) \);
36: \( s[t] := -s[t] \);
38: begin (*store*) \( s[s[t - 1]] := s[t] \); \( t := t - 2 \) end;
45: begin \( t := t - 1 \); \( s[t] := btoi(s[t] = s[t+1]) \) end;
46: begin \( t := t - 1 \); \( s[t] := btoi(s[t] <> s[t+1]) \) end;
47: begin \( t := t - 1 \); \( s[t] := btoi(s[t] < s[t+1]) \) end;
48: begin \( t := t - 1 \); \( s[t] := btoi(s[t] <= s[t+1]) \) end;
49: begin \( t := t - 1 \); \( s[t] := btoi(s[t] > s[t+1]) \) end;
50: begin \( t := t - 1 \); \( s[t] := btoi(s[t] >= s[t+1]) \) end;
51: begin \( t := t - 1 \); \( s[t] := btoi(itob(s[t]) or itob(s[t+1]) \) end;
52: begin \( t := t - 1 \); \( s[t] := s[t] + s[t+1] \) end;
53: begin \( t := t - 1 \); \( s[t] := s[t] - s[t+1] \) end;
54: begin \( t := t - 1 \); \( s[t] := btoi(itob(s[t]) and itob(s[t+1])) \) end;
55: begin \( t := t - 1 \); \( s[t] := s[t] * s[t+1] \) end;
56: begin \( t := t - 1 \);
   if \( s[t+1] = 0 \) then \( ps := divchk \) else
   \( s[t] := s[t] \div s[t+1] \)
end;
57: begin \( t := t - 1 \);
   if \( s[t+1] = 0 \) then \( ps := divchk \) else
   \( s[t] := s[t] \mod s[t+1] \)
end;
58: if \( \text{eof(input)} \) then \( ps := \text{rechk} \) else readln;
59: begin writeln; lnent := lnent + 1; chrnt := 0;
   if \( \text{lncnt} > \text{linelimt} \) then \( ps := \text{linchk} \)
   end
   (*case*);
until \( ps <> \text{run} \);
60: writeln;
61: if \( ps <> \text{fin} \) then begin
with ptab[curpr] do
   write(#0halt at#, pc:5,# in process#, curpr:4, # because of #);
   case \( ps \) of
      deadlock: writeln(#deadlock#);
      divchk: writeln(#division by 0#);
      inxchk: writeln(#invalid index#);
      stkchk: writeln(#storage overflow#);
      linchk: writeln(#too much output#);
      lngchk: writeln(#line too long#);
      redchk: writeln(#reading past end of file#);
   end;
   writeln(#0process active suspend pc#);
   for \( h_1 := 0 \) to pmax do with ptab[\( h_1 \)] do
      writeln(#0#, h_1: 4, active, suspend, pc);
   writeln(#0global variables#);
for \( h_1 := biab[1]. \text{last} + 1 \) to \( \text{imax} \) do

with \( \text{tab}[h_1] \) do if \( \text{lev} <> 1 \) then goto 97

else if \( \text{obj} = \text{variable} \) then if \( \text{typ} \in \text{stantyps} \) then

case \( \text{typ} \) of

- \( \text{ints} : \text{writeln} \( \text{name}, \#, = \#, s[\text{adr}] \) ; \)
- \( \text{bools} : \text{writeln} \( \text{name}, \#, = \#, \text{itob}(s[\text{adr}]) \) ; \)
- \( \text{chars} : \text{writeln} \( \text{name}, \#, = \#, \text{chr}(s[\text{adr}] \mod 64) \) ; \)

end;

97: writeln

end (*interpret*);

(* --------------------------------------------------- main---* )

begin (*main*)

\( \text{message}(\# - \text{concurrent pascal-s#}); \)

\( \text{key[1]} := \#\text{and} \# ; \)
\( \text{key[2]} := \#\text{array} \# ; \)
\( \text{key[3]} := \#\text{begin} \# ; \)
\( \text{key[4]} := \#\text{cobegin} \# ; \)
\( \text{key[5]} := \#\text{coend} \# ; \)
\( \text{key[6]} := \#\text{const} \# ; \)
\( \text{key[7]} := \#\text{div} \# ; \)
\( \text{key[8]} := \#\text{do} \# ; \)
\( \text{key[9]} := \#\text{else} \# ; \)
\( \text{key[10]} := \#\text{end} \# ; \)
\( \text{key[11]} := \#\text{for} \# ; \)
\( \text{key[12]} := \#\text{function} \# ; \)
\( \text{key[13]} := \#\text{if} \# ; \)
\( \text{key[14]} := \#\text{mod} \# ; \)
\( \text{key[15]} := \#\text{not} \# ; \)
\( \text{key[16]} := \#\text{of} \# ; \)
\( \text{key[17]} := \#\text{or} \# ; \)
\( \text{key[18]} := \#\text{procedure} \# ; \)
\( \text{key[19]} := \#\text{program} \# ; \)
\( \text{key[20]} := \#\text{repeat} \# ; \)
\( \text{key[21]} := \#\text{then} \# ; \)
\( \text{key[22]} := \#\text{to} \# ; \)
\( \text{key[23]} := \#\text{type} \# ; \)
\( \text{key[24]} := \#\text{until} \# ; \)
\( \text{key[25]} := \#\text{var} \# ; \)
\( \text{key[26]} := \#\text{while} \# ; \)
\( \text{ksy[1]} := \text{andsy} ; \)
\( \text{ksy[2]} := \text{arraysys} ; \)
\( \text{ksy[3]} := \text{beginsy} ; \)
\( \text{ksy[4]} := \text{beginsys} ; \)
\( \text{ksy[5]} := \text{endsy} ; \)
\( \text{ksy[6]} := \text{constsy} ; \)
\( \text{ksy[7]} := \text{idiv} ; \)
\( \text{ksy[8]} := \text{dosy} ; \)
\( \text{ksy[9]} := \text{elsesy} ; \)
\( \text{ksy[10]} := \text{endsys} ; \)
\( \text{ksy[11]} := \text{forsy} ; \)
\( \text{ksy[12]} := \text{functionsy} ; \)
\( \text{ksy[13]} := \text{ifsy} ; \)
\( \text{ksy[14]} := \text{imod} ; \)
\( \text{ksy[15]} := \text{notsy} ; \)
\( \text{ksy[16]} := \text{ofsy} ; \)
\( \text{ksy[17]} := \text{orsy} ; \)
\( \text{ksy[18]} := \text{proceduresy} ; \)
\( \text{ksy[19]} := \text{programsy} ; \)
\( \text{ksy[20]} := \text{repeatsy} ; \)
\( \text{ksy[21]} := \text{thensy} ; \)
\( \text{ksy[22]} := \text{tossy} ; \)
\( \text{ksy[23]} := \text{typesy} ; \)
\( \text{ksy[24]} := \text{untilsy} ; \)
\( \text{ksy[25]} := \text{varsy} ; \)
\( \text{ksy[26]} := \text{whilesy} ; \)
sps[#++] := plus;  sps[#--] := minus;
sps[#++] := lparent;  sps[#]# := rparent;
sps[#==] := eql;  sps[#.,#] := comma;
sps[#[]} := lbrack;  sps[#}#] := rbrack;
sps[#*#] := neq;  sps[#&#] := andsy;
sps[#;#] := semicolon;  sps[#**#] := times;

constbegsys := [plus, minus, intcon, charcon, ident];
typebegsys := [ident, arraysy];
blockbegsys := [constsy, typesy, varsy, proceduresy, functionsy, beginsy];
facbegsys := [intcon, charcon, ident, lparent, notsy];
statbegsys := [beginsy, ifsy, whilesy, repeatesy, forsy];
stantyps := [notyp, ints, bools, chars];
lc := 0; ll := 0; cc := 0; ch := # #;
errpos := 0; errs := [ ]; insymbol;
t := -1; a := 0; b := 1; sx := 0; c_2 := 0;
display[0] := 1;
skipflag := false;

if sy <> programsy then error(erkey) else
begin insymbol;
  if sy <> ident then error(erid) else
  begin proiname := id; insymbol; end
end;

enter(# #, variable, notyp, 0); (*sentinel*)
enter(#false #, konstant, bools, 0);
enter(#true #, konstant, bools, 1);
enter(#char #, type1, chars, 1);
enter(#boolean #, type1, bools, 1);
enter(#integer #, type1, ints, 1);
enter(#eof #, funktion, bools, 17);
enter(#eoln #, funktion, bools, 18);
enter(#read #, prozedure, notyp, 1);
enter(#readln #, prozedure, notyp, 2);
enter(#write #, prozedure, notyp, 3);
enter(#writeln #, prozedure, notyp, 4);
enter(#wait #, prozedure, notyp, 5);
enter(#signal #, prozedure, notyp, 6);
enter(# #, prozedure, notyp, 0);

with riab[1] do
begin last := t; lastpar := 1; psize := 0; vsize := 0
end;
block(blockbegsys+statbegsys, false, 1);
if sy <> period then error(erpun);
if btab[2]. vsize > stmax−stkincr * pmax then error(ernl);
emit(31); (*halt*)
if not eof(input) then readln;
if errs = [ ] then interpret else errormsg;
99: writeln
end.
BIBLIOGRAPHY

TEXTBOOKS

Concurrent programming is an abstraction of the type of programming that is common in operating systems, and in fact its study is rooted in the difficulties that were encountered in programming operating systems. Thus it is not surprising that other books on this subject deal with operating systems and conversely that books on operating systems usually have a short chapter on concurrent programming. Exceptions are the texts by Holt et al. (1978) and Brinch Hansen (1973). The text by Holt describes the construction and use of the CSP/k system for exercising concurrency. CSP/k uses monitors. The text contains a good description of monitor programming and of implementation of concurrency. Its treatment of other synchronization primitives is sketchy.

Brinch Hansen's text is addressed to about the same level as this book. His discussion emphasizes the conditional critical region.

Books on operating systems are those by Tischritzis and Bernstein (1974) at an elementary level, by Brinch Hansen (1973) and Habermann (1976) at an intermediate level, and by Coffman and Denning (1973) at an advanced level.

One of my favorite books is Brinch Hansen (1977) which contains a description of the language Concurrent Pascal (which uses monitors) and the design and listing of three operating systems.

For an introduction to Pascal, the original reference manual is that by Jensen and Wirth (1975); there are numerous newer texts such as that by Welsh and Elder (1979). An introduction to preliminary Ada is provided by Wegner (1980). There is a newer text by Pyle (1981). For the design and construction of programs see Welsh and McKeag (1980).

SOURCES

The preliminary report on the Ada language is Ichbiah (1979). The manual of the revised language is available from the U.S. Superintendent of Documents, Washington, D.C. Most of the rest of the text is based on the excellent articles by Dijkstra (1968b) and Hoare (1974) both of which should be read. The dining philosophers are discussed in Dijkstra (1971) and Hoare and Perrott (1972).
Conway’s problem is in Conway (1963) and appears again later in Hoare (1978). While Hoare’s system CSP was the basis for the Ada synchronization primitives, CSP is different and worth learning. Most current theoretical work is being done on CSP rather than Ada: Francez (1980) and Apt, Francez and de Roever (1980). Guarded commands were invented by Dijkstra (1975). Another formalism for distributed synchronization has been published by Brinch Hansen (1978).

Lamport’s bakery algorithms are described and proved in his papers of 1974, 1977 and 1979. The exercise attributed to Roussel is found in Kowalski (1979). The appendix is based on a program that the Author has used for class exercise for several years. A short description of a preliminary version was published in Ben-Ari (1981). The Pascal-S report has been reprinted in Barron (1981). More sophisticated systems are described in Holt et al. (1978) and Kaubisch et al. (1976). If you have access to Concurrent Pascal (Brinch Hansen, 1977), that is preferable.

The proofs of the programs in the text are semi-formal expositions of formal proofs I have been working on using temporal logic. If this interests you, places to start are Manna and Pnueli (1979) for sequential programs and Pnueli (1981) for concurrent programs. Compare the proof of Dekker’s Algorithm given in this book with that in the article by Francez and Pnueli (1978). For another approach to proving concurrent programs see Owicki and Gries (1976).

To test your knowledge of concurrent programming, make the effort needed to understand the mutual exclusion algorithm in Morris (1979).


Lamport, L., “A new approach to proving the correctness of multiprocess programs”, *ACM Trans. on Programming Languages and Systems*, 1, 84–97 (1979).


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